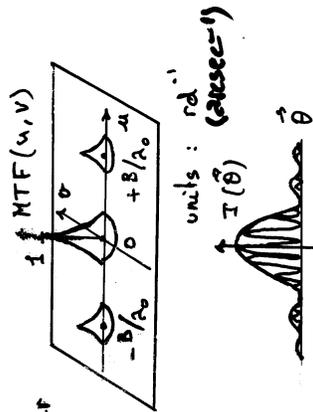


6. Types of interferometers

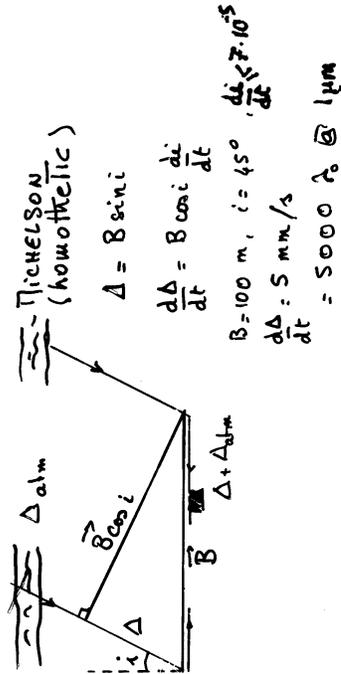
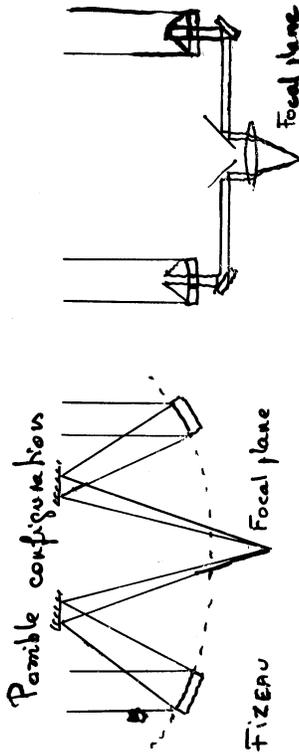
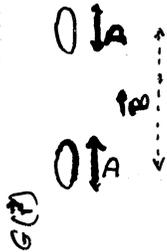
- MTF of a real interferometer
- The Fizeau recombination
- The classical Michelson recombination
- Other methods to carry the radiation phase
 - single-mode optical fibers
 - heterodyning the radiation
- Delay lines, coherencing or cophasing
- Field-of-view of an interferometer
- Polarisation effects
- The *densified pupil* Michelson recombination

Summer school on Space and Ground-based Optical Interferometry - Leiden, Sept. 18-22, 2000 - page 7

26



The real interferometer



Michelson (homothetic)

$$\Delta = B \sin i$$

$$\frac{d\Delta}{dt} = B \cos i \frac{di}{dt}$$

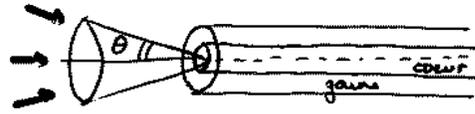
$$B = 100 \text{ m}, i = 45^\circ, \frac{di}{dt} \leq 7 \cdot 10^{-5}$$

$$\frac{d\Delta}{dt} = 5 \text{ mm/s}$$

$$= 5000 \lambda @ 1 \mu\text{m}$$

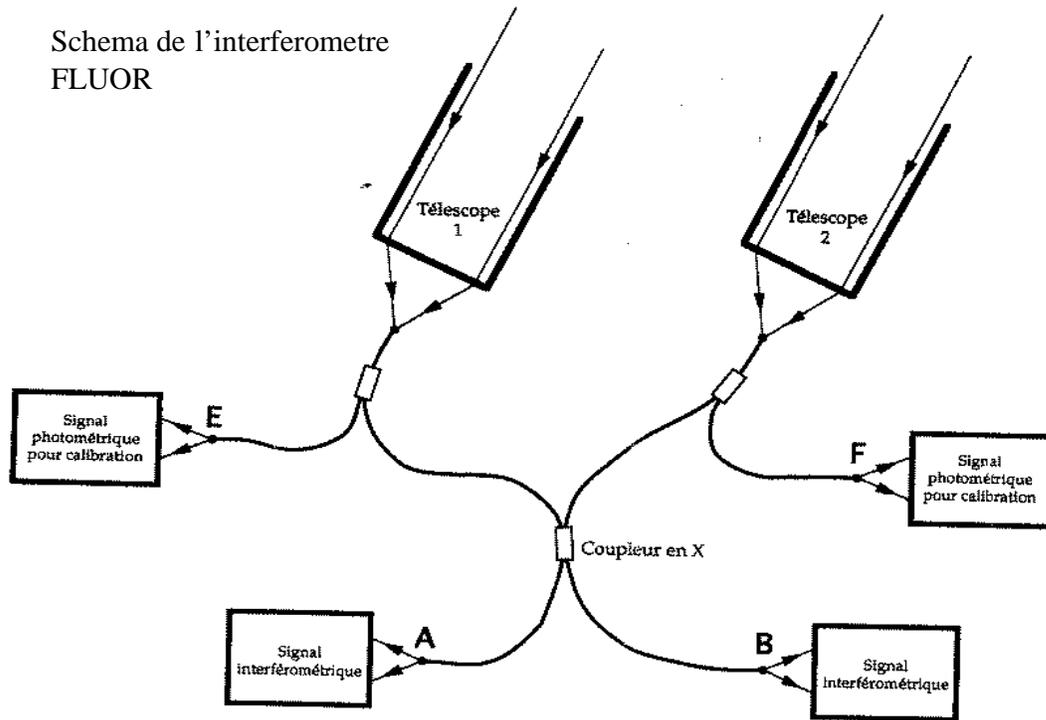
Fibres optiques

- ouverture numérique : $\sin \theta = (n_{\text{coeur}}^2 - n_{\text{gaine}}^2)^{1/2}$

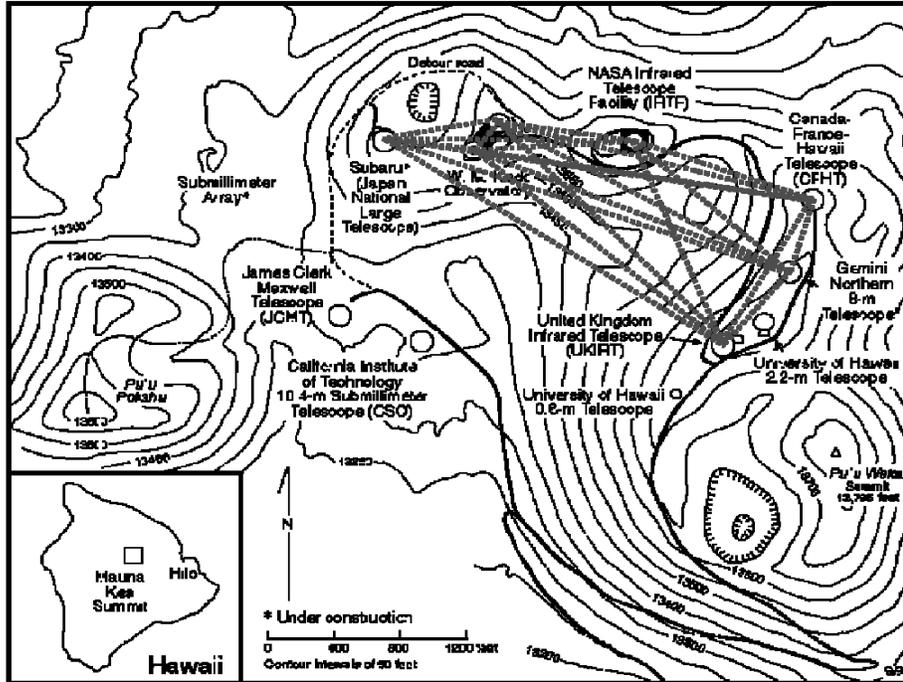


- atténuation db/km : $-10 \log \frac{I_{\text{out}}}{I_{\text{in}}}$
- longueur d'onde de coupure (monomode) λ_c
 - $\lambda < \lambda_c$: propage
 - $\lambda > \lambda_c$: non-propage
- efficacité de couplage
- polarisation

Schema de l'interferometre FLUOR



Coude du Foresto, Ridgway, Mariotti



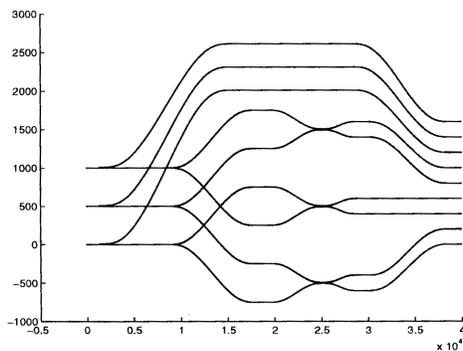
$$D=400m : \lambda/D = 2 \text{ mas @ } 4\mu m$$

$$\lambda/D = 20 \text{ mas @ } 40\mu m$$

From J. M. Mariotti et al. : Interferometric connection of large ground-based telescopes

3 telescope beam combiners: 2 examples under development

Coaxial scheme:

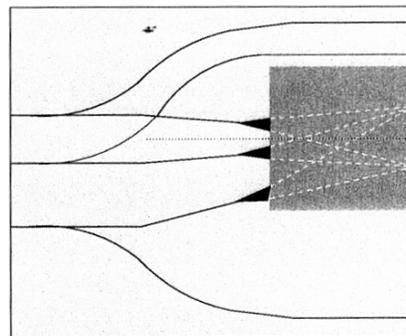


Main characteristics:

- Temporal encoding of fringes (coaxial combination).
- Pairwise beam combination.

(Severi et al, Torino,1999)

Multiaxial scheme:

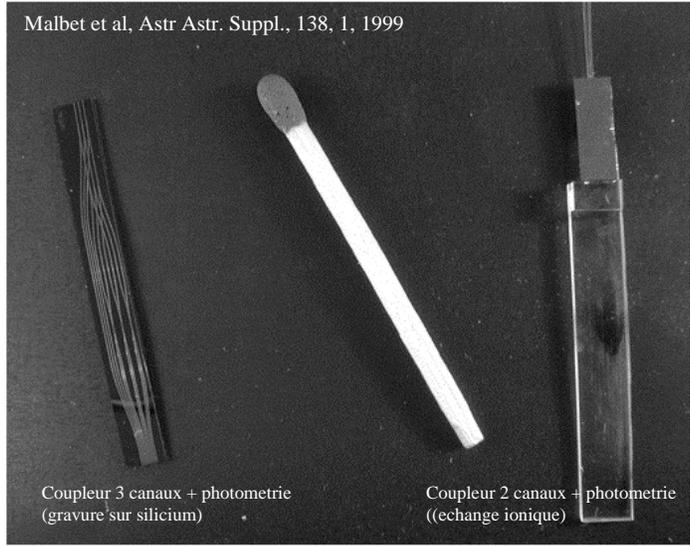


Main characteristics:

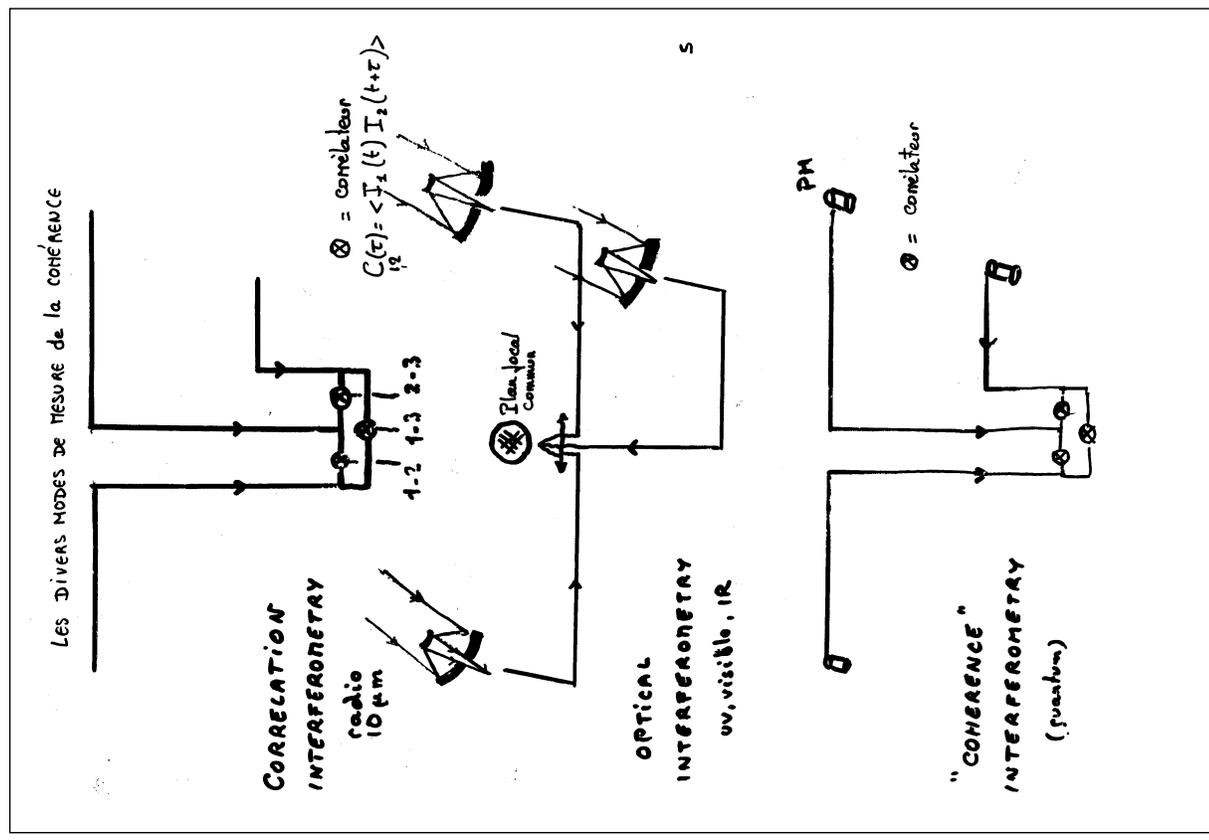
- Spatial encoding of fringes.
- Alltogether beam combination.

SFO - Bordeaux - 7 septembre 1999

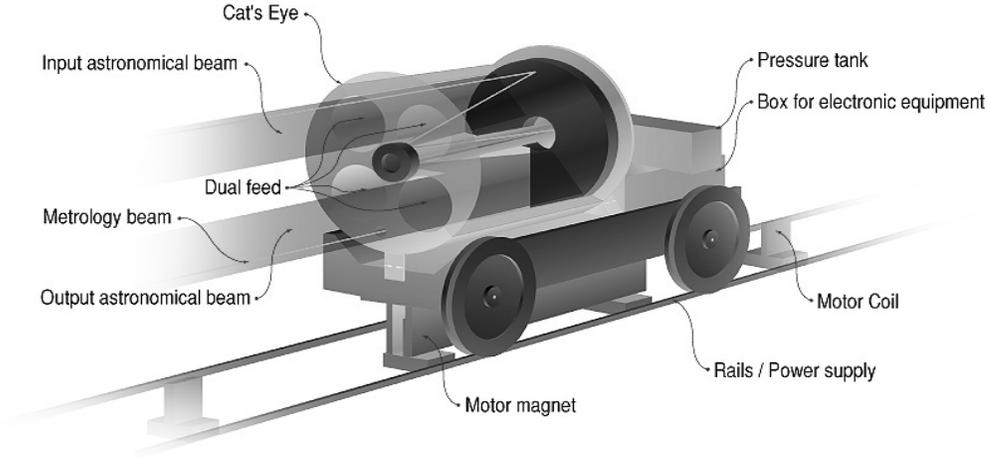
Optique intégrée : fonctions de recombinaison d'un interféromètre



J-Ph. Berger, These, Universite Joseph Fourier, 199 (LAOG)



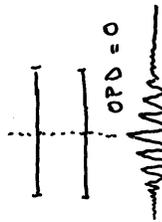
The VLTI Delay Line



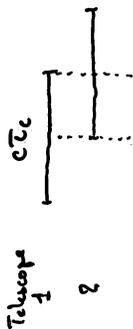
Retroreflector (Ritchey-Chretien type, "cat's eye") mounted on a moving carriage.

- OPD range: > 120 meters
- OPD resolution: < 20 nm
- Maximum velocity: 0.5 m/sec
- Velocity accuracy: 1 $\mu\text{m}/\text{sec}$
- Field of view: 200 arcsec

Co-phasing



Coherencing



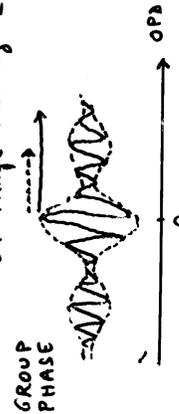
No dispersion = vacuum line
no strength differential effect

K band: $\lambda_0 = 2.2 \mu\text{m}$ $\Delta\lambda_0 / \lambda_0 \sim 0.1$
 $\nu_0 = 1.5 \cdot 10^{14} \text{ Hz}$ $\tau_c \sim 10^{-13} \text{ s}$

Heterodyne: $\lambda_0 = 10.6 \mu\text{m}$ $c\tau_c = 30 \mu\text{m}$
 $\Delta\nu_0 \sim 3 \text{ GHz}$ $\Delta\nu_0 / \nu_0 \sim 10^{-4}$ $c\tau_c = 3 \text{ cm}$

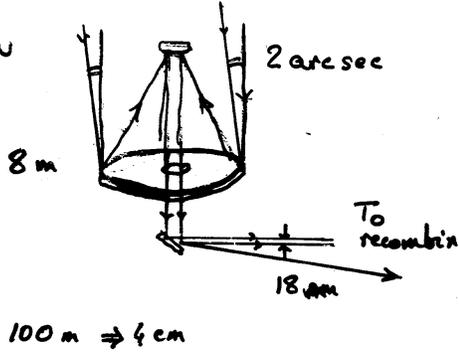
Steps with metrology

1. Coherencing = Find the fringes
2. Co-phasing = find the OPD
3. Fringe tracking = Follow the OPD (Earth + atmosphere) which algorithm if dispersion



6.3

Field of view



$$2'' = 10^{-5} \text{ rad}$$

$$10^{-5} \times \frac{8}{0.18} \sim 4.4 \cdot 10^{-4} \text{ rad}$$

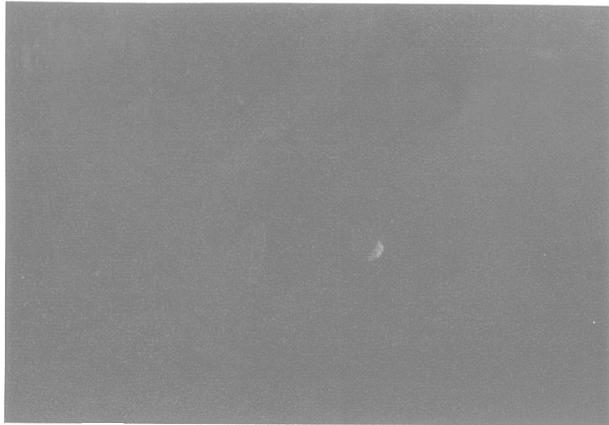
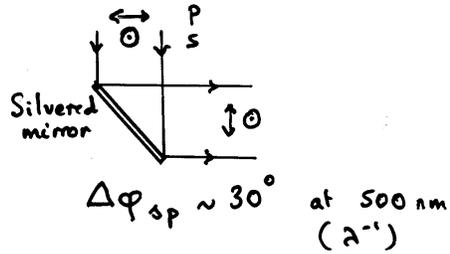
over 100 m \Rightarrow 4 cm

Field of view is a serious concern in optical interferometry

Polarization

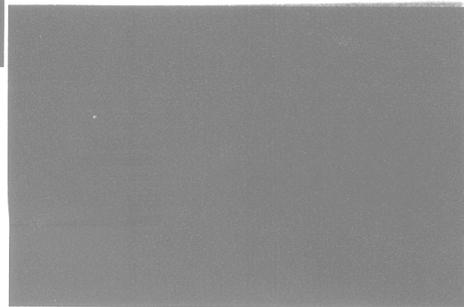
loss :

$$V_{pol} = \cos \left| \frac{\varphi_s - \varphi_p}{2} \right|$$



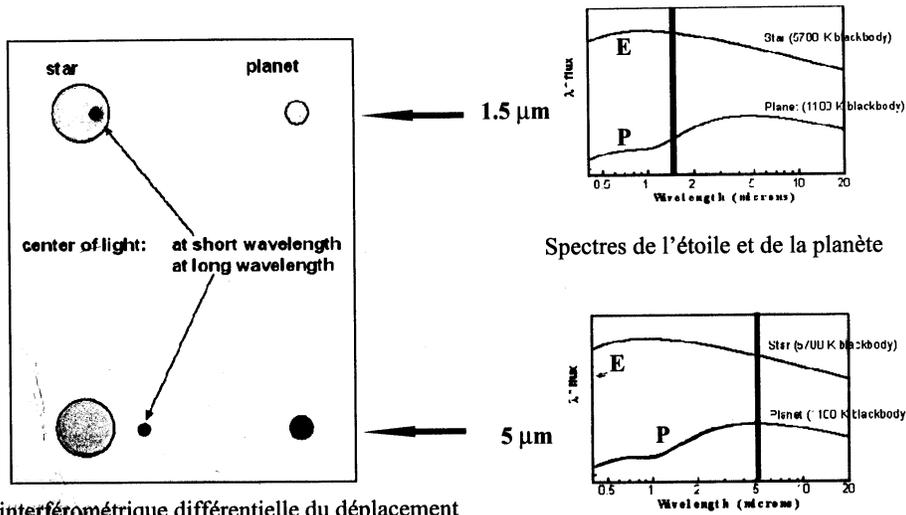
0.04 pc = 20''

Protoplanetary young discs in Orion
HST - O'Dell - 1998



600 u.a. = 6''

Détection directe (1) : photocentre étoile-planète



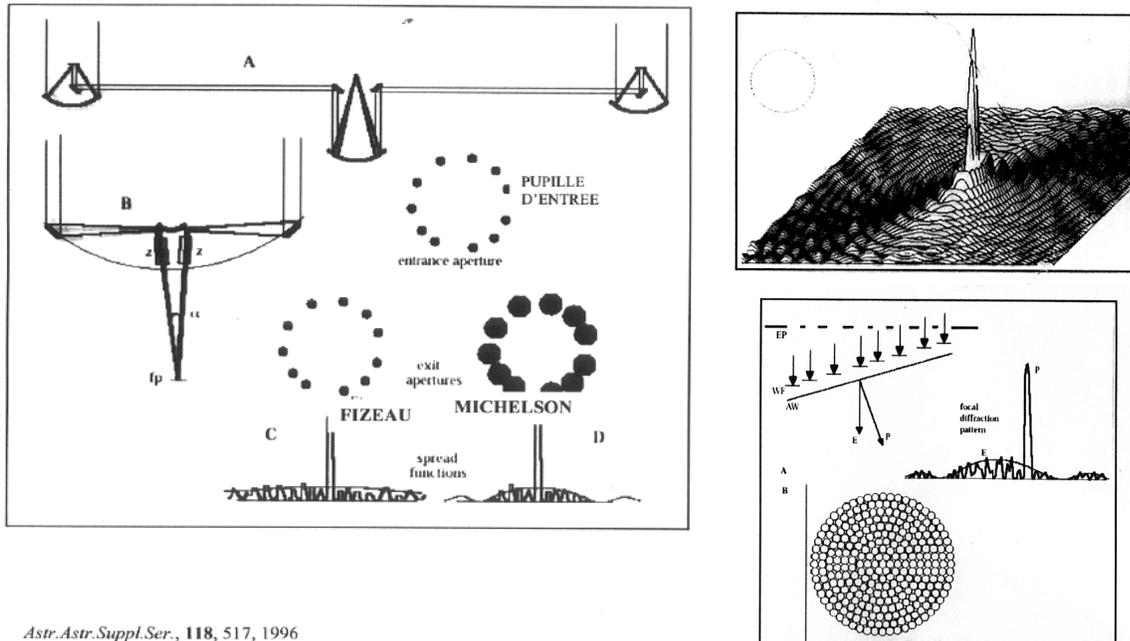
Spectres de l'étoile et de la planète

Mesure interférométrique différentielle du déplacement du photocentre étoile-planète à deux longueurs d'onde

Source : The Keck Interferometer, Science Requirements Document, Rév. 2.2, May 98, G. van Belle & G. Vashist

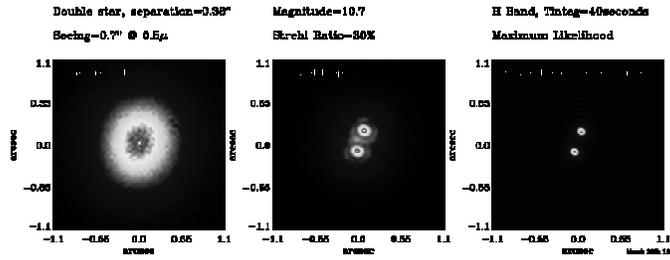
- "Jupiters" chauds (1300-600 K) à $\lambda = 1.6-10 \mu\text{m}$
- distance 0.15 au de l'étoile, éloignée de $< 10 \text{ pc}$
- magnitude $K < 10$: 1000 étoiles cibles
- résolution spectrale 100 : $\text{CH}_4, \text{H}_2\text{O}, \text{NH}_3$
- précision différentielle : 10^{-3} radians

Imagerie par densification de pupille (5) (Labeyrie 1996)



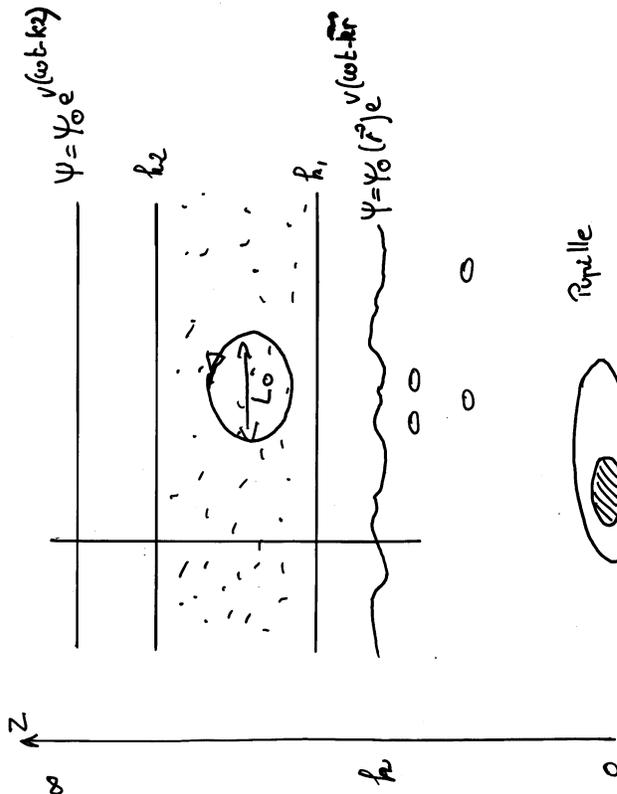
Astr. Astr. Suppl. Ser., 118, 517, 1996

CFHT Adaptive Optics Bonnette & Monica



7. Effects of the Earth's atmosphere

- Overview on atmospheric coherence loss
- Parameters : $r_0(\lambda)$, $\tau_0(\lambda)$, $\theta_0(\lambda)$, L_0 , l_0
- Adaptive optics, principle
 - Zernike polynomials description of wavefront
 - Strehl ratio S
- Effects on interferometric observables
 - speckled fringes and visibility degradation
 - piston noise
- Fringe dispersion & group delay

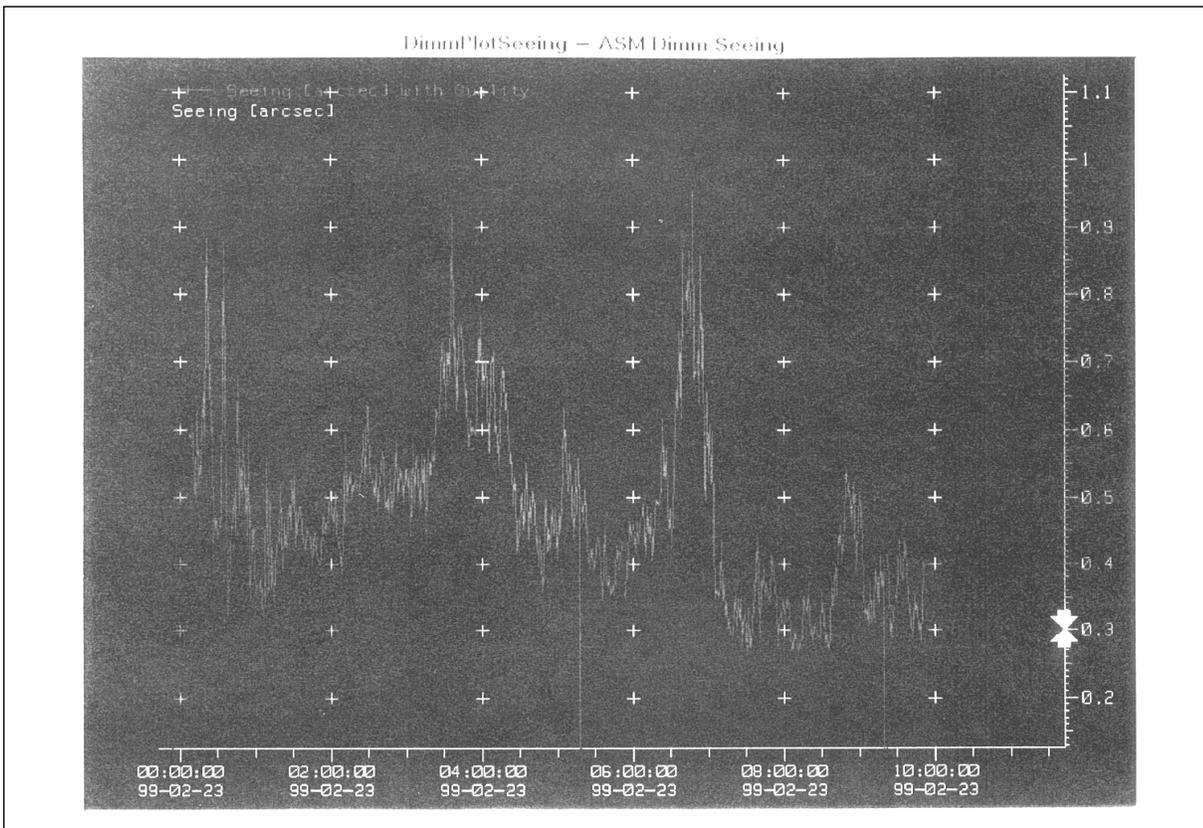
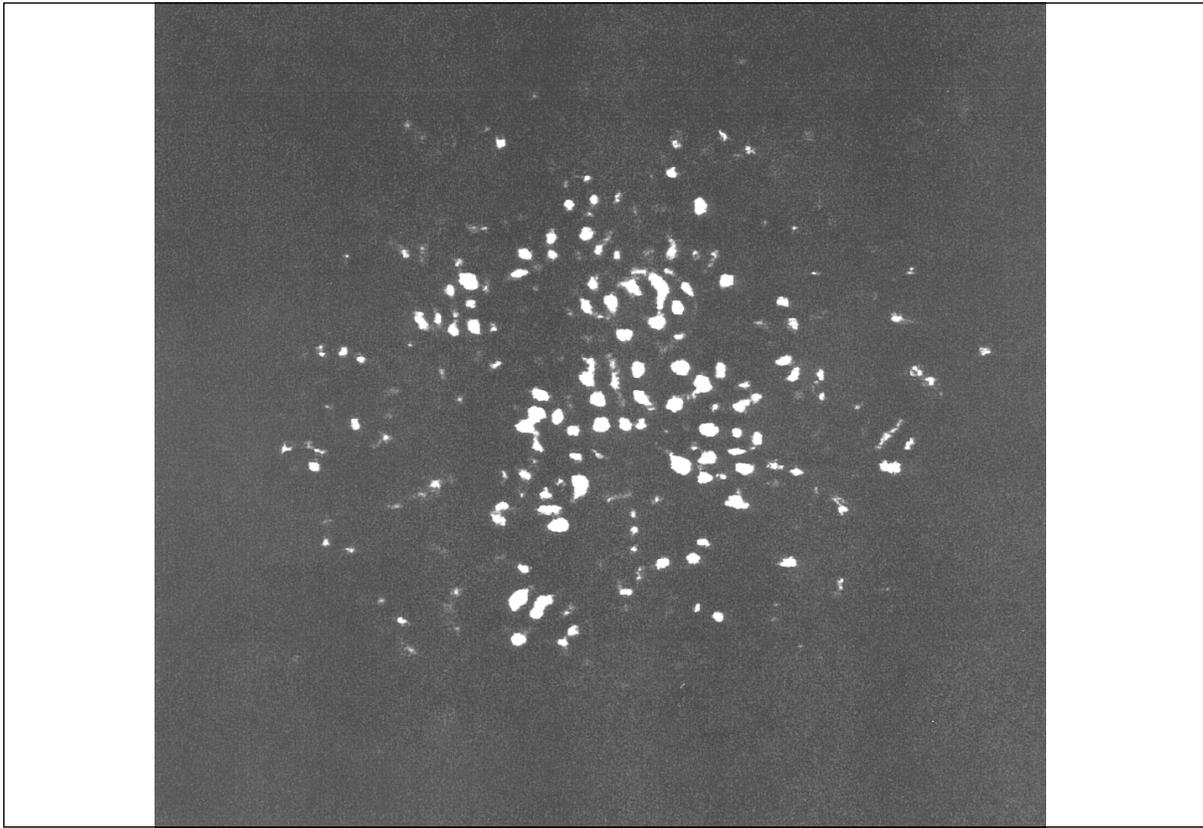


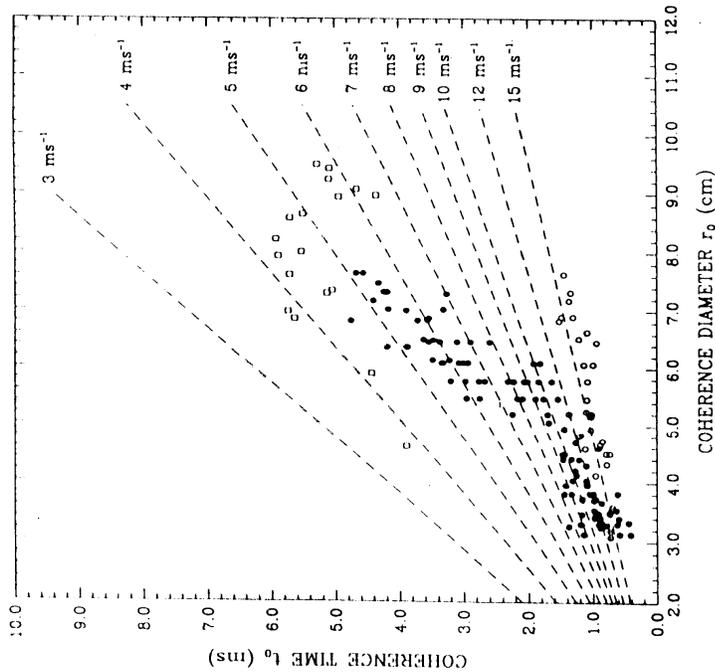
Atmospheric OTF :

average over time $\langle H_{atm}(f) \rangle = \exp -3.44 \left(\frac{\lambda f}{r_0} \right)^{5/3}$

$$r_0(\lambda) \approx \left[\frac{16}{\lambda^2} \frac{1}{\cos^2 i} \cdot \int_0^L C_n^2 dh \right]^{-3/5}$$



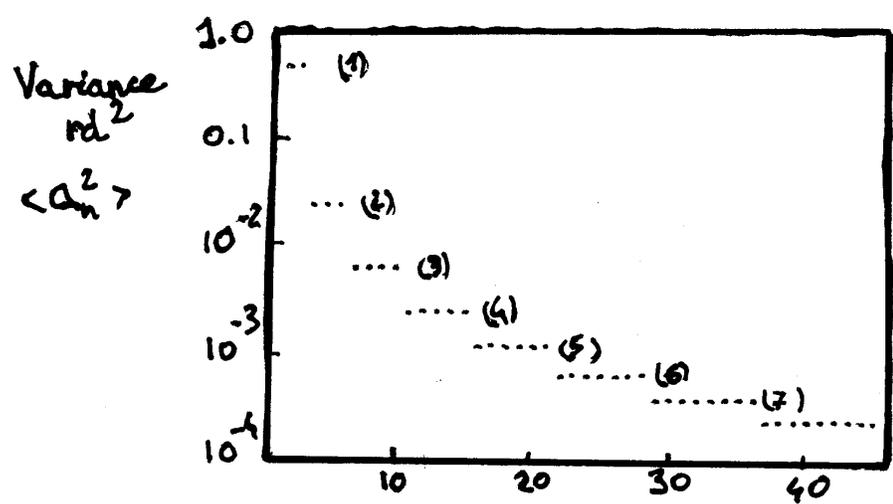




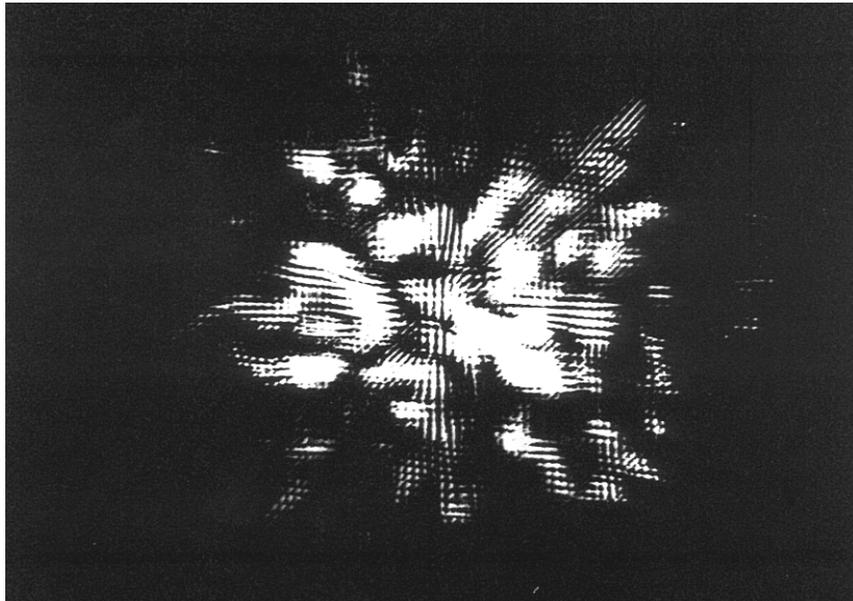
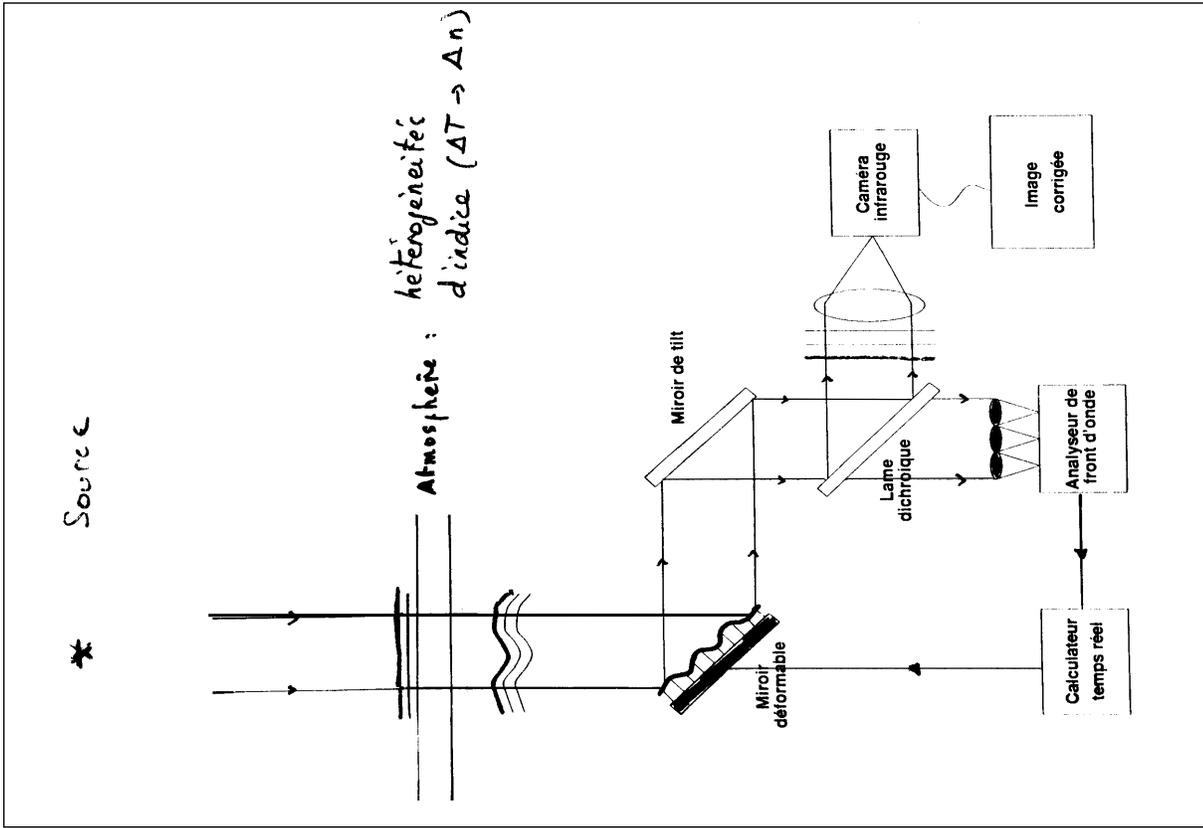
$$t_0 = 0.314 \frac{r_0}{V}$$

where V is the "average windspeed" carrying the turbulent layers past the interferometer.

Chatterton Astronomy Department



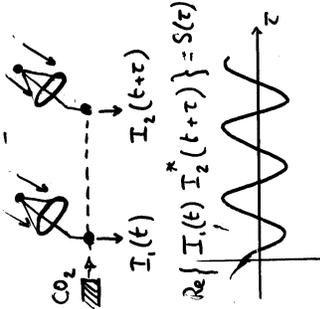
$L_0 = \infty$, donc indépendant du diamètre D
 Si $L_0 \downarrow$, $\langle a_n^2 \rangle \downarrow$



Simulation: focal plane of 3 UTs
coherent coupling without adaptive optics

**Interferometre ISI
Infrared Spatial Interferometer)
Berkeley/Mt Wilson**

$\lambda = 10.6 \mu\text{m}$
Oscillateur local = laser CO_2



$\Delta t = \text{temps de pose} = 270 \text{ s}$

$(1/\Delta t) \approx 0.004 \text{ Hz}$

L'élargissement de la DSP à mi-hauteur est dû à une modulation de fréquence aléatoire de $S(\tau)$: effet d'accordéon.

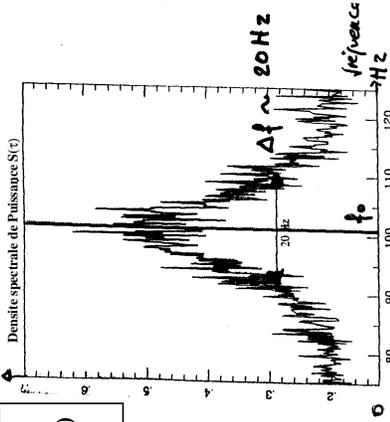
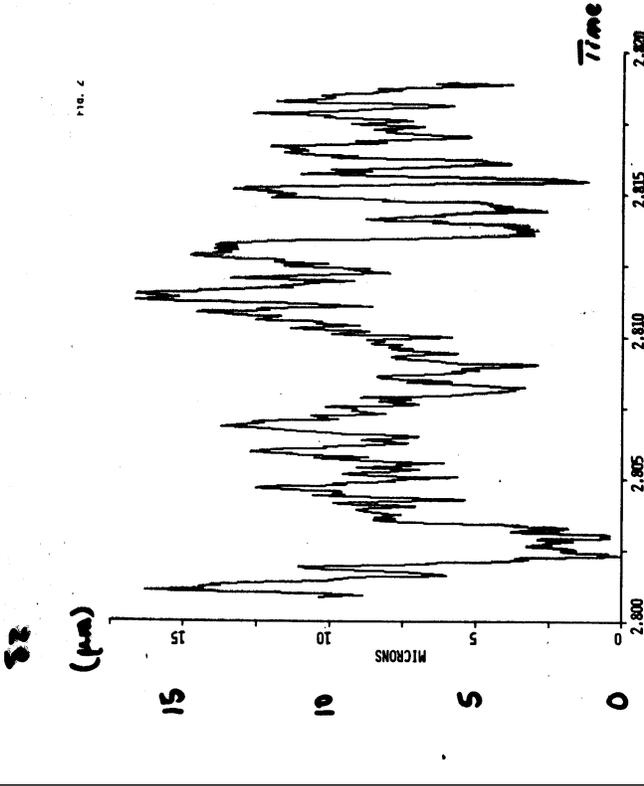
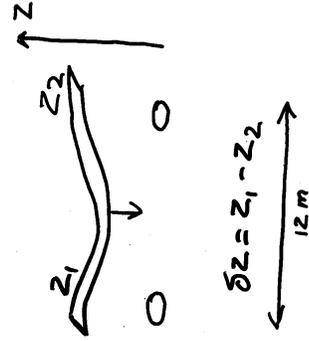


Figure 4-31 Densité spectrale de puissance du signal interférométrique (franges) obtenu par l'interféromètre hétérodyné à $10.6 \mu\text{m}$ ISI sur l'étoile α Orionis en 1992. La fréquence des franges, proche de 100 Hz, est fixée par la rotation de la Terre, la position de la source dans le ciel et la base B (longueur et orientation). Cet enregistrement est particulier car durant cette période d'observation l'atmosphère introduit une phase aléatoire importante et variable dans les franges, ce qui se traduit par un élargissement de la densité spectrale et une diminution corrélative de son amplitude. D'après Towles C. H. et al., *Infrared Physics*, 36, 1994.



Time
HOURS UT
18.0

Fig. 3



4

Visibility loss in interferometry due to atmospheric phase changes



$\varphi_1(\vec{r}, t)$ $\varphi_2(\vec{r}, t + \tau)$

Modulated signal:

$$I(\vec{r}, \tau) = 2 \operatorname{Re} \llbracket A_1(\vec{r}, \sigma, t) e^{i\varphi_1(\vec{r}, \sigma, t)} A_2^*(\vec{r}, \sigma, t + \tau) e^{-i\varphi_2(\vec{r}, \sigma, t + \tau)} \rrbracket$$

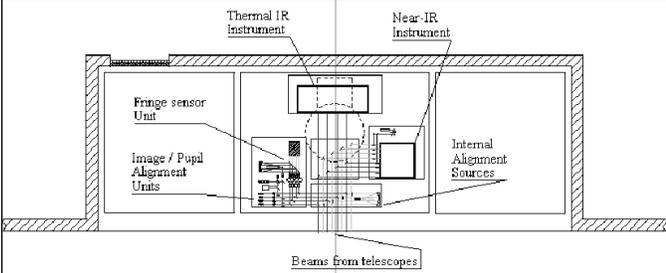
T exposure time (\ll atmospheric time)
 \vec{r} point on pupil's aperture
 σ wave number ($6/\lambda$)
 A_1, A_2 amplitudes
 τ delay between the two waves

$$I(\vec{r}, \tau) = \frac{\pi D^2}{2} \cos(\omega\tau) \operatorname{Re} \llbracket A_1 A_2^* \rrbracket e^{i(\varphi_1 - \varphi_2)}$$

$=$ Visibility \times Contrast $\times C$

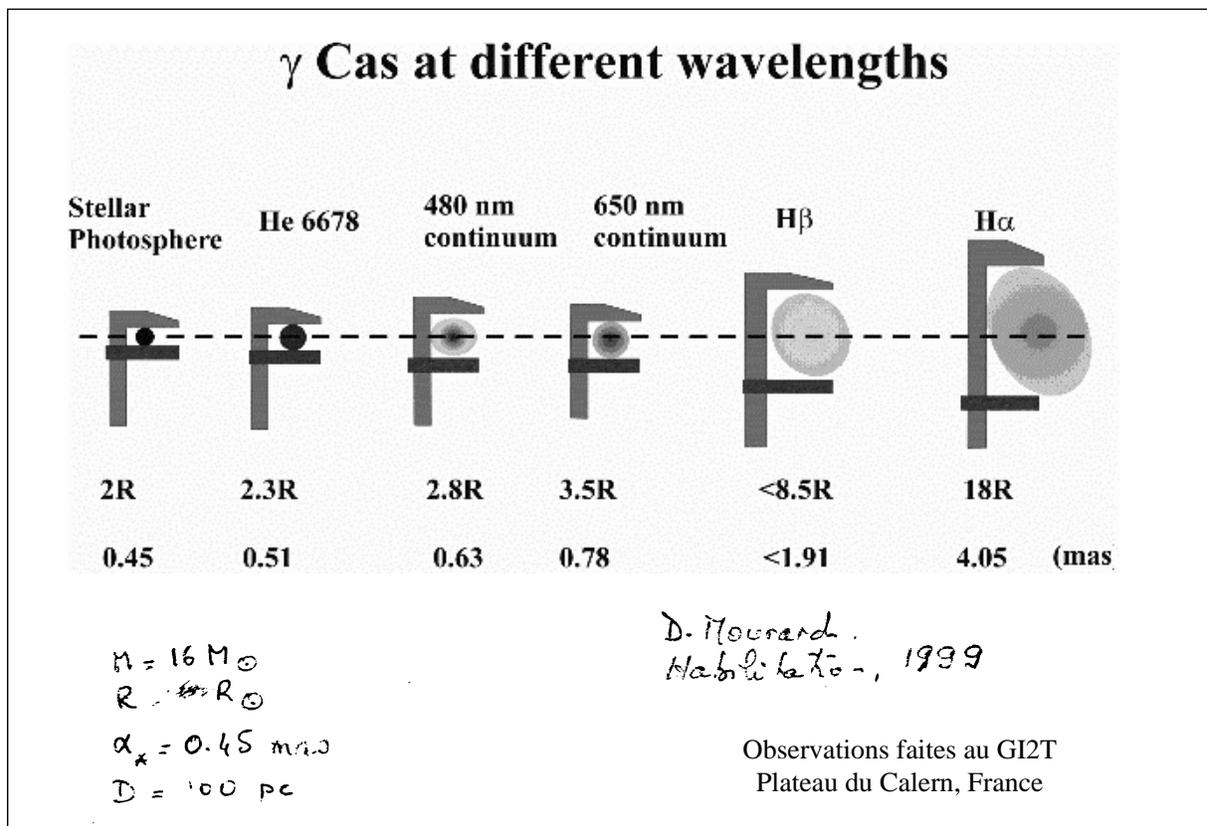
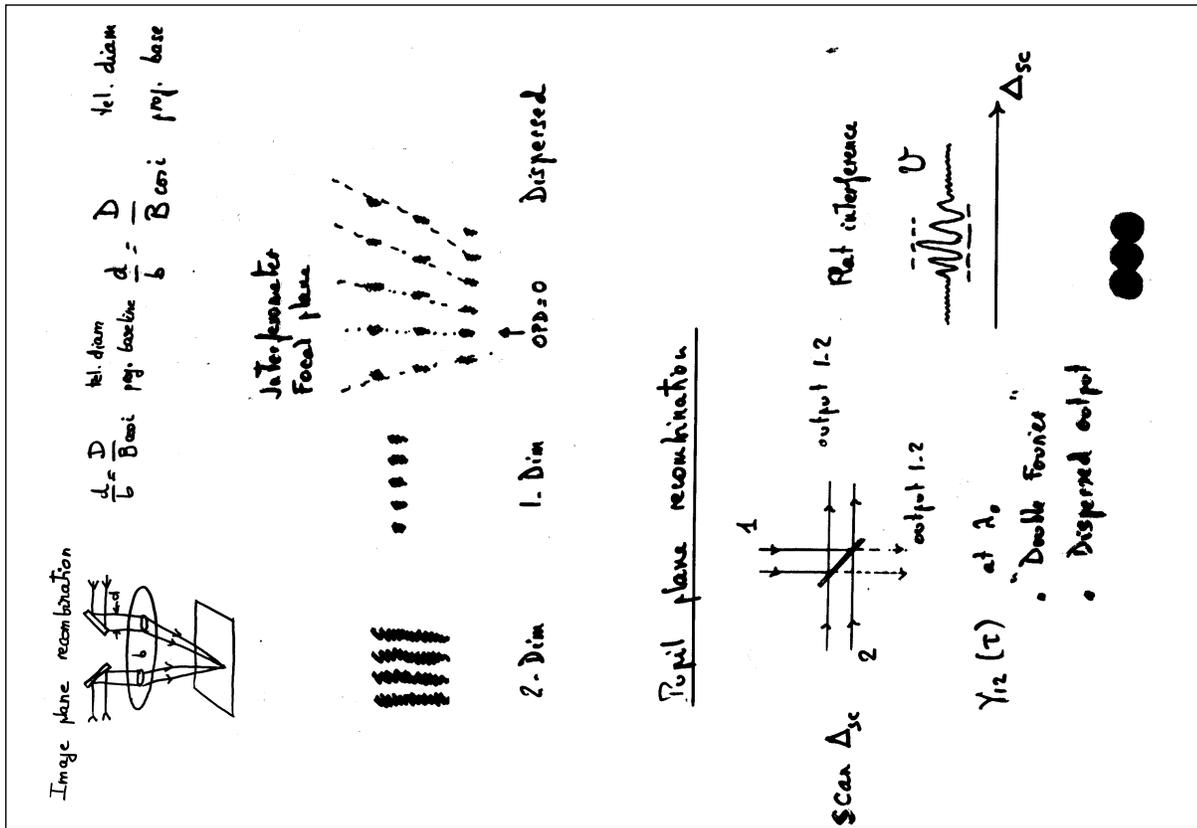
$$C = e^{-\frac{1}{2}(\sigma_{\varphi_1}^2 + \sigma_{\varphi_2}^2)} \approx [E_{\text{coh}, 1} E_{\text{coh}, 2}]^{1/2}$$

when $E_{\text{coh}, 1, 2}$ are coherent fraction of energy on 1 and 2.

$$\sigma_{\varphi_1}^2 = \sigma_{\varphi_2}^2 = 1 \text{ rad}^2 \rightarrow C = \frac{1}{2}$$


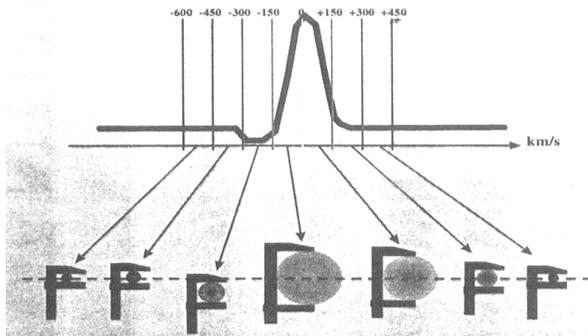
8. Methods of light recombination

- **Internal metrology in an interferometer**
- **Image plane recombination**
 - dispersed fringes & spectral analysis
 - pupil reconfiguration ($N_{\text{telescopes}} > 2$)
- **Pupil plane recombination**
 - Double Fourier spectral analysis
- **Integrated optics recombiners**
- **Dual-beam (dual-feed) operation**



Angular Diameter of P Cyg in H α and HeI6678

Size of P Cyg's Envelope versus Doppler-Shift across H α

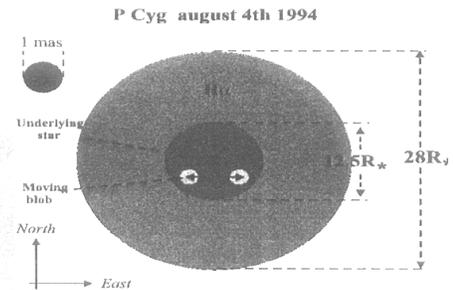


Schematic Morphology of P Cyg Wind Projected on the Sky According to GI2T Observations.

The Extent of H α and HeI6678 Envelopes are Given in Units of Photospheric Radius Assumed as $76 \pm 15 R_{\odot}$ and Corresponding to 0.4 mas . The Angular Scale is Given in mas Taking a Distance of $1.8 \pm 0.1 \text{ kpc}$.

The Projected Position of the Detected Blob is at $4 R_{*}$ to the South of P Cyg but its Absolute Position in the E-W Direction Remains Unknown.

Pictorial Representation of P Cyg as a Function of Doppler-shift Across H α Emission Line : the Slide Caliper Represents the Interferometric Process to Estimating the Equivalent Uniform Disk Size of P Cygni

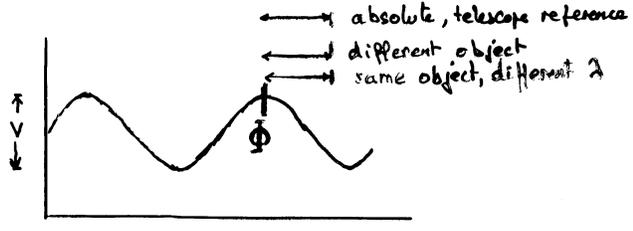


9. Signal detection & noise sources, sensitivity

- From measured to real visibility : calibration
- Expression of the interferometric signal : amplitude & phase
- Noise sources
 - signal photon noise
 - background (thermal) noise
 - detector read-out noise
 - atmospheric noises (piston, scintillation)
- Sensitivity & accuracy
- Phase determination
 - differential
 - phase closure

FRINGES = Visibility $\times e^{i\Phi}$

Interferometric sensitivity



Signal = Intensity . Area. Bandwidth. Exposure time. Transm. Visibility. Strehl
Atmosph. piston

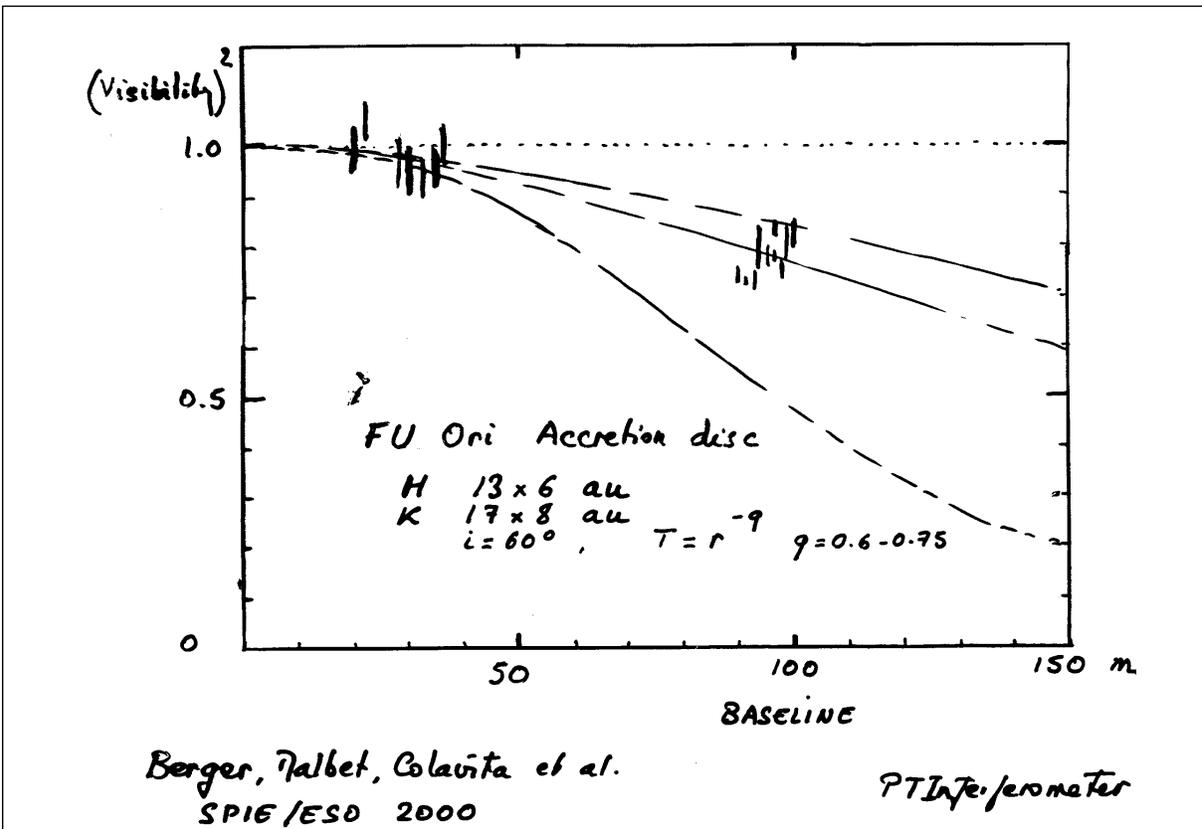
Noise = Signal Photon (visible)
 Read-out (J,H,K)
 Background (L,M,N)

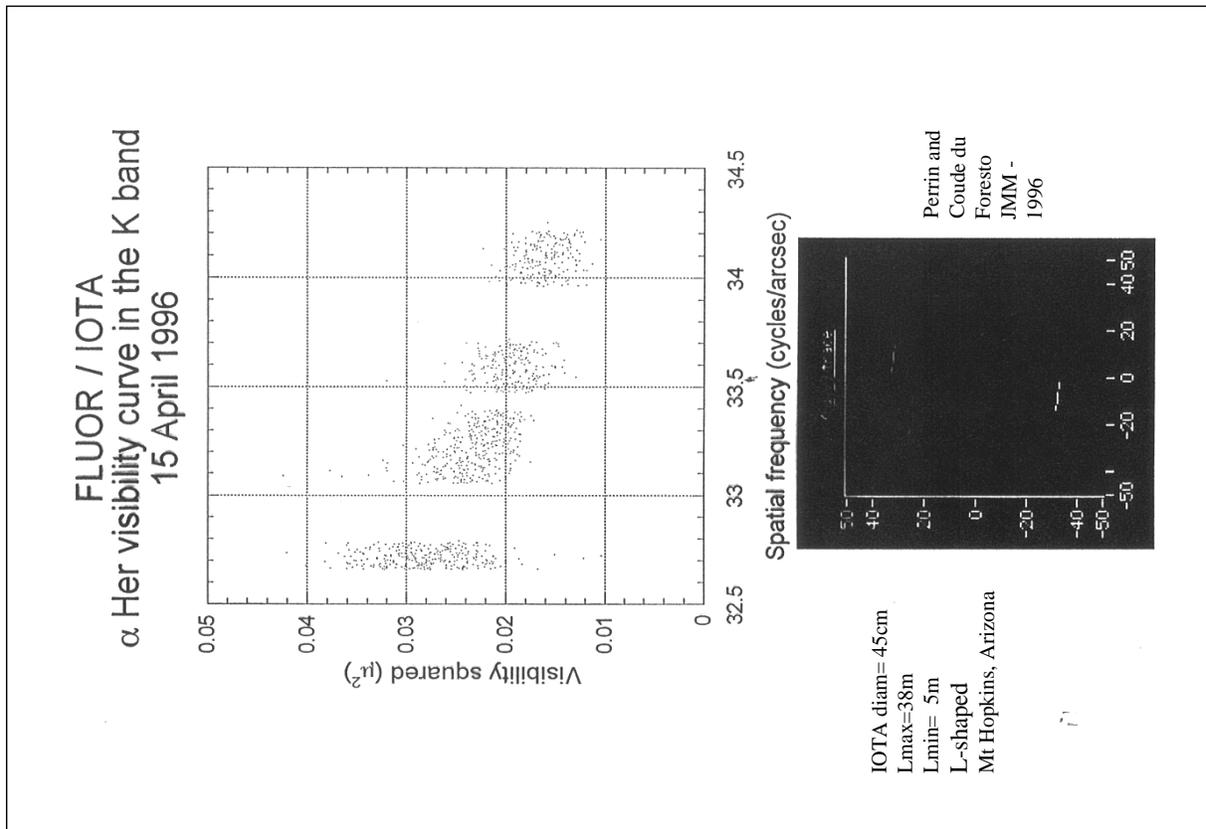
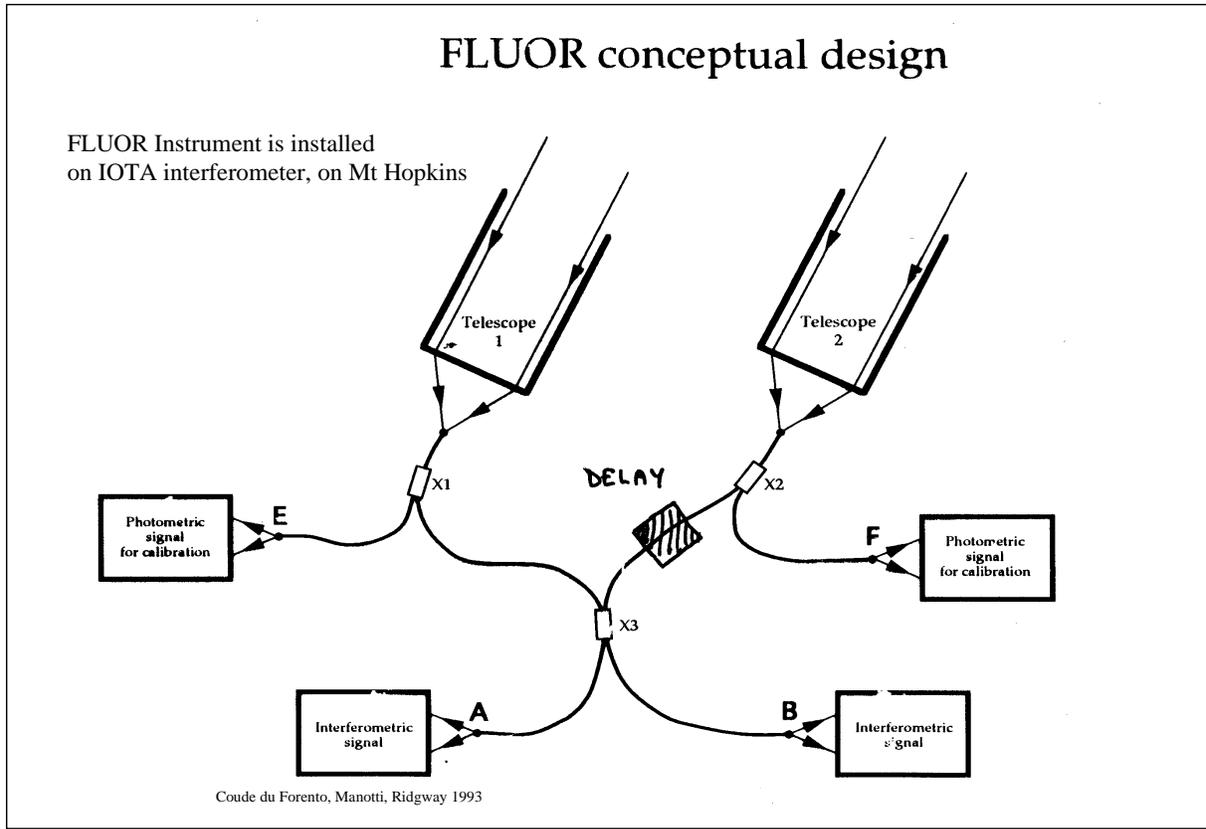
Exposure time = Atmospheric piston stability (ca. 50 ms)
 Long integration if fringe tracking (hours ?)

Transmission = 0.3 to 0.01

Strehl = 0.5-0.7 if proper AO correction ($m_v < 15$)

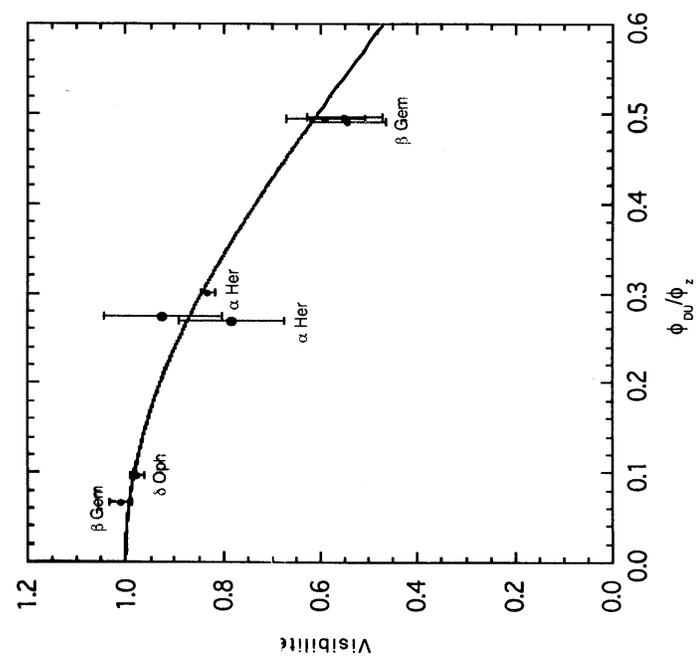
Visibility = $V_{source} \cdot V_{atm} \cdot V_{mirror} \dots$





Gain en précision apporté par les fibres

Mesures de visibilité en bande K (2.0 - 2.4µm)



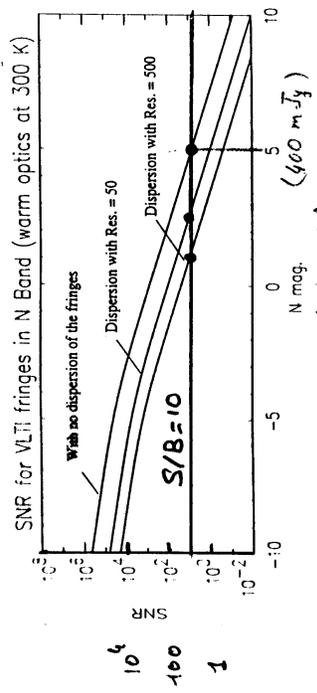
Interféromètres classiques:

- IRMA: Benson et al., Astr. J. 105 (1993)
- I2T: Di Benedetto and Rabbia, A&A 188 (1987)

Interféromètre à fibres:

FLUOR: Coudé du Foresto, PhD thesis (1994)

Performances MIDI (Rapport 1998, Leinert et al, ESO/SPIC 2b)



magnitude N
100 msec exposure (bright object)

If 10 s exposure (fixed stack on reference),
 $\Delta m_N \approx 2.5$

NGC 253, 1068, 3758, S128, Circinus
(12 in complete list above 400 mJy)

AMBER - The J,H,K VLT1 instrumen

K limiting magnitudes (conservative)

mode	exp. t.	resol.	K =	K =
High precision	0.01 s	5	11.3	8.0
High sensitivity	0.1 s	5	13.2	9.9
Fringe tracking	4 h	5	17	12.1
" "	4 h	100	16.5	11.6
" "	4 h	1,000	15.0	11.1
" "	4 h	10,000	14.2	9.6
			UT	AT

Richichi et al., ESO/SPIE 2000

These measurement

2 apertures }
1 source } impossible

2 apertures }
2 sources } Ground : $\delta\theta \lesssim 1$ arc min
Space : $\delta\theta$ arbitrary
+ internal metrology

≥ 3 apertures }
1 source } Ground : phase closure
Space : internal metrology

Simple case : Photon-noise (signal)

$$\sigma_{\varphi} = \frac{2}{\pi} \sigma \sqrt{N} \quad N_{\text{photon / frame}}$$

$$\sim 0.1 \text{ rad} \quad (\text{const})$$

∴ atmospheric

$$\sigma_{\varphi} (\vec{B}, \text{turbulence}, \delta\theta)$$

PHASE CLOSURE

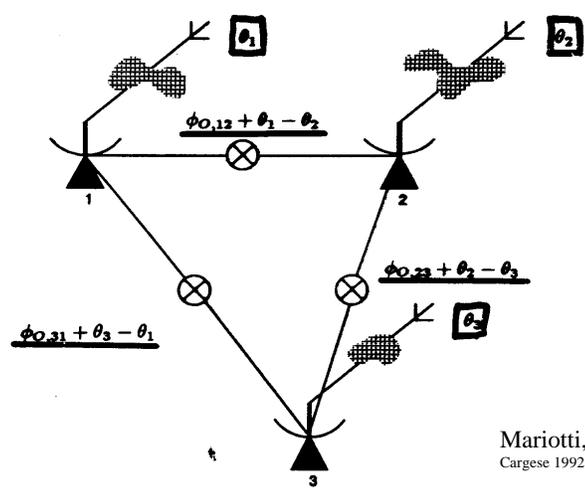


Figure 1. Measured phases for a simple three-element interferometer. $\phi_{0,12}$, $\phi_{0,23}$ and $\phi_{0,31}$ represent the true visibility phases that would be measured in the absence of turbulence. θ_1 , θ_2 and θ_3 are phase errors associated with each telescope.

THERMURE DE PHASE en radio-interferometrie

102 PEARSON & READHEAD

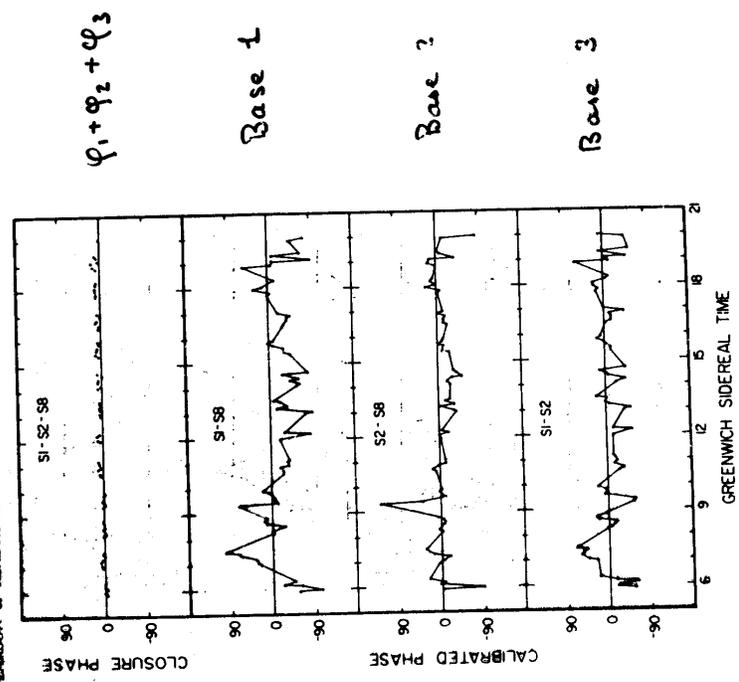


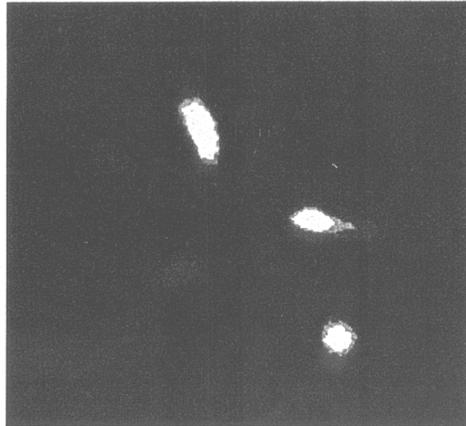
Figure 1. Illustration of the elimination of antenna-based phase errors by the calculation of closure phases. The lower three frames show the visibility phases observed on three baselines of the VLA in bad weather, after conventional calibration on a nearby point source. The upper frame shows the closure phase formed by summing the three visibility phases. The scatter is greatly reduced; the deviations from zero are due to structure in the source (the quasar 3C 147). Reproduced, with permission, from Readhead et al. (84).

SFO - Bordeaux - 1999

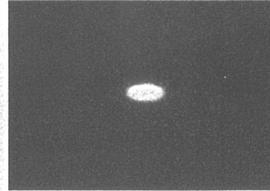
Détection directe (3) : annulation interférométrique de l'étoile (*nulling*)

Rapport d'intensité étoile/planète = 10^{-9} - 10^{-10} aux λ visible, 10^{-6} - 10^{-7} dans l'IR (5-20 μm)

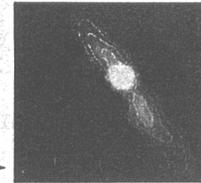
- Bracewell 1979
- Angel 1986, 1997
- Mariotti 1997,1999(+)



Système solaire à 10 pc, $\lambda = 10 \mu\text{m}$
Menesson et al 1998



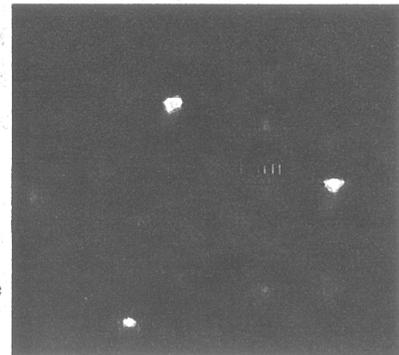
β Pic
→



Exo-lumière zodiacale : à $\lambda = 10 \mu\text{m}$, brillance de la lumière zodiacale du Syst. sol. est 300 x Flux(Terre)

Simulations de *nulling*,

3 planètes telluriques à
10 pc, modulation interne
Menesson 1999



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