

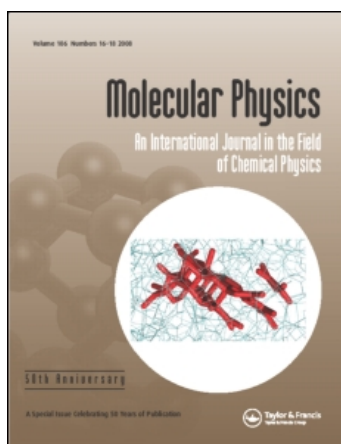
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RESEARCH ARTICLE

Deep-UV Rayleigh scattering of N₂, CH₄ and SF₆

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Rayleigh scattering room temperature cross-section values of N₂, CH₄ and SF₆ have been obtained between 198 and 270 nm by combining cavity ring-down spectroscopy (CRDS) and pressure ramp measurements. The experimental data have been fitted to a functional representation, describing the $\sim 1/\lambda^4$ like behaviour of the Rayleigh scattering cross section over a wide wavelength range. The resulting values are compared with numerical predictions, based on refractive indices and molecular anisotropy data available in the literature. From this, values of molecular volume polarizability α_{vol} and depolarization ratios are derived. It is found that the optical extinction for all three gases is governed by Rayleigh scattering for wavelengths down to 200 nm. No absorption onsets in the specified deep-UV region have been observed.

Keywords: Rayleigh scattering; optical extinction; cavity ring-down spectroscopy; atmospheric molecules

1. Introduction

Detailed information of Rayleigh scattering processes is a prerequisite to quantitatively interpret e.g. atmospheric and laser diagnostic results [1,2,3]. This is particularly true for deep-UV wavelengths as light scattering phenomena intensify because of the $1/\lambda^4$ scaling of the Rayleigh scattering. Furthermore, optical extinction studies are important to verify whether or not constituents exhibit absorption in addition to Rayleigh scattering. The absorption onset for CO₂ in the atmospherically relevant window around 200 nm, for example, has been known for many years [4] and was studied in detail recently [5,6]. In laser diagnostics Rayleigh scattering cross sections are needed to determine gas density and temperature distribution, e.g. in combustion or flow media [7]. In this paper the focus is on three molecular and atmospherically relevant species: N₂, CH₄ and SF₆.

Molecular nitrogen is the most abundant molecule in the Earth's atmosphere and hence information on the absorption and scattering of UV solar radiation by N₂ is important. Nitrogen has strong dipole-allowed transitions at wavelengths shorter than 100 nm. In the wavelength region studied here only symmetry-forbidden and consequently weak transitions have been reported. More specifically, in the 200 nm region the

(0,0) origin band of the Vegard–Kaplan system is located. However, the oscillator strength of this $A^3\Sigma_u^+ - X^1\Sigma_g^+$ spin forbidden system is small, and in addition the Franck–Condon factor of the (0,0) band is very weak. Consequently, the absorption cross section is expected to be well below the Rayleigh scattering value, i.e. the extinction behaviour should be fully Rayleigh dominated.

Information on the optical extinction behaviour of the greenhouse gas CH₄ around 200 nm is largely lacking. So far only absorption studies have been reported for a series of temperatures in the 106 to 145 nm region [8,9] and more recently theoretical results on the photodissociation of CH₄ around 124 nm has been reported [10]. Longer wavelength experimental studies are lacking.

Sulphur hexafluoride is an atmospheric trace gas that is primarily of anthropogenic origin but also occurs naturally. It is highly stable, this being the reason why it is used in a number of industrial applications. This may have caused an atmospheric SF₆ increase of 0.24 ppt in the early 1970s to nearly 4 ppt at the end of the 20th century [11]. Deep-UV absorption spectra of SF₆ have been recorded in the 78–185 nm region [12,13], but information on the light extinction at longer wavelengths is essentially lacking.

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In this paper, an experimental study of the optical extinction behaviour of N_2 , CH_4 and SF_6 in the 198–270 nm region is presented. This is achieved by combining highly sensitive cavity ring-down spectroscopy (CRDS) and the so called pressure ramp technique that allows unraveling the linear extinction signal associated with molecular scattering. In the next section, first the analytical approach is described, followed by experimental details. The results are discussed within the context of existing literature values. In the conclusion the main points are summarised.

2. Analytical approach

Rayleigh scattering [14], being considered in terms of classical electrodynamics theory [15,16], originates from the secondary radiation of oscillating electric dipoles, induced by an electric field from the incident light. Consequently, the Rayleigh scattering cross-section σ_R can be defined in two ways, either via molecular volume polarizability α_{vol}

$$\sigma_R = \frac{128}{3\lambda^4} \pi^5 \alpha_{vol}^2 \quad (1)$$

or, more conveniently, via [17,18]:

$$\sigma_R = \frac{24\pi^3}{\lambda^4 N^2} \left(\frac{n(\lambda)^2 - 1}{n(\lambda)^2 + 2} \right)^2 F_k(\lambda) \quad (2)$$

where λ is the wavelength in cm, N is the density of the molecules in cm^{-3} and $n(\lambda)$ is the wavelength dependent refractive index. This convention is used throughout this work. The Rayleigh formula (Equation (2)) relates the scattering cross section to two directly measurable quantities; the refractive index and the gas density. Note that the latter two are macroscopic properties of the gas such that σ_R represents a single-particle cross section. A comparison between measurements of the Rayleigh cross section and the refractive index, for a known density, yields information on the dimensionless King correction factor $F_k(\lambda)$ [15]. This factor accounts for the anisotropy in scattering by non-spherical molecules, which is important for the description of polarization and angular-dependent effects and is defined by

$$F_k(\lambda) = \frac{3 + 6\rho_p(\lambda)}{3 - 4\rho_p(\lambda)} = \frac{6 + 3\rho_n(\lambda)}{6 - 7\rho_n(\lambda)}. \quad (3)$$

Here ρ_p and ρ_n stand for the depolarization ratio of either polarised or natural (unpolarised) incident light, respectively, which is specified in [16,19,20,21].

The role of molecular polarization effects becomes significantly stronger in the deep UV compared to the visible. Consequently, the depolarization ratio of investigated molecular species must be taken into account as well [22].

3. Experiment

The experimental setup and approach to measure Rayleigh scattering cross sections have been described in detail previously [6,23,24] and are based upon direct absorption spectroscopy applying CRDS. Pulsed laser radiation is obtained by frequency doubling of the blue-green output of a Spectra Physics PDL-2 dye laser (operated on Coumarin 152, Coumarin 307 and Stilbene 3 laser dyes), pumped by a 355 nm Nd:YAG laser at 10 Hz repetition rate, yielding wavelengths at 270.15, 251.72, 215.38 and 210.12 nm. Wavelengths at 203.76, 199.27, 198.48 and 197.70 nm are generated by frequency-tripling the output of a pulsed (SIRAH) dye laser, running near 600 nm on Rhodamine-B dye and pumped by a Nd:YAG laser at 532 nm, also at 10 Hz repetition rate. The final bandwidth, in both configurations, is better than 0.2 cm^{-1} and the absolute accuracy of the wavelength calibration, performed by an echelle-grating spectrometer, is of the order of 0.01 nm.

The laser light is focused into an optical cavity comprising of two highly reflective mirrors and the light leaking out is detected by a photo-multiplier tube (Hamamatsu H9858 series) and subsequently digitised by a LeCroy9450 350 MHz oscilloscope. The reflectivity of the CRD mirrors ($r_{curv} = 25\text{ cm}$) is better than 99.4% in the 215.38–270.15 nm region and $\sim 98\%$ at 210.12 nm. These mirrors are mounted onto a 40 cm long cell, resulting in decay times of about 250 ns. High-quality mirrors ($r_{curv} = 1\text{ m}$) have been obtained (from LaserOptik) with an effective reflectivity of 99.2% in the 198–201 nm region; this constitutes a major improvement over previous deep-UV CRDS experiments [25]. The mirrors are mounted onto an 82 cm long cell, previously designed for pressure ramp CRDS studies [24]. This cell contains a multitude of inlet holes for the gas to enter the scattering region, while avoiding turbulence effects. The pressure in both cells is measured with high precision (0.15%) using an Edwards type 600AB Baratron. Pressure ramps are used to separate the molecular extinction signal from cavity losses and to extract absolute absorption cross sections [23]. For this both the pressure and the decay time of the cavity are continuously monitored, while gradually increasing the gas density in the scattering region.

The decay rate β obtained in this CRDS measurement, equaling the inverse of the ring down decay time τ , scales with the gas density

$$\beta = \frac{c|\ln R(\lambda)|}{d} + c\sigma N. \quad (4)$$

Hence, from a series of measurements at fixed wavelength and at increasing gas density N , both the averaged reflectivity $R(\lambda)$ of the mirror set and the absolute extinction cross section σ can be obtained. Note that the latter follows from the slope of each β vs. N measurement and that the resulting value is independent of the cell length d . CRDS pressure ramp scans have been recorded in pressure ranges up to atmospheric pressure. At every momentary pressure value, five decay transients are digitised and fitted. The slope coefficient of each individual pressure ramp measurement is determined with an accuracy of a few percent. The resulting cross-section values over the entire set of measurements are spread over a relatively large range and, therefore, a significant number of pressure ramp scans (typically 10) has been taken to statistically decrease the experimental error. All measurements have been taken at 293 ± 3 K.

High purity gases are used (99.999% for N_2 , 99.995% for CH_4 and 99.8% for SF_6) and a 0.5 micron filter cleans the injected gas from dust and aerosol particles, which may affect the scattering properties of the gas. It should be noted that the laser wavelength is not scanned during subsequent gas fillings, as only for fixed wavelengths frequency-dependent baseline fluctuations can be excluded. This also explains why only a limited number of frequency measurements is presented here, well distributed over the region of interest.

4. Results and discussion

The resulting extinction curves for N_2 , CH_4 and SF_6 are shown in Figures 1, 3 and 5, respectively. In Table 1, the measured and predicted extinction cross-sections (with 1σ uncertainties) are listed using Equation (2). These predicted values are calculated to equal the Rayleigh scattering cross-section values, and hence it is assumed that no absorption occurs. Formulas for the refractive indices and for the King correction factor are taken from the literature and extrapolated to the deep-UV region, if necessary.

It should be noted that due to the wavelength dependence of the refractive index and the King correction factor, the Rayleigh scattering cross section is not exactly proportional to $1/\lambda^4$. Consequently, a proper mathematical function accounting for this

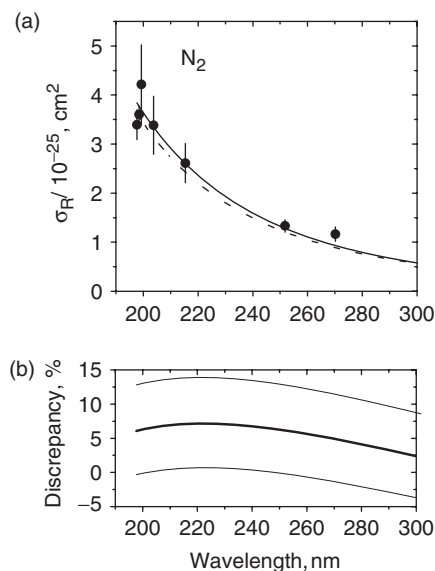


Figure 1. (a) The Rayleigh scattering cross-section behaviour of N_2 derived from a combined CRD – pressure ramp experiment (black circles). The dashed line represents the Rayleigh scattering cross-section values, calculated from dispersion data for refractive indices taken from [28] and for a King correction factor as used in [27]. The solid line shows the fit representation for $\sigma = 1.80(6) \times 10^{-46}$ and $\varepsilon = 0.534(3)$. (b) The difference between calculated (from the dispersion) and fitted (from CRDS measurements) values, plotted as a solid line. The dashed lines indicate the confidence interval, based on the uncertainties of σ and ε (Table 2).

difference [26] has to be used as demonstrated previously [6,23,24],

$$\sigma_R = \sigma \nu^{(4+\varepsilon)} \quad (5)$$

where ν is the light frequency in cm^{-1} . Hence, the wavelength-dependent Rayleigh scattering σ_R is expressed in terms of two variables σ and ε . In this functional representation is ε a dimensionless parameter and the dimension of σ consequently depends on the value of ε . In the following this is not addressed further. A simultaneous fit of both variables results in large error margins because of a strong correlation. Therefore, a two step fitting procedure has been applied: the σ parameter is kept fixed to the predicted and uncorrected theoretical value (calculated from the refractive index and the King correction factor), while the value for ε is repeatedly optimised. During the second step free and fixed parameters are interchanged and statistically reliable values are found after a few iterations. The experimental and predicted values for the three gases studied here are given in Table 2.

Table 1. Measured and predicted light extinction cross-section values in the 197.7–270.15 nm region for N₂, CH₄ and SF₆, obtained from CRD pressure ramp measurements.

λ [nm]	Extinction cross section/ 10^{-25} [cm ²]					
	N ₂		CH ₄		SF ₆	
	Measured	Predicted ^{a,b,c}	Measured	Predicted ^{c,e}	Measured	Predicted ^{d,e}
197.70	3.39 ± 0.30	3.62 ± 0.09	11.92 ± 0.64	10.82 ± 0.03	26.86 ± 2.54	23.71
198.48	3.60 ± 0.18	3.55 ± 0.08	12.59 ± 1.30	10.62 ± 0.03	19.35 ± 2.22	23.28
199.27	4.22 ± 0.80	3.48 ± 0.08	11.09 ± 2.42	10.43 ± 0.03	20.68 ± 2.14	22.86
203.76	3.38 ± 0.59	3.14 ± 0.08	–	9.39 ± 0.02	–	20.64
210.12	–	2.72 ± 0.06	–	8.13 ± 0.02	18.33 ± 4.04	17.94
215.38	2.61 ± 0.42	2.43 ± 0.06	7.79 ± 1.25	7.25 ± 0.02	16.09 ± 2.59	16.04
251.72	1.33 ± 0.10	1.21 ± 0.03	3.56 ± 0.2	3.57 ± 0.01	8.06 ± 1.35	8.00
270.15	1.17 ± 0.17	0.89 ± 0.02	2.53 ± 0.33	2.61 ± 0.01	5.98 ± 0.40	5.88

^aDispersion relationship, derived from refractive index measurements in [28].

^bDispersion formula for King correction factor, available from [27].

^{c,d}Dispersion relationships for the refractive indices, available from [24].

^eThe absolute error values given here are derived from the uncertainties of the King correction factor and the refraction index dispersion relationships. For SF₆ the latter is not available, which is the reason why in the last column no error values can be listed.

Table 2. Results of a non-linear square fit of Equation (5) to the experimental data points, both from the present work and from literature, for N₂, CH₄ and SF₆ gas.

Gas	Fit representation				Wavelength interval [nm]
	σ [10^{-46}]		ε		
	Experimental	Predicted ^a	Experimental	Predicted ^a	
N ₂	1.80 ± 0.06	1.796	0.534 ± 0.003	0.529	197.70 – 270.15
CH ₄	0.94 ± 0.02	0.942	0.699 ± 0.002	0.689	197.70 – 270.15
SF ₆	17.90 ± 0.76	17.897	0.490 ± 0.004	0.490	197.70 – 270.15

^aValues for σ and ε , derived from the fit, compared to predicted (dispersion-based) Rayleigh scattering cross-section values.

4.1. Molecular nitrogen

Accurate information (with an uncertainty of about 2×10^{-5} percent) of the N₂ refractive index behaviour in the 145–270 nm region is available for 273.15 K and 101325 Pa from [27,28]. To convert the refractive index data from [28] to the present laboratory conditions (293 K, similar pressure) the following equation is used [28,29];

$$\frac{n_1 - 1}{n_2 - 1} = \frac{P_1 T_2 Z_2}{P_2 T_1 Z_1} \left(1 + \frac{n_1}{6} \left(1 - \frac{P_2 T_1}{P_1 T_2} \right) \right) \quad (6)$$

with n_i the refractive index at pressure P_i [Pa] and temperature T_i [K] and where Z , the value of gas compressibility is given by [28,29]

$$Z_i = 1 - \frac{P_i}{101325} (317.6 - T_i) \times 10^{-5}. \quad (7)$$

In this way, 31 measured values of refractive indices $n_i(\lambda_i)$ [28] were scaled to 293K and 101325Pa and then fitted to a two term Sellmeier formula [30], resulting in the dispersion relationship;

$$n(\lambda) - 1 = \left(\frac{3.635 \cdot \lambda^2}{43.878 \times 10^{-5} \cdot \lambda^2 - 1} + \frac{0.0261 \cdot \lambda^2}{0.134 \times 10^{-5} \cdot \lambda^2 - 1} \right) \times 10^{-8} \quad (8)$$

The absolute uncertainty achieved during the fit is better than 0.1%. This determines the final uncertainty in the dispersion formula, since the error of the measured values of the refractive index is much smaller.

The King correction factor for the 200–633 nm region is available with an uncertainty better than 1% from [27] and given as

$$F_k(\lambda) = 1.03 + \frac{3.17 \times 10^{-12}}{\lambda^2}. \quad (9)$$

Seven data points for the wavelength-dependent Rayleigh cross section of N_2 are indicated in Figure 1(a). The points follow a dashed line that represents the prediction of the Rayleigh scattering cross-section based on dispersion relationships, given by Equations (8) and (9). The solid line in Figure 1(a) represents the fit for the resulting $\sigma = 1.80 \times 10^{-46}$ and $\varepsilon = 0.543$ values as listed in Table 2. The difference between the calculated and predicted values and the corresponding uncertainty range by the present fit representation is plotted in the lower graph (Figure 1(b)). All values overlap within their uncertainties, with exception of the 270.15 nm results. This may be due to the relatively low experimental sensitivity at this wavelength.

Since N_2 is a non-spherical molecule significant depolarization effects are expected in the deep-UV domain. To estimate how strong these effects are, a further quantitative analysis of the experimental data set has been performed and refractive index and King correction factor values have been derived using the current fit representation, as defined in Equation (5). The King correction factor values are derived using Equation (2), assuming that the refractive index dispersion is equal to Equation (8). A similar approach has been used to calculate the refractive index values for N_2 , using Equation (9). The molecular volume polarizability values have been calculated directly from Equation (1), assuming that the Rayleigh scattering cross-sections are equal to those predicted by the fit representation as given by Equation (5). The values of the depolarization ratio for polarised light have been calculated using Equation (3). The resulting values for, $F_k^{\text{exp}}(\lambda)$, $n^{\text{exp}}(\lambda)$, $\alpha_{\text{vol}}^{\text{exp}}(\lambda)$ and $\rho_p^{\text{exp}}(\lambda)$ are plotted in Figure 2(a) to (d), respectively (see figure caption for detailed information). In all cases the confidence intervals that are based on the experimental uncertainties are plotted as well. This shows that the values calculated from the fit representation using the measured Rayleigh scattering cross sections are in good quantitative agreement (within the specified uncertainty) with data available in the literature [7,27,28,]. The deviation between the calculated values of the King correction factor, refractive index, molecular volume polarizability and the depolarization ratio becomes smaller towards 300 nm. It should be noted that the difference between values of the King correction factor, derived from the present Rayleigh scattering cross-section determinations and the values, available from [27] is larger than that of the refractive index data. This is also reflected in the discrepancy between calculated and theoretical values of the molecular volume polarizability and the depolarization ratio. The reason for this is a general lack of

depolarization measurements in the deep-UV domain (shorter than 300 nm).

The outcome confirms that the light extinction in the deep UV for N_2 is fully determined by Rayleigh scattering and that there is no evidence for a (detectable) absorption onset in the studied wavelength region.

4.2. Methane

Six data points for the wavelength dependent Rayleigh cross section of CH_4 were measured and are plotted in Figure 3. Methane refractive index data have been reported only in the interval between 325.13 and 632.99 nm, based on the polarizability measurements given in [31]. Other information, particularly depolarization measurements, is largely lacking. A comparison with the depolarization effects for the symmetrically comparable CCl_4 at 632.8 nm suggests that these are small [16] and it seems reasonable to set $F_k(\lambda) = 1$ for methane. The dispersion formula for the refractive as extracted in [24] from the experimental data in [31] is used to calculate the Rayleigh scattering cross-sections.

$$n(\lambda) - 1 = \left(46662 + \frac{4.02 \times 10^{-6}}{\lambda^2} \right) \times 10^{-8}. \quad (10)$$

In view of the very limited number of refractive index measurements the accuracy of this equation is assumed to be on the level of 4% [24]. Extrapolation to the deep UV, as necessary here, most likely gives rise to additional uncertainty.

The values that result from the extinction measurements are plotted in Figure 3(a). For a quantitative estimate of the difference between the measured and predicted $\sim 1/\lambda^4$ Rayleigh scattering behaviour in CH_4 (based on dispersion), a non-linear least square fit along Equation (5) has been made that is included in Figure 3 as well. The resulting values for σ and ε are listed in Table 2. The discrepancy between the dispersion-related and CRDS derived cross sections is below 10% (Figure 3(b)).

As for molecular nitrogen values for the refractive index and the molecular volume polarizability have been derived for methane. For this depolarization effects are neglected and $F_k(\lambda) = 1$ is taken for all wavelengths. The resulting curves for the refractive index and molecular volume polarizability are plotted in Figure 4(a) and (b). The estimated discrepancy between the calculated and predicted values of the refractive index values is less than 6% (Figure 4(c)), originating from inaccuracies in the CRDS measurements and from the extrapolation of the dispersion

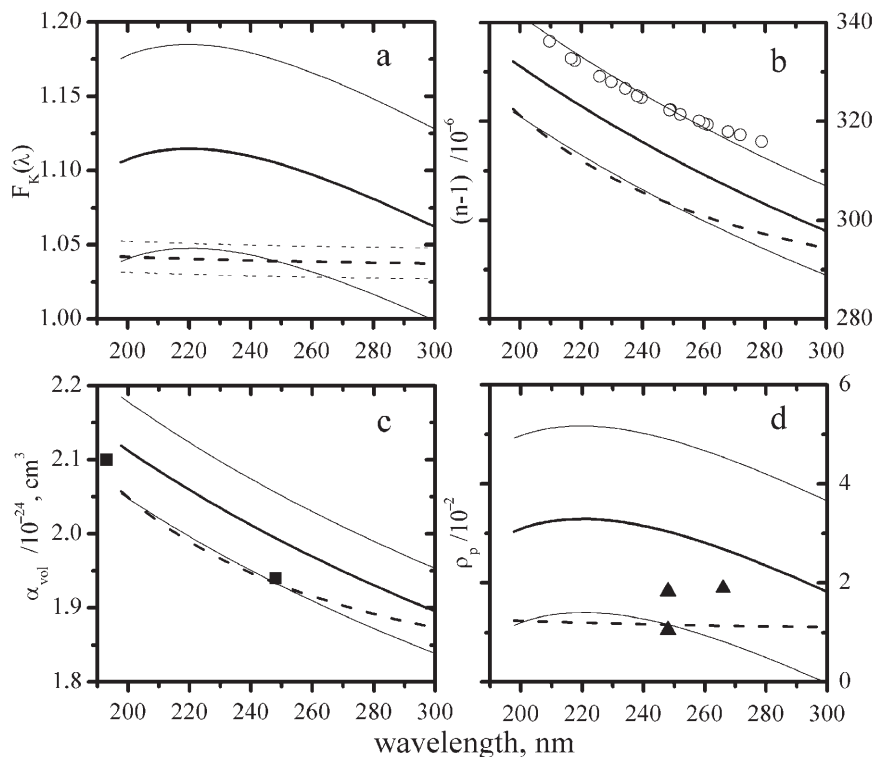


Figure 2. Different comparisons between the present experimental results and previous dispersion data. (a) Calculated behaviour of N_2 King correction factor: the black dashed line follows Equation (9) [27] and the thin dashed lines indicate the corresponding error margins. The solid black line is calculated from the present Rayleigh scattering cross-section measurements and the refractive index values, given by Equation (8). Error margins are again plotted as thin solid lines. (b) Calculated behaviour of N_2 refractive index: the black dashed line corresponds to the dispersion relationship, given by Equation (8), open circles indicate the refractive index measurements from [28] at 273.15 K. The black solid line corresponds to refractive index values as calculated from the present Rayleigh scattering cross-section measurements and the King correction factor, given by Equation (9). The error margins are indicated by thin solid lines. (c) N_2 molecular volume polarizability values (black solid line), calculated from the fit representation of the present Rayleigh scattering cross-section measurements. The error margins are indicated by thin solid lines. The dashed line represents values, calculated from the dispersion formulas, Equations (8) and (9), for the refractive index and King correction factor. The reported results on $\alpha(\lambda)$ in [7] are indicated by solid squares. (d) Calculated values of N_2 depolarization ratio, derived from Equation (8) for the King correction factor [27] are shown by a black dashed line. The black solid line corresponds to the calculated values, derived from the present Rayleigh scattering cross-section measurements. Error margins are shown as thin solid lines. Solid triangles correspond to direct depolarization measurements as reported in [21].

formula for the refractive index in CH_4 . This is comparable with the absolute uncertainty of the dispersion formula of $\sim 4\%$ in the 325–632 nm region [24,31]. Also here, the outcome confirms that the deep-UV light extinction is fully governed by Rayleigh scattering and that the refractive index in CH_4 in the deep-UV domain can be described by the dispersion relationship in the form of Equation (10) within a few percent uncertainty. The molecular volume polarizability values, calculated from the present CRDS measurements are found to be in a good agreement with the data available in [32].

It is important to note that the purity of the CH_4 gas used is critical. In a first set of measurements with purity

less than 99.5% and most likely hydrocarbon-like impurities an absorption onset was found around ~ 210 nm that definitely cannot be attributed to methane.

4.3. Sulphur hexafluoride

In Figure 5 the data point set for the wavelength dependent Rayleigh cross section of SF_6 is shown. In the literature a limited data set of SF_6 refractive indices and extinction coefficient measurements have been reported [12,13,24]. Sulphur hexafluoride is a highly symmetrical molecule, so $F_k(\lambda) = 1$ is used. The derived empirical formula for dispersion of the refractive

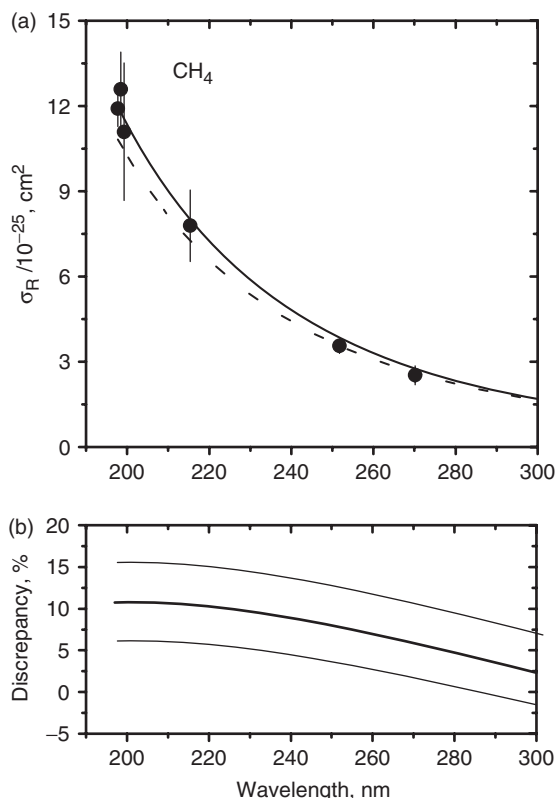


Figure 3. (a) Rayleigh scattering cross-section behaviour of CH_4 derived from a combined CRDS – pressure ramp measurement (black circles) and the fit representation (solid line) for $\sigma = 0.94(2) \times 10^{-46}$ and $\varepsilon = 0.699(2)$. The dashed line represents the Rayleigh scattering cross-section values, calculated from dispersion relationships [24]. (b) Difference between calculated and fitted values shown as a black solid line. Solid thin lines indicate the error margins.

index, based on measurements at 633 and 1300 nm [33], has been used in the UV-VIS [23,24,25]:

$$n(\lambda) - 1 = \left(71517 + \frac{5 \times 10^{-6}}{\lambda^2} \right) \times 10^{-8}. \quad (11)$$

The data points follow a dashed line that represents predictions of Rayleigh scattering cross-section values based on available dispersion data, as can be seen in Figure 5. This line coincides with a solid line that is the fit representation for $\sigma = 17.90 \times 10^{-46}$ and $\varepsilon = 0.490(4)$ as summarised in Table 2. The measured and predicted Rayleigh scattering cross-sections agree within 2% for the deep-UV domain, and the overall picture indicates that light extinction in SF_6 gas is governed by Rayleigh scattering in the entire studied wavelength interval.

Additional information is available from Figure 6 that shows the refractive index (solid black line in Figure 6(a)) and the molecular volume polarizability

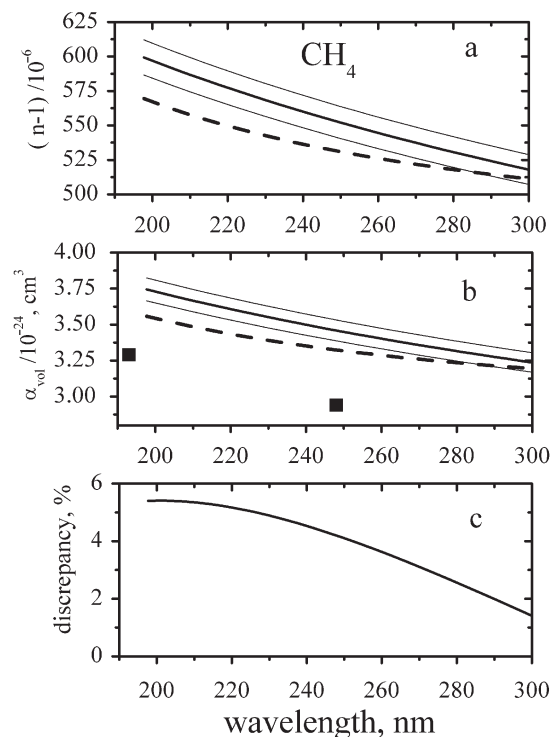


Figure 4. (a) CH_4 refractive index values, calculated from the Rayleigh scattering cross-section measurements (black solid line). The error margins are indicated by thin solid lines. The black dashed line corresponds to the dispersion formula for the refractive index, given by Equation (10). (b) Values of CH_4 molecular volume polarizability, calculated from the present study (black solid line). The error margins are plotted as solid grey lines. The dashed line represents the calculated values, calculated from the dispersion formula for the refractive index [24]. Black squares correspond to data, calculated in [32] from results obtained in [34]. (c) Discrepancy between refractive index values derived from the present Rayleigh scattering cross-section measurements and predicted refractive index values, using the dispersion formula as given by Equation (10).

(solid line in Figure 6(b)) values, derived from the fit representation of the measured Rayleigh scattering cross-section values. The dashed lines in Figure 6 show the predicted values derived from the Rayleigh scattering cross section, based on dispersion data available in the literature [24].

The comparison made for calculated molecular volume polarizability values shows that SF_6 has the largest polarizability among all investigated gas species. The error margins that originate from the absolute uncertainty of the σ and ε values are shown as grey solid lines in Figure 6 as well. The literature values [24,33] are indicated for comparison. From the numerical analysis it can be concluded that despite the lack of laboratory data, the refractive index of SF_6 follows the dispersion

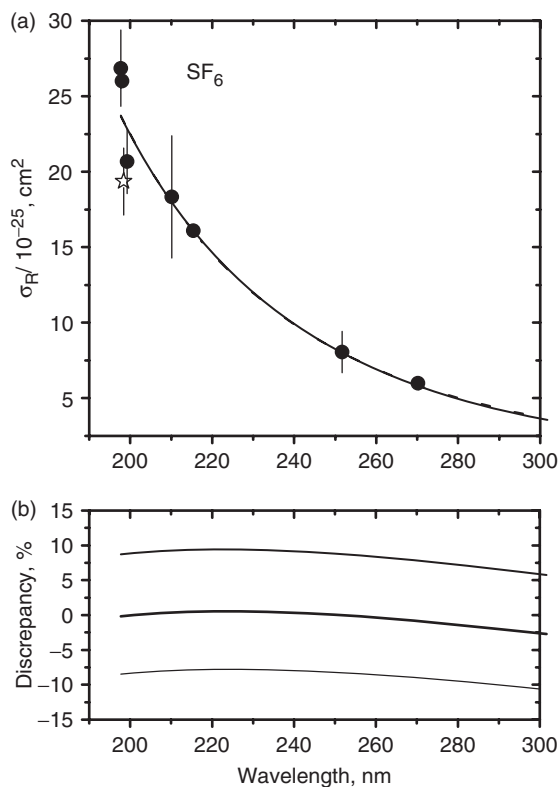


Figure 5. (a) SF₆ Rayleigh scattering cross-section behaviour derived from a combined CRDS – pressure ramp approach (black circles) and data available from [25] (empty star). The dashed line represents the calculated Rayleigh scattering cross-section values and the solid line corresponds to the fit representation for $\sigma = 17.90(76) \times 10^{-46}$ and $\varepsilon = 0.490(4)$. (b) Difference between calculated and fitted values is shown as a solid black line. Solid thin lines indicate the error margins.

formula, given by Equation (11), within a few percent uncertainty, even when extrapolated to the deep UV.

5. Conclusions

Extinction coefficients have been measured for gaseous N₂, CH₄ and SF₆ at room temperature between 197.7 and 270.15 nm applying cavity ring down spectroscopy to pressure ramp measurements. A non-linear squares fit of a $\sim 1/\lambda^4$ like function shows the actual behaviour of the Rayleigh scattering and gives an estimate of the discrepancy between measured and predicted values, based on dispersion formulas as available from literature. The light extinction in the deep UV is for all three molecular systems dominated by Rayleigh scattering. Due to the present lack of experimental data for light extinction cross sections and refractive indices between the deep UV and visible domain, it is not yet possible to construct a universal empirical

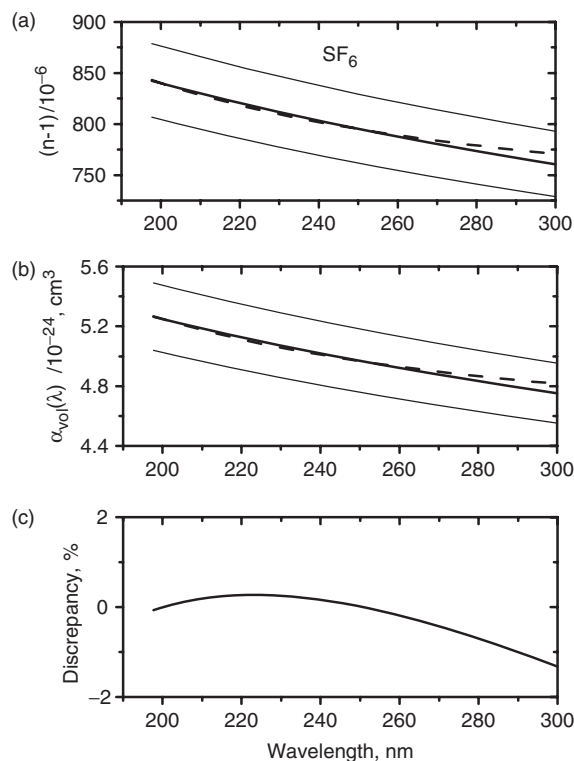


Figure 6. (a) SF₆ refractive index values, calculated from Rayleigh scattering cross-section measurements (black solid line). The error margins are given by grey solid lines. The black dashed line corresponds to the dispersion formula for the refractive index taken from [33] and given by Equation (11) [24]. (b) Molecular volume polarizability behaviour, calculated from the present CRDS measurements (black solid line). The error margins are plotted as solid grey lines. The dashed line represents the calculated values, calculated from the dispersion formula for the refractive index [24]. (c) Discrepancy between refractive index values derived from the present Rayleigh scattering cross-section measurements and the predicted values using the dispersion formula, as given by Equation (11).

relation that accurately predicts the $1/\lambda^4$ Rayleigh scattering behaviour for the entire UV-VIS region.

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