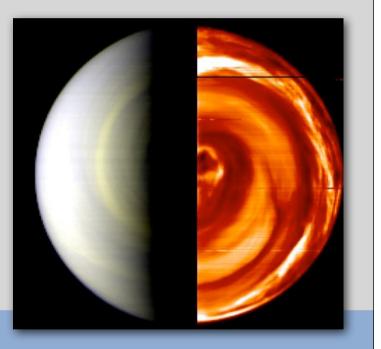
Radiative transfer

Planetary Sciences Chapters 3 - 4

Daphne Stam





Netherlands Organisation for Scientific Research

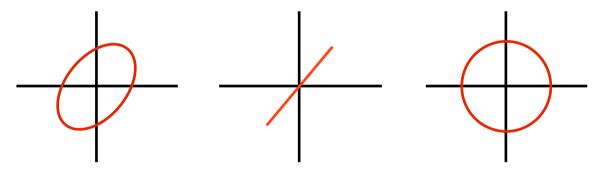
Outline

- A description of radiation
- Blackbody radiation
- Extinction of radiation
- Optical thicknesses
- Scattering cross-sections
- Colours of the skies
- Absorption cross-sections
- Phase functions and scattering matrices
- Reflection spectra
- Thermal spectra
- Spectra of transiting exoplanets

A description of radiation

Light consists of many waves that are each completely elliptically polarised: the end-point of their electric vector traces out an ellipse in a plane perpendicular to the direction of propagation of the light.

Special cases of the ellipse are a straight line (linear polarisation), and a circle (circular polarisation):

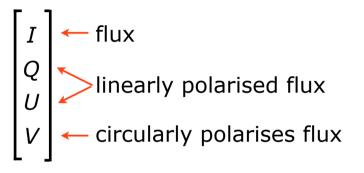


If the waves in a beam of light have a preferential shape and direction of their ellipses, the light is said to be (partially) polarised. The degree of polarisation of this light is defined as:

 $P = I_{\text{polarised}}/I_{\text{total}}$

A description of radiation

A beam of light can fully be described by a 4-vector:





The degree of polarisation is defined as: $P = \sqrt{(Q^2 + U^2 + V^2)/I}$

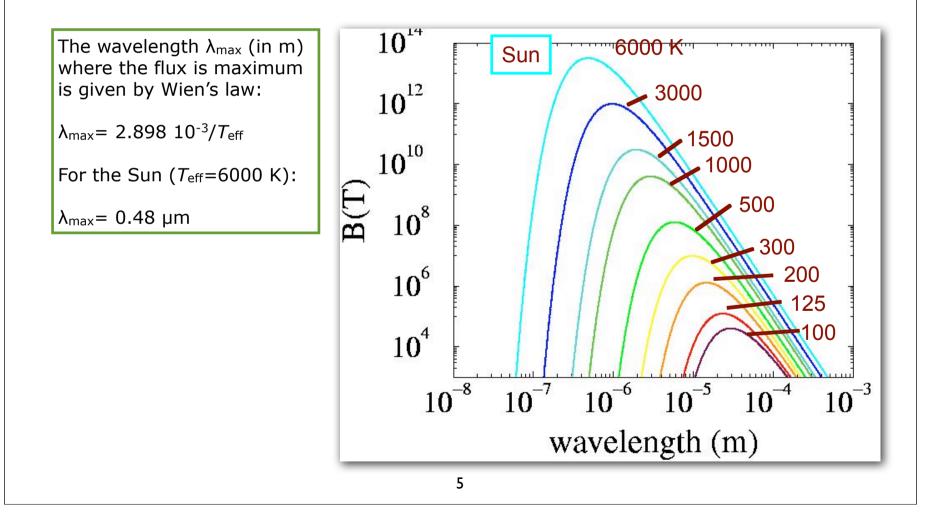
The degree of linear polarisation as: $P = \sqrt{(Q^2 + U^2)/I}$

The degree of circular polarisation as: P = V/I

Natural light, e.g. light of solar-type stars, when integrated over the stellar disk, can be assumed to be unpolarised: P=0

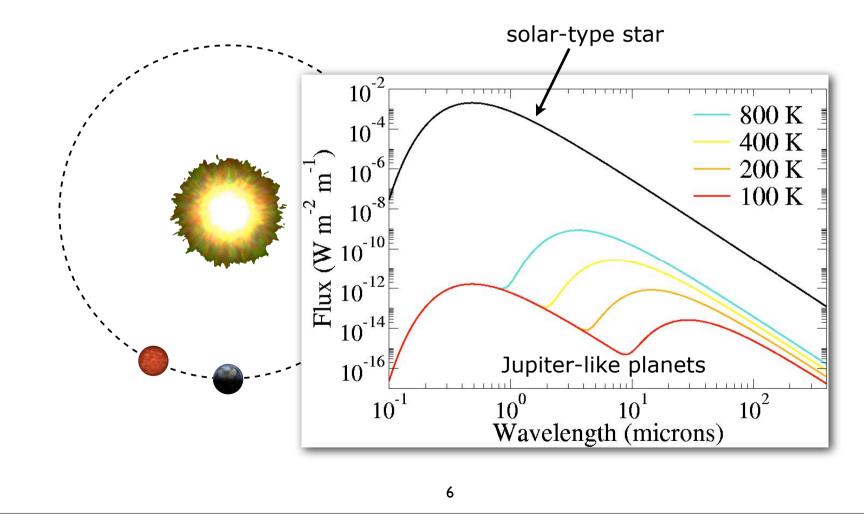
Blackbody radiation

The radiation that is emitted by a blackbody with an effective temperature T_{eff} can be described by a Planck-curve:



Planetary radiation

The radiation from a planet consists of thermal radiation (infrared) and reflected starlight (ultraviolet-visible-near infrared):

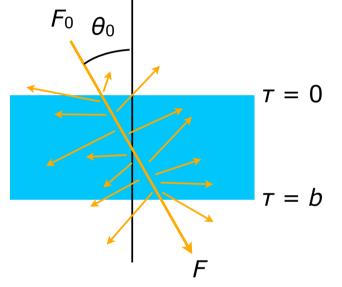


Extinction of radiation

The extinction of a parallel beam of radiation through a slab of material can be described as follows:

 $F(\lambda) = F_0(\lambda) \exp(-b(\lambda)/\cos \theta_0)$

 F_0 is the irradiance of the incident beamF is the irradiance of the transmitted beamb is the slab's extinction optical thickness τ is the optical depth in the slab θ_0 is the angle of incidence of the beam λ is the wavelength of the radiation



The radiation that is 'lost' to the beam is either absorbed or scattered in all directions. The extinction optical thickness *b* of an atmospheric layer is thus the sum of the layer's absorption and scattering optical thicknesses:

 $b(\lambda) = b_{abs}(\lambda) + b_{sca}(\lambda)$

The optical thickness of an atmospheric layer

A layer's extinction optical thickness *b* depends on:

- the types of gases, aerosol and cloud particles
- the amounts of gases, aerosol and cloud particles
- \bullet the wavelength λ of the radiation

A layer's extinction optical thickness is given by:

$$b(\lambda) = \int_{Z_1}^{Z_2} \sum_{i=1}^{I} \sigma_i(\lambda, z) n_i(z) dz$$

With:

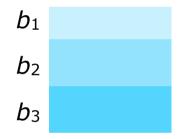
z the altitude (in m)

 σ_i the extinction cross-section of particle type i (in m²)

 n_i the number density of particle type i (in m⁻³)

For a homogeneous layer, we find: $b(\lambda) = \sum_{i=1}^{I} \sigma_i(\lambda) N_i$

With N_i the column number density of particle type i (in m⁻²)



$$b_{\text{tot}} = b_1 + b_2 + b_3$$

Absorption and scattering optical thicknesses

Remember: $b(\lambda) = b_{abs}(\lambda) + b_{sca}(\lambda)$

For a homogeneous layer, we have:

$$b(\lambda) = \sum_{i=1}^{I} (\sigma_{abs\,i} (\lambda) + \sigma_{sca\,i} (\lambda)) N_i$$

With:

 $\sigma_{abs i}$ the *absorption cross-section* of particle type i (in m²) $\sigma_{sca i}$ the *scattering cross-section* of particle type i (in m²) N_i the column number density of particle type i (in m⁻³)

Thus:

$$b_{abs}(\lambda) = \sum_{i=1}^{I} \sigma_{abs i} (\lambda) N_i$$
$$b_{sca}(\lambda) = \sum_{i=1}^{I} \sigma_{sca i} (\lambda) N_i$$

т

N_i depends on the ambient pressure, the temperature, and the gas mixing ratio

The single scattering albedo in the layer: $a(\lambda) = b_{sca}(\lambda)/b(\lambda)$

Scattering cross-sections

Scattering cross-sections σ_{sca} of gases, aerosol and cloud particles are usually smooth functions of the wavelength.

Scattering by gases or particles that are very small compared to the wavelength of the radiation $(2\pi r/\lambda \ll 1)$ is usually referred to as Rayleigh scattering.

For Rayleigh scattering of Earth-like air, the cross-section is given by:

$$\sigma_{\rm sca}(\lambda) = \underbrace{\frac{24\pi^3}{\lambda^4} N^2_L}_{\text{blue light scatters more efficiently than red light!}}_{\frac{6+3\rho_n(\lambda)}{6-7\rho_n(\lambda)}}$$

With:

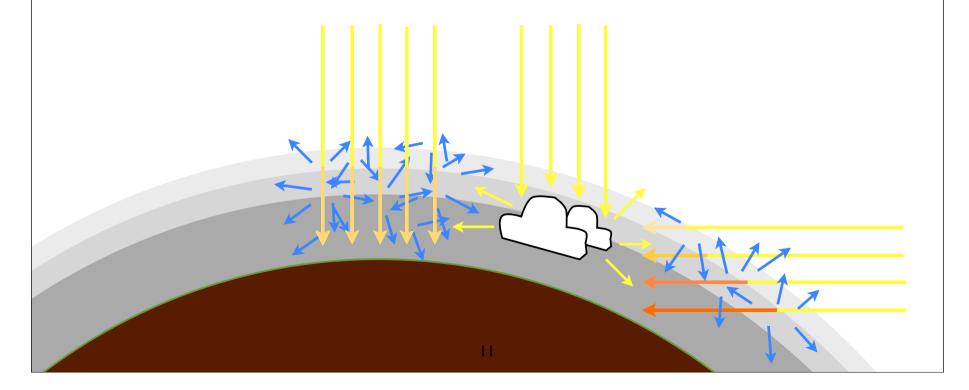
n the refractive index of dry air under standard conditions

- *N*_L Loschmidt's number
- $\rho_n \,$ the depolarisation factor of the air

Effects of the scattering cross-section

Why is the clear sky blue during the day? Why is the clear sky red during twilight?

Particles that are large with respect to the wavelength $(2\pi r \gg \lambda)$, such as some types of aerosol and cloud particles, scatter all colours of sunlight equally well, leaving the scattered light whitish or white:



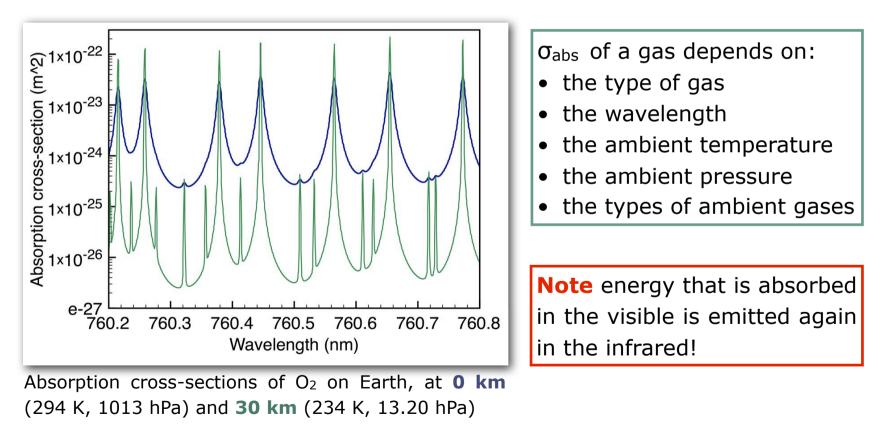
Colours of the skies:

The colour of a planetary atmosphere depends on its composition:



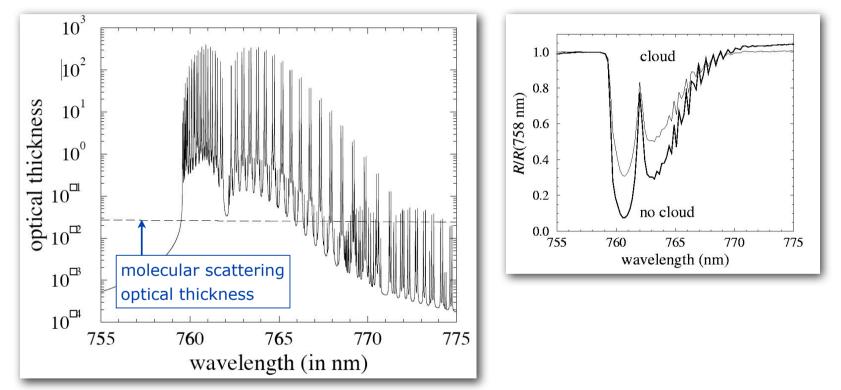
Absorption cross-sections

Absorption cross-sections of aerosol and cloud particles are usually smooth functions of the wavelength. Absorption cross-sections of gases are usually strongly varying functions of the wavelength:



Absorption cross-sections

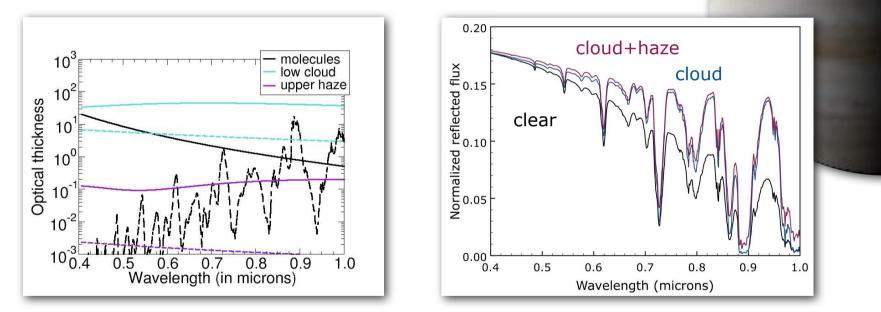
The spectral resolution of observations determines the strength and details that can be seen of an absorption band:



Calculated absorption optical thickness of O_2 in the Earth's atmosphere (left), and the same band observed (twice) by the GOME instrument onboard the ERS-2 satellite (right).

Cross-sections throughout an atmosphere

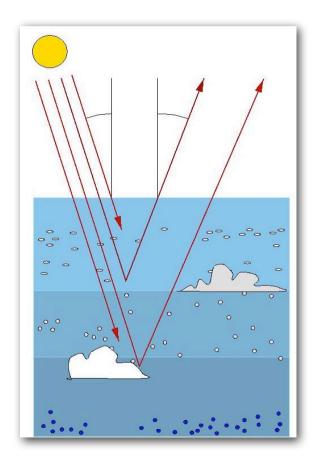
What a spectrum of a planet looks like depends on the scattering and absorption cross-sections of atmospheric constituents and their spatial distribution.



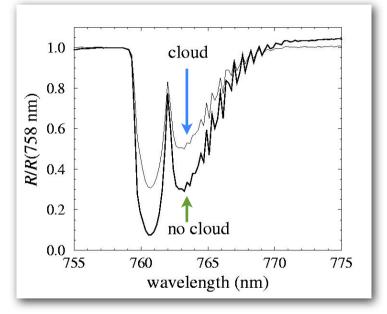
Above left calculated optical thicknesses (solid line: scattering; dashed line: absorption) of components of Jupiter-like atmospheres. Above right calculated spectra of the planets, seen at 90° phase angles.

Cloud top altitudes from absorption bands

What a spectrum of a planet looks like depends on the scattering and absorption cross-sections of atmospheric constituents and their spatial distribution:



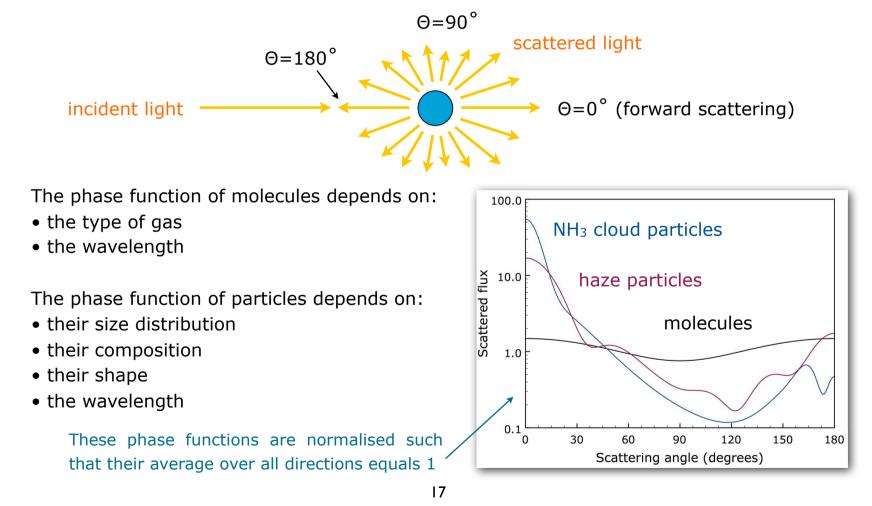




When observing a region on a planet, the cloud coverage will influence the band depth too!

Phase functions

The angular distribution of the flux of the light that is singly scattered by molecules, aerosol or cloud particles is described by the phase function:



Scattering matrices

The angular distribution of the flux and state of polarisation of the light that is singly scattered by molecules, aerosol or cloud particles* is described by the scattering matrix: phase function

$$\begin{bmatrix} F \\ Q \\ U \\ V \end{bmatrix} = \begin{bmatrix} P_{11} & P_{21} & 0 & 0 \\ P_{21} & P_{22} & 0 & 0 \\ 0 & 0 & P_{33} & -P_{43} \\ 0 & 0 & P_{43} & P_{44} \end{bmatrix} \begin{bmatrix} F_0 \\ Q_0 \\ U_0 \\ V_0 \end{bmatrix}$$
scattered scattering matrix incident light

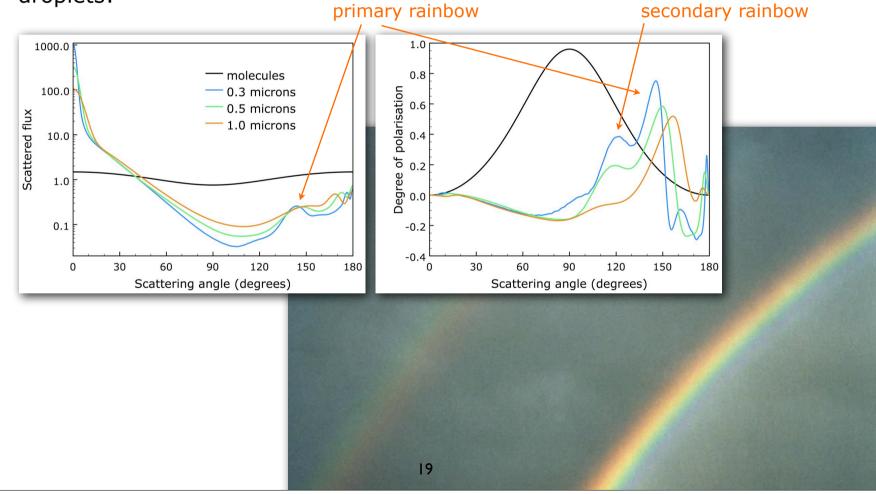
For incident unpolarised light:

Flux $F(\Theta) = P_{11}(\Theta) F_0$ Degree of linear polarisation $P(\Theta) = -P_{21}(\Theta)/P_{11}(\Theta)$

* if non-spherical, these have to be randomly oriented

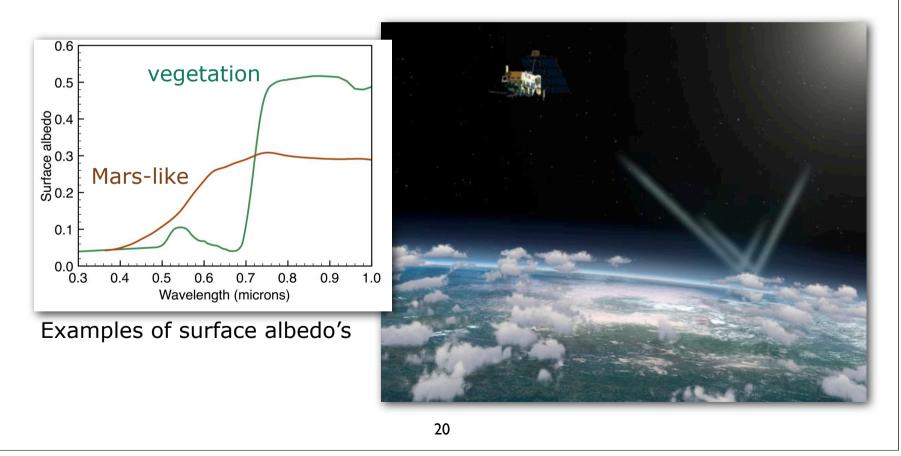
Scattering matrices of water droplets

The flux (left) and degree of linear polarisation (right) of unpolarised incident light of different wavelengths that is singly scattered by small water droplets:



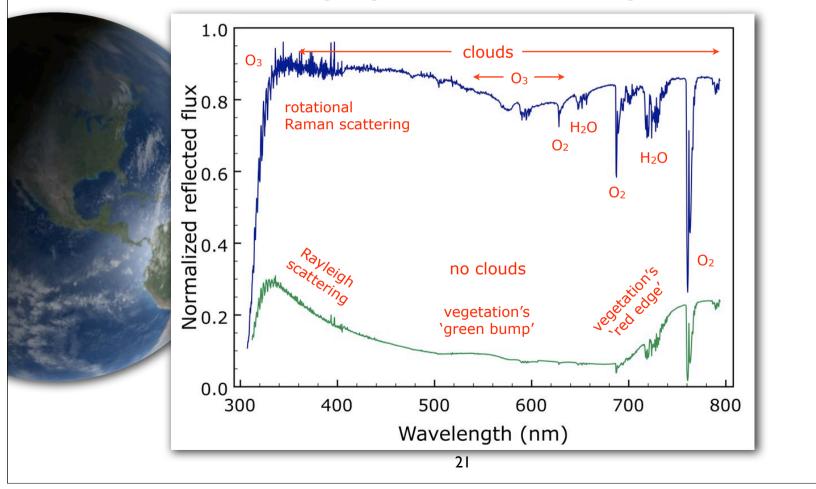
Reflection spectra: b \approx **1**

When observing rocky planets with optically thin atmospheres, you will not only receive sunlight that has been singly or multiply scattered by the molecules, aerosol and cloud particles within the atmosphere, but also light that has been reflected by the surface:



Reflected sunlight: Earth

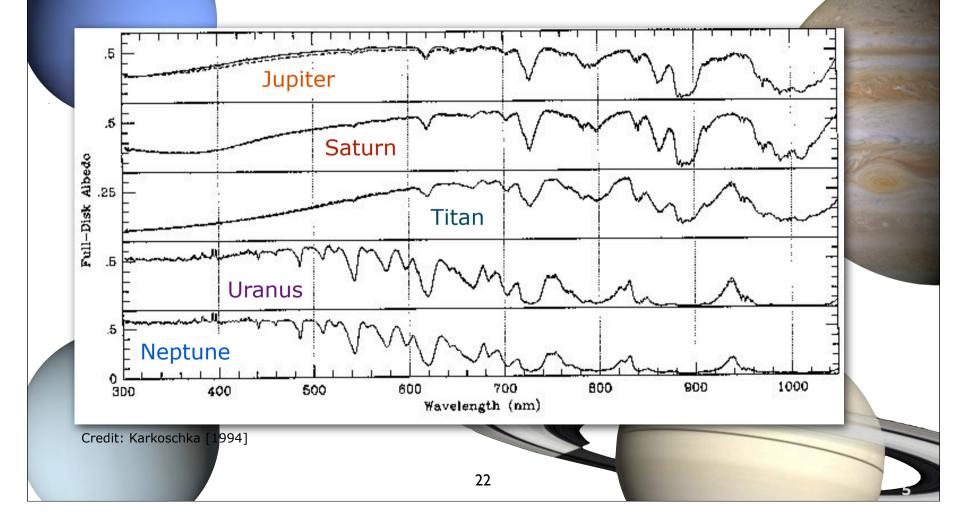
Reflected irradiance of a region on Earth, once clear and once completely covered by clouds, as measured by GOME on the ERS-2 satellite, for nadir viewing angles and solar zenith angles of 34° :



Reflected starlight: observations

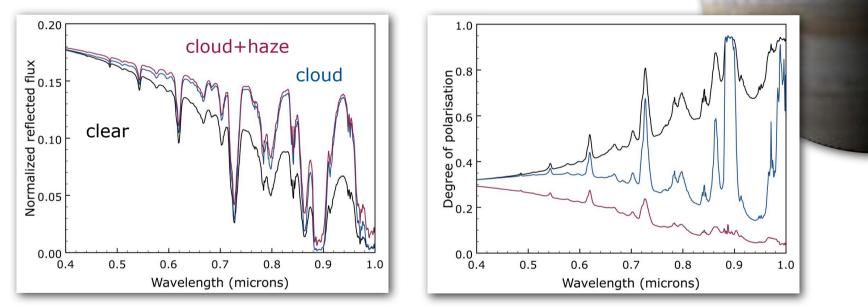


Disk-integrated observations of sunlight reflected by the Solar System's giant planets and Titan. Almost all absorption bands are due to CH₄:



Reflected starlight: simulations

The flux and degree of polarisation of starlight that is reflected by exoplanets can be calculated. Such simulations are required for instrument design, optimising the observation strategy, and the interpretation of observations.

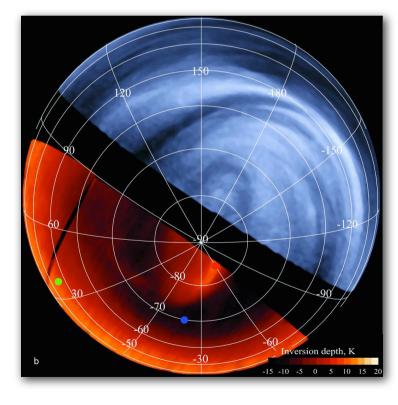


Above left calculated fluxes of starlight that is reflected by Jupiter-like exoplanets. Above right calculated degree of polarisation of the reflected starlight. The planets are seen at 90° phase angles.

Ultraviolet, visible & thermal radiation: Venus

Observations at different wavelengths reveal different compositions of the atmosphere and/or show different altitude regions.

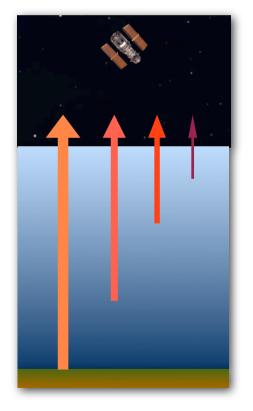
Left: Venus in UV reflected light and IR radiation as seen by Venus Express. Right: Venus in VIS reflected light as seen by the Galileo mission.

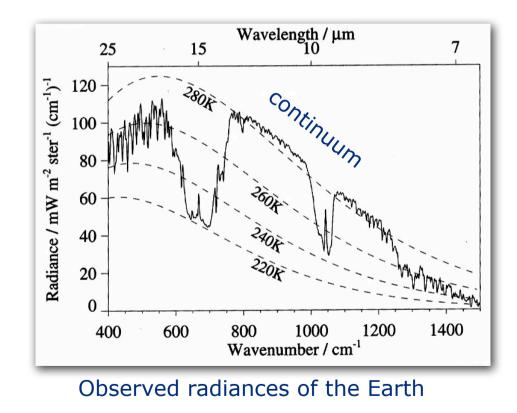




Thermal spectra: $b \approx 1$

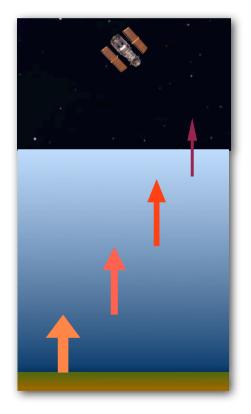
At wavelengths where the atmosphere is **optically thin**, most of the thermal radiation will come from the surface and the lowest, densest regions of the atmosphere, and is not absorbed before escaping to space:

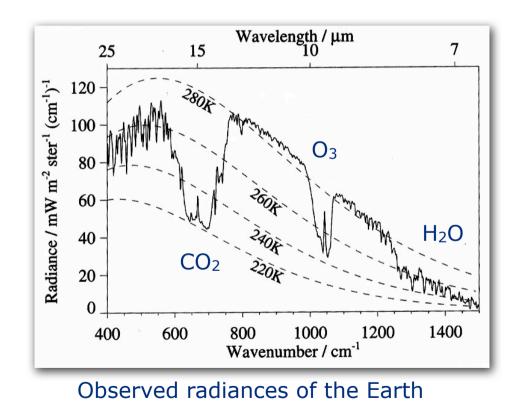




Thermal spectra: $b \gg 1$

At wavelengths where the atmosphere is **optically thick**, most of the thermal radiation observed from space will come from the highest regions of the atmosphere:

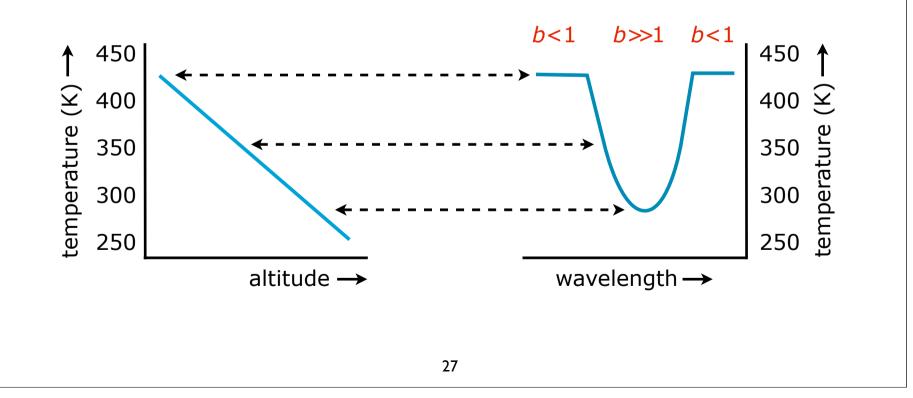




Thermal spectra: absorption features

The **shape** of molecular absorption bands in thermal emission spectra depends on the atmospheric temperature profile:

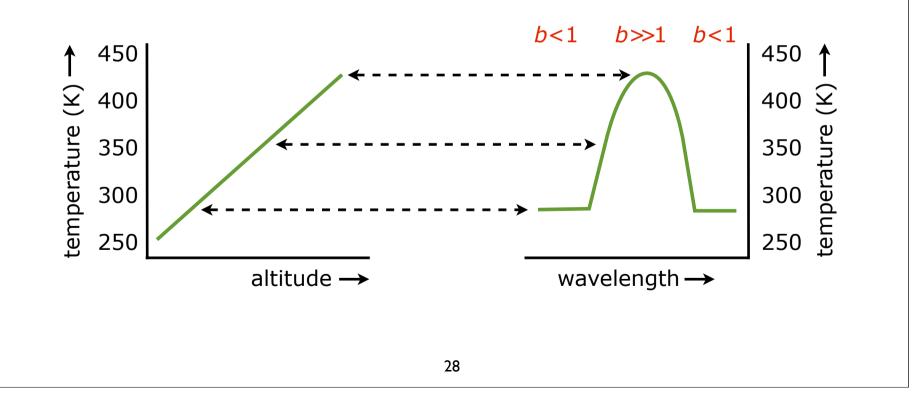
If *T* decreases with altitude, the band is seen in absorption



Thermal spectra: absorption features

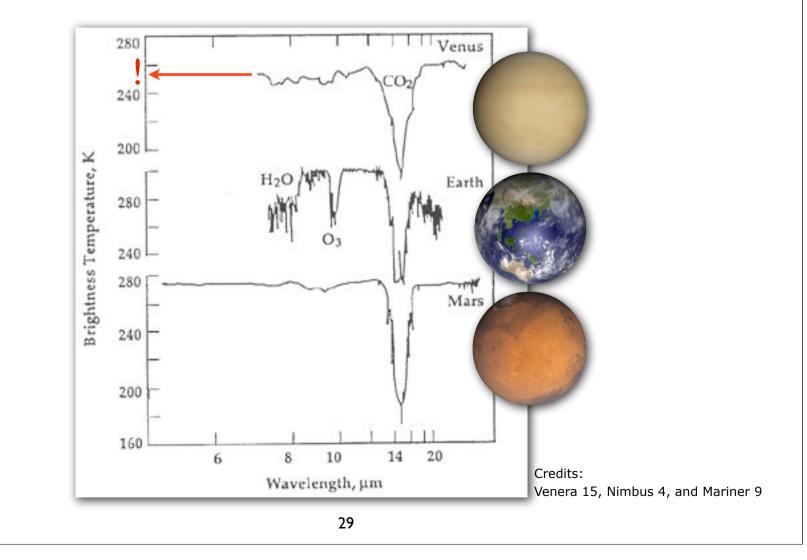
The **shape** of molecular absorption bands in thermal emission spectra depends on the atmospheric temperature profile:

If *T* increases with altitude, the band is seen in emission



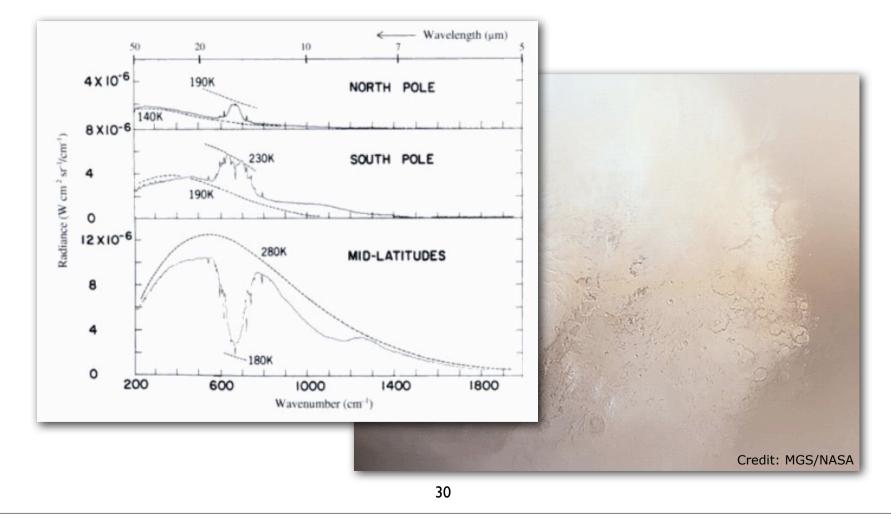
Thermal spectra: observations

The brightness temperatures of Venus, the Earth, and Mars:



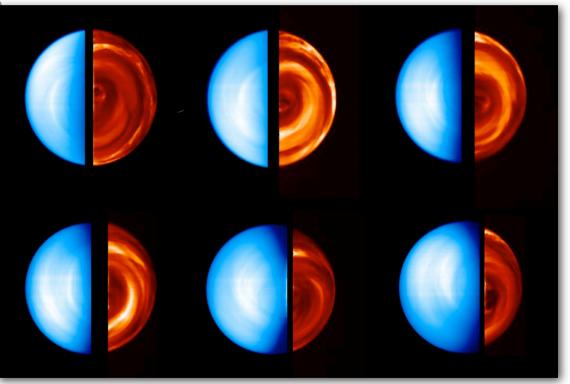
Thermal spectra: observations

Emission spectra can vary across a planet, depending on the local temperatures:



Thermal spectra: observations

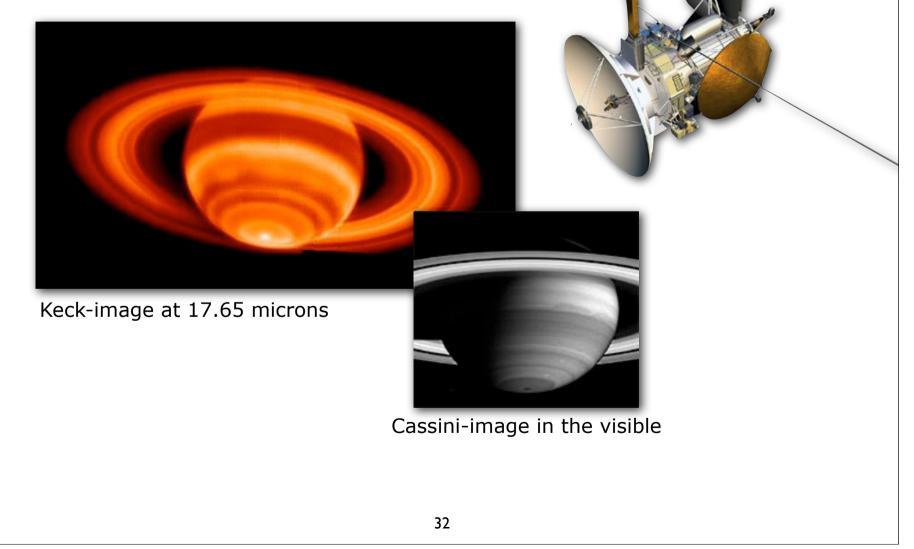
Venus' south pole observed by VIRTIS on the Venus Express mission over 7 consecutive Earth days. Left side: reflected light; right side: thermal emission



Venus' south polar vortex: bright at λ =1.7 µm: low, warm clouds, dark at λ =1.7 µm: upper, cold clouds

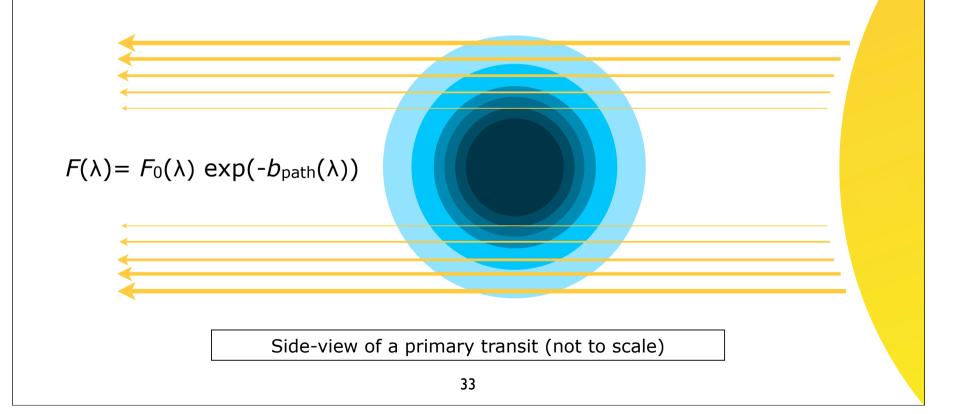
Reflected and thermal spectra: observations

Saturn's South pole is unexpectedly hot: > 150 K



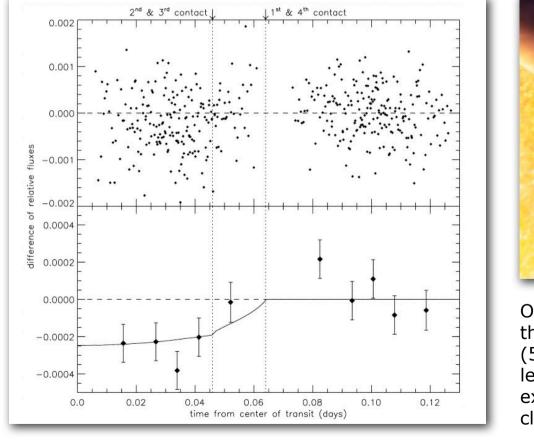
Planetary transit spectroscopy: principle

During the primary transit, starlight filters through the outer edges of the planetary atmosphere. How much flux at wavelength λ is transmitted, depends on the atmospheric extinction optical thickness at wavelength λ , thus on the **scattering** and **absorption optical thicknesses** of the gases, aerosol and cloud particles:



Planetary transit spectroscopy: observations

The first indications of an exoplanetary atmosphere were obtained from a primary transit observation of HD209458b (Charbonneau et al., 2001):

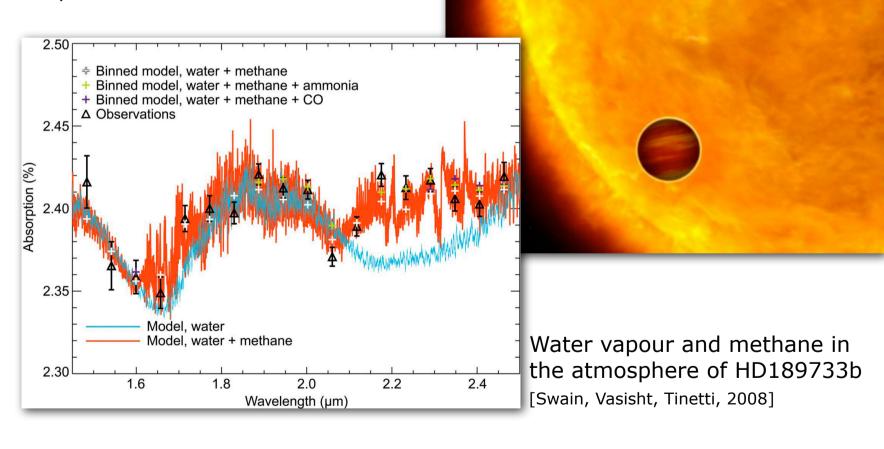




Observations of the depth of the Na D absorption lines (589.3 nm) with STIS/HST: less sodium detected than expected from models (high clouds?)

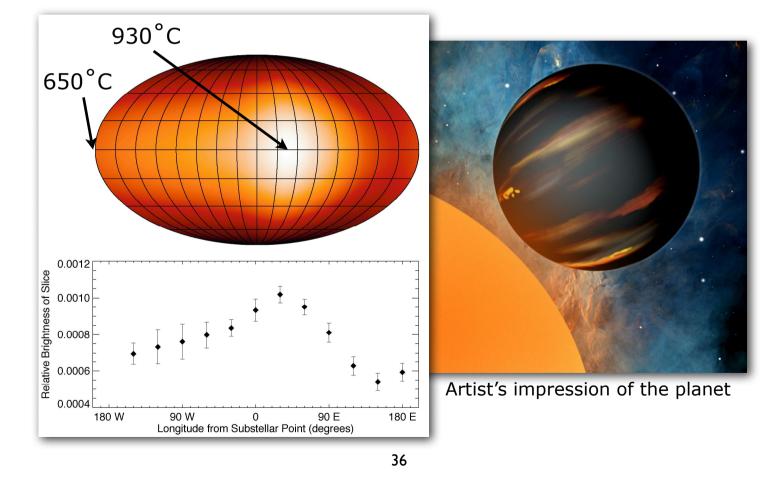
Planetary transit spectroscopy: observations

Various gases have been found in the atmospheres of transiting, giant exoplanets:



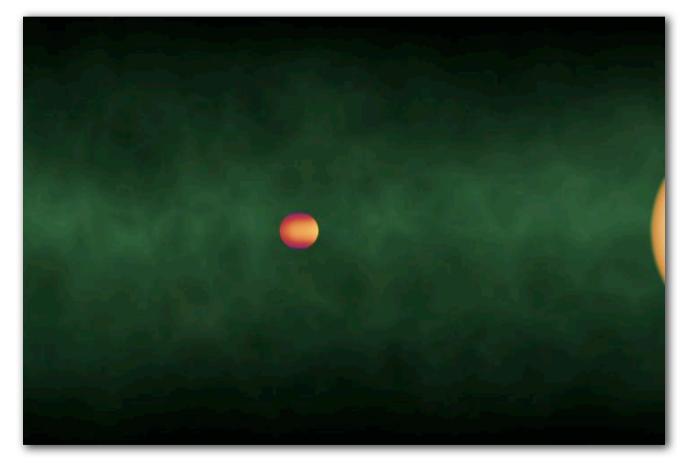
Transiting planets: a thermal map

Below is the first thermal map of an exoplanet derived from observations at 8 microns (Knutson et al., 2007). HD189733b is a hot-Jupiter that orbits its star in 2.2 days, it is tidally locked to its star:



Transiting planets: a thermal map

Below is a movie of HD189733b orbiting its star. Note: in the observations, the planet is not spatially resolved!



Planetary transit spectroscopy: exo-Earths?

Using transit spectroscopy to detecting gases in the atmospheres of terrestrial exoplanets appears to be very difficult:

- the atmospheres are *very* thin compared to the solid planet
- the variability/noise of the starlight will overwhelm the planet's signal

If the terrestrial exoplanet is in the habitable zone of a solar-type star, there are additional problems:

- a transit takes only a few hours (for Earth \sim 13 hours)
- a transit occurs only once a year

