

Previous lecture:

“real” maximum likelihood  
method: Poissonian data

Finding periodicities in data

- Lomb-Scarle diagrams
- Phase dispersion minimisation
- Fourier techniques

OAF2 chapter 6.1 & 6.2

Num Res chapter 13.8, 14.3, 14.5 & 14.7

Today

# Correlations

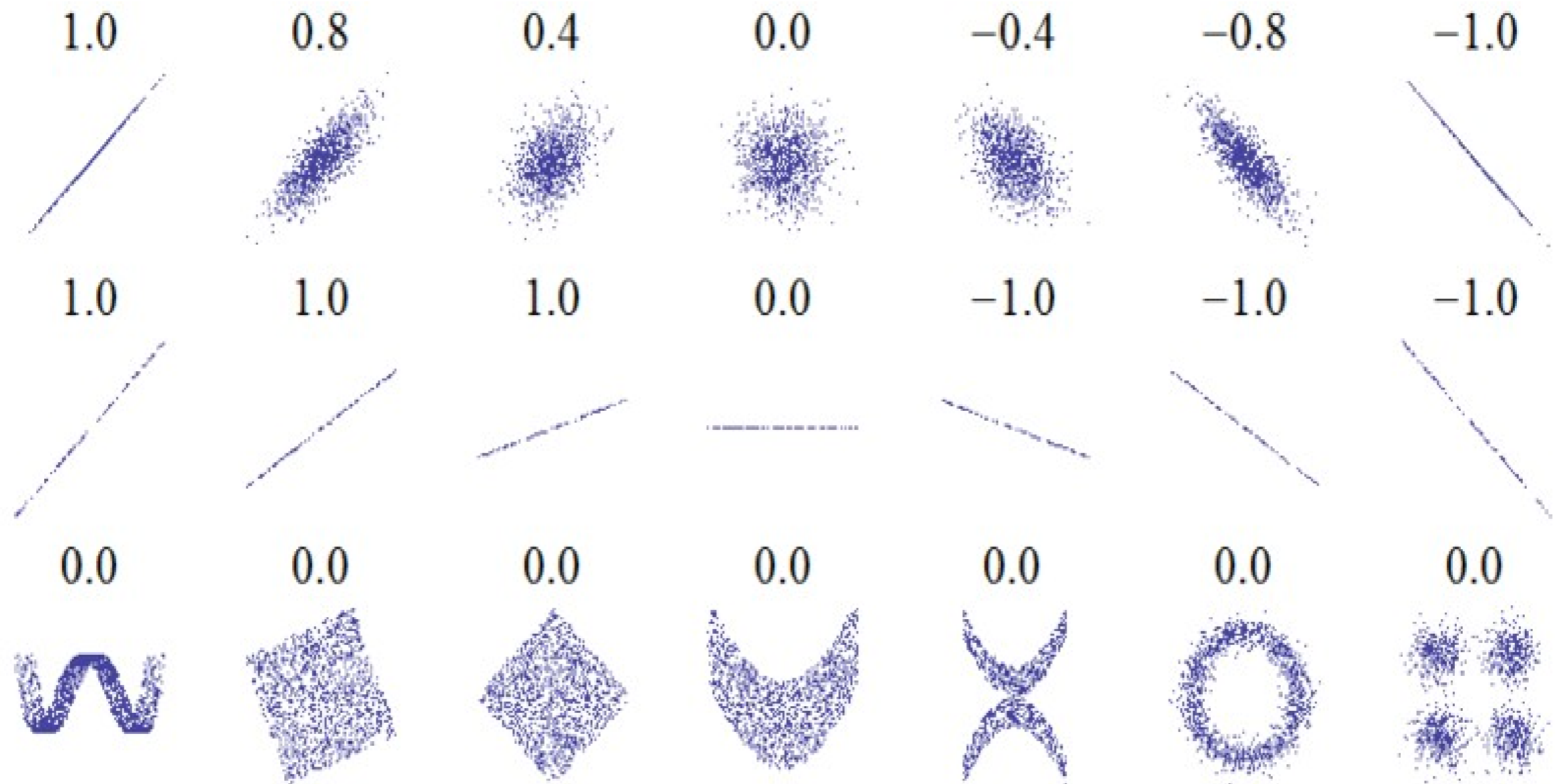
Kolmogorov-Smirnov test

Data is variable but not  
necessary periodic

Example: compare cumulative  
distribution function with model of a  
constant

Pearson's  $r$

$$r = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_i (x_i - \bar{x})^2} \sqrt{\sum_i (y_i - \bar{y})^2}}$$



Examples from Wikipedia

Another way of looking at Pearson's  $r$

$$\rho_{X,Y} = \frac{\text{cov}(X, Y)}{\sigma_X \sigma_Y} = \frac{E((X - \mu_X)(Y - \mu_Y))}{\sigma_X \sigma_Y},$$

A simple special case (if each value in  $x$  and  $y$  is unique): **Spearman's** rank

$$\rho = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$$

Significance? Monte Carlo (scramble data)

# Example Spearman's rank (from Wikipedia)

**IQ** Hours of **TV** per week

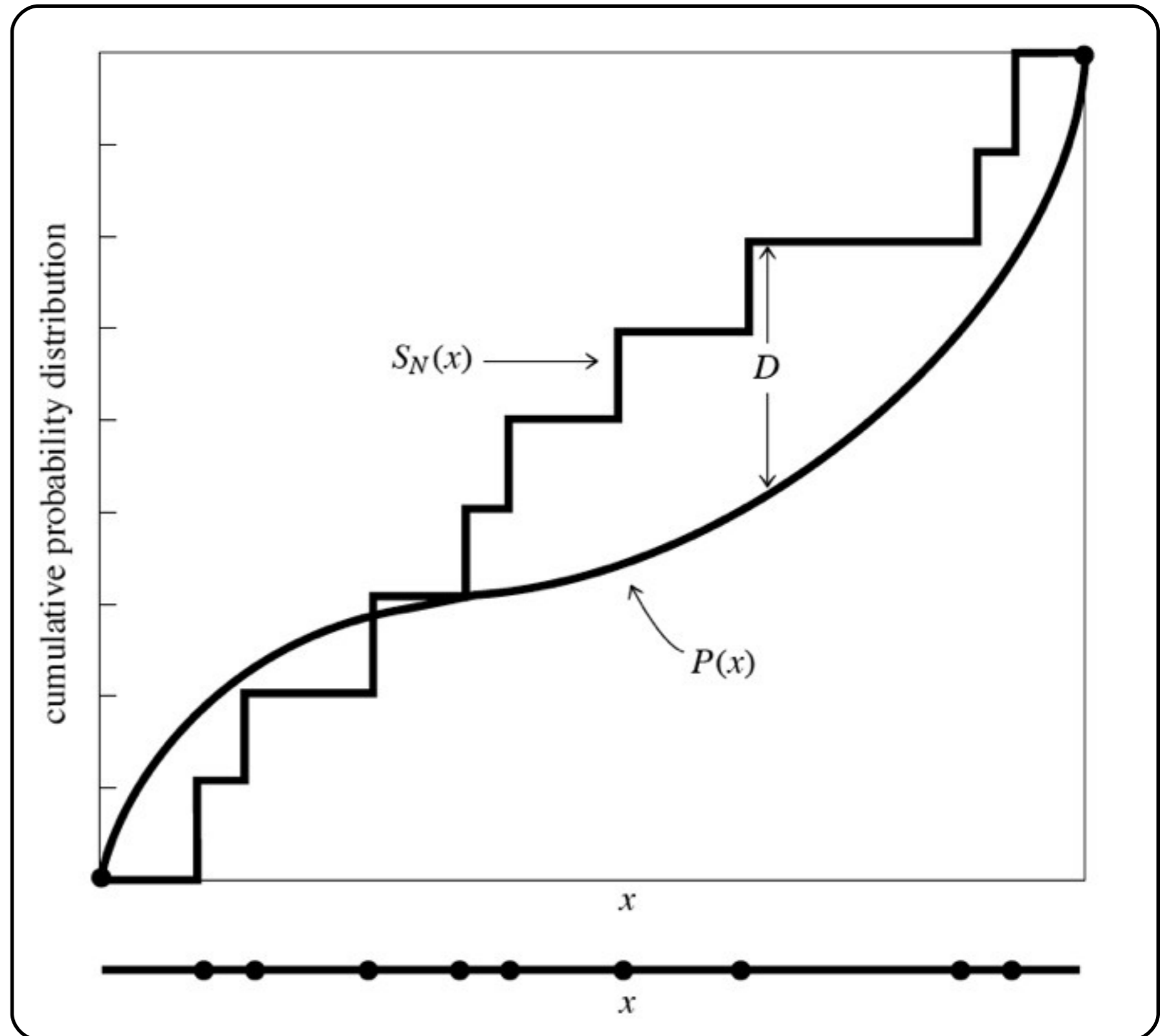
$X_i$	$Y_i$	rank $x_i$	rank $y_i$	$d_i$	$d_i^2$
86	0	1	1	0	0
97	20	2	6	-4	16
99	28	3	8	-5	25
100	27	4	7	-3	9
101	50	5	10	-5	25
103	29	6	9	-3	9
106	7	7	3	4	16
110	17	8	5	3	9
112	6	9	2	7	49
113	12	10	4	6	36

Sum over  $d_i^2 = 194$ ,  $n=10$ ,  $\rho = -0.176$

# Comparing a distribution with a theoretical distri or two distributions

Kolmogorov-Smirnov test:

compare two cumulative distribution functions  
e.g. 1 observed and 1 theoretical  
or  
e.g. 2 observed



# K-S test

an advantage of using  
K-S statistic

the distribution can be calculated in  
the case of the null-hypothesis  
(data sets from same distri/data  
drawn from theoretical curve )

$$Q_{KS}(x) = 2 \sum_{j=1}^{\infty} (-1)^{j-1} e^{-2j^2 x^2}$$

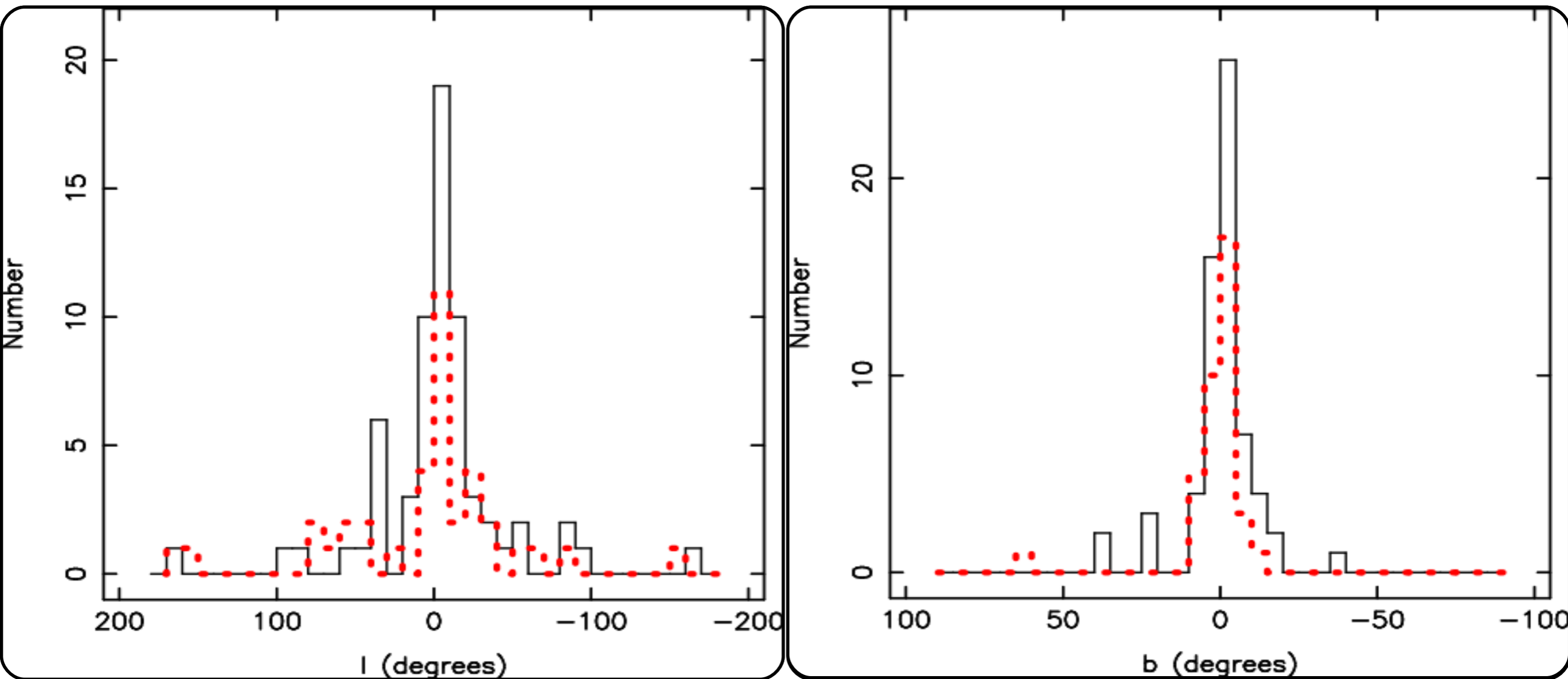
$$\text{Probability } (D > D_{obs}) = Q_{KS}\left(\left[\sqrt{N_e} + 0.12 + \frac{0.11}{\sqrt{N_e}} D\right]\right)$$

with  $N_e = N$       number of  
1 distribution      data pnts

or  $N_e = \frac{N_1 N_2}{N_1 + N_2}$   
2 distributions

# Example K-S test

distribution of neutron stars and black hole X-ray binaries in our Galaxy



Jonker & Nelemans 2004

Probability that BHs and NSs from the same distribution

**37%,  $D=0.19$**

**90%,  $D=0.12$**



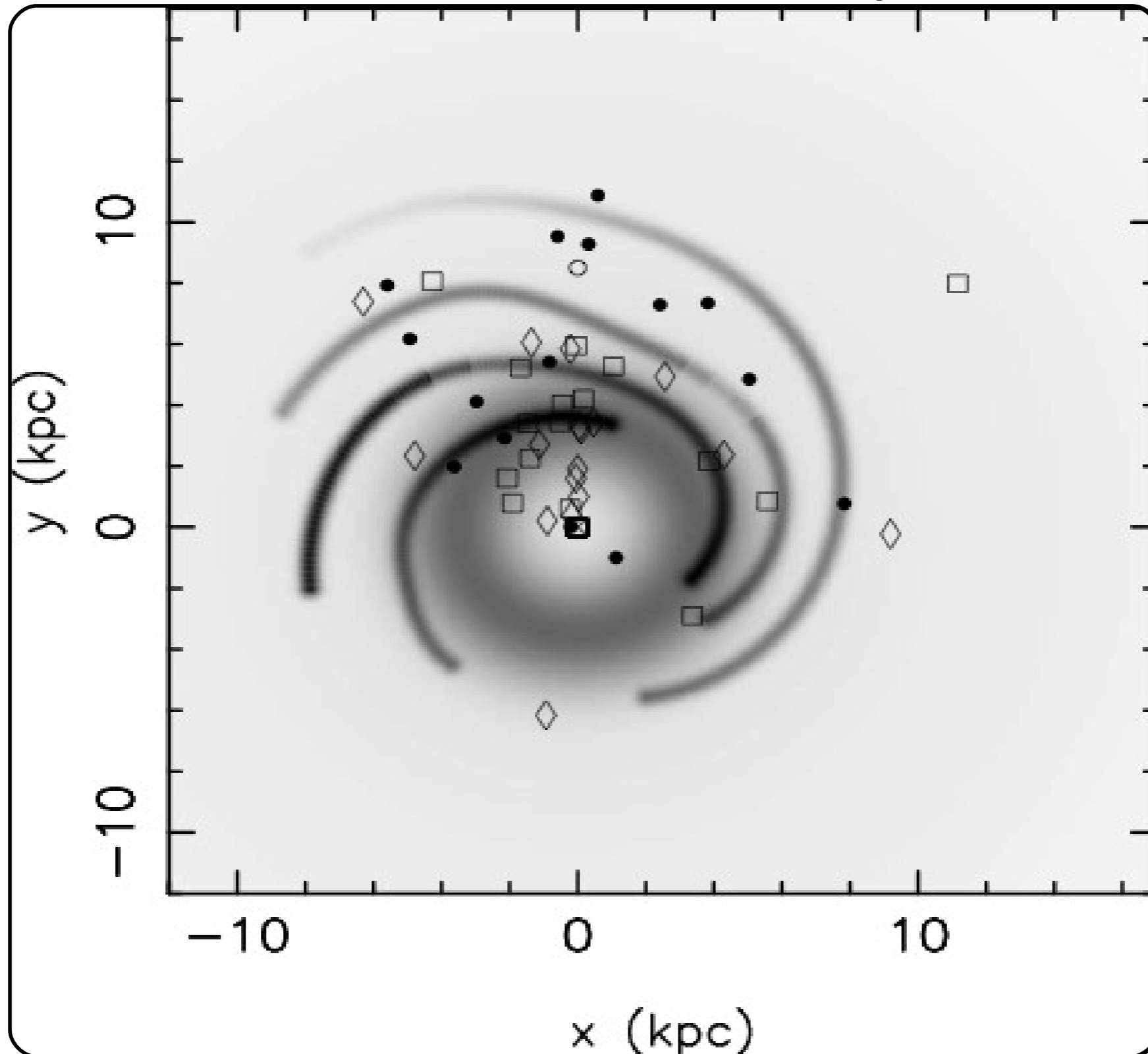
M101 HST image





# 2D K-S test

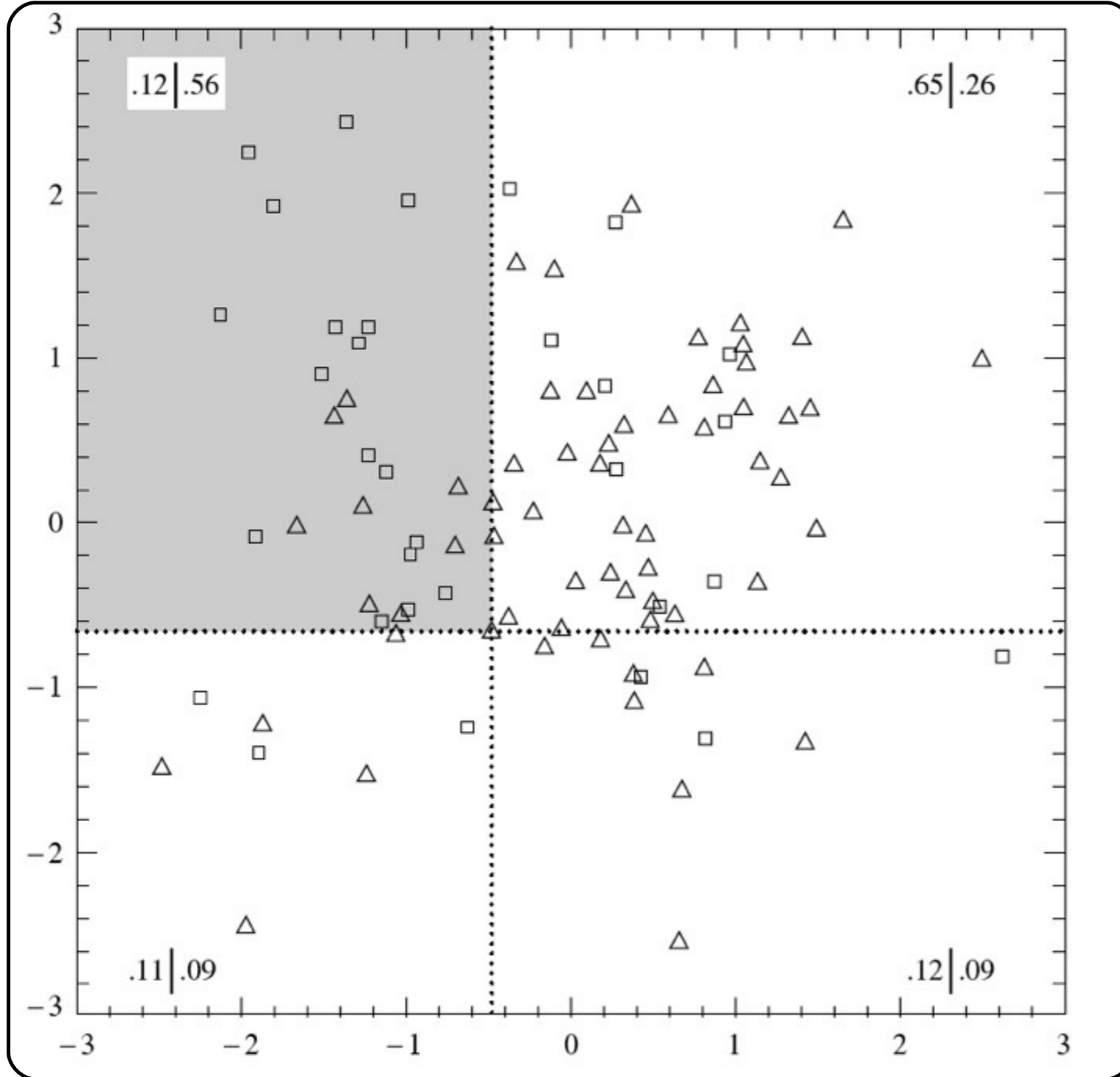
distribution of neutron stars and black hole X-ray binaries in our Galaxy



5.2%  
 $D=0.45$

Jonker & Nelemans 2004    Spiral structure Taylor & Cordess 1993

# 2D K-S test



$$P(D > D_{obs}) = Q_{KS} \left( \frac{\sqrt{ND}}{1 + \sqrt{1 - r^2(0.25 - 0.75/\sqrt{N})}} \right)$$

## 2D K-S test

$$r = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_i (x_i - \bar{x})^2} \sqrt{\sum_i (y_i - \bar{y})^2}}$$

r=correlation coefficient

## Science at SRON staff members

Wim Hermsen: pulsars, INTEGRAL

Jean in 't Zand: type I X-ray bursts

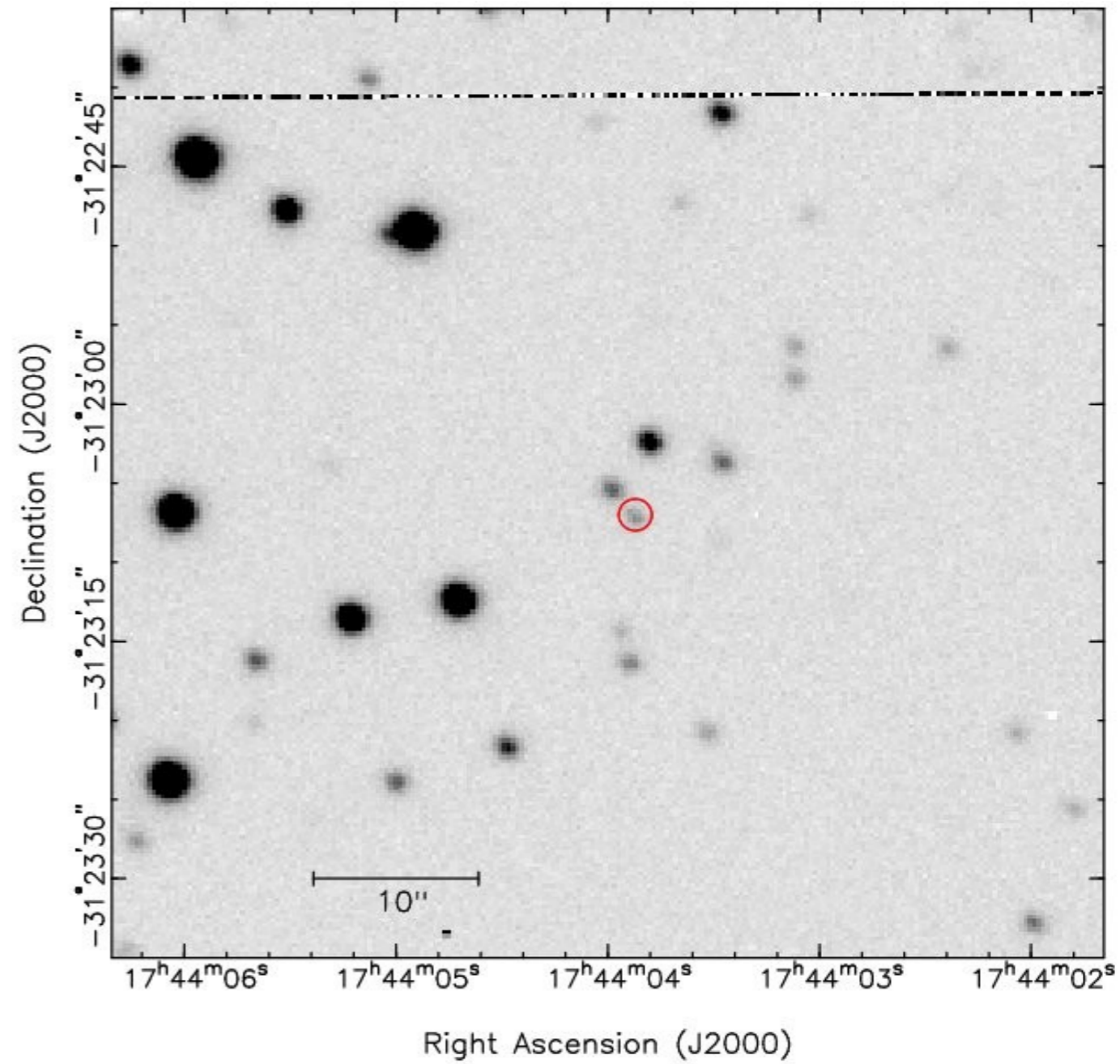
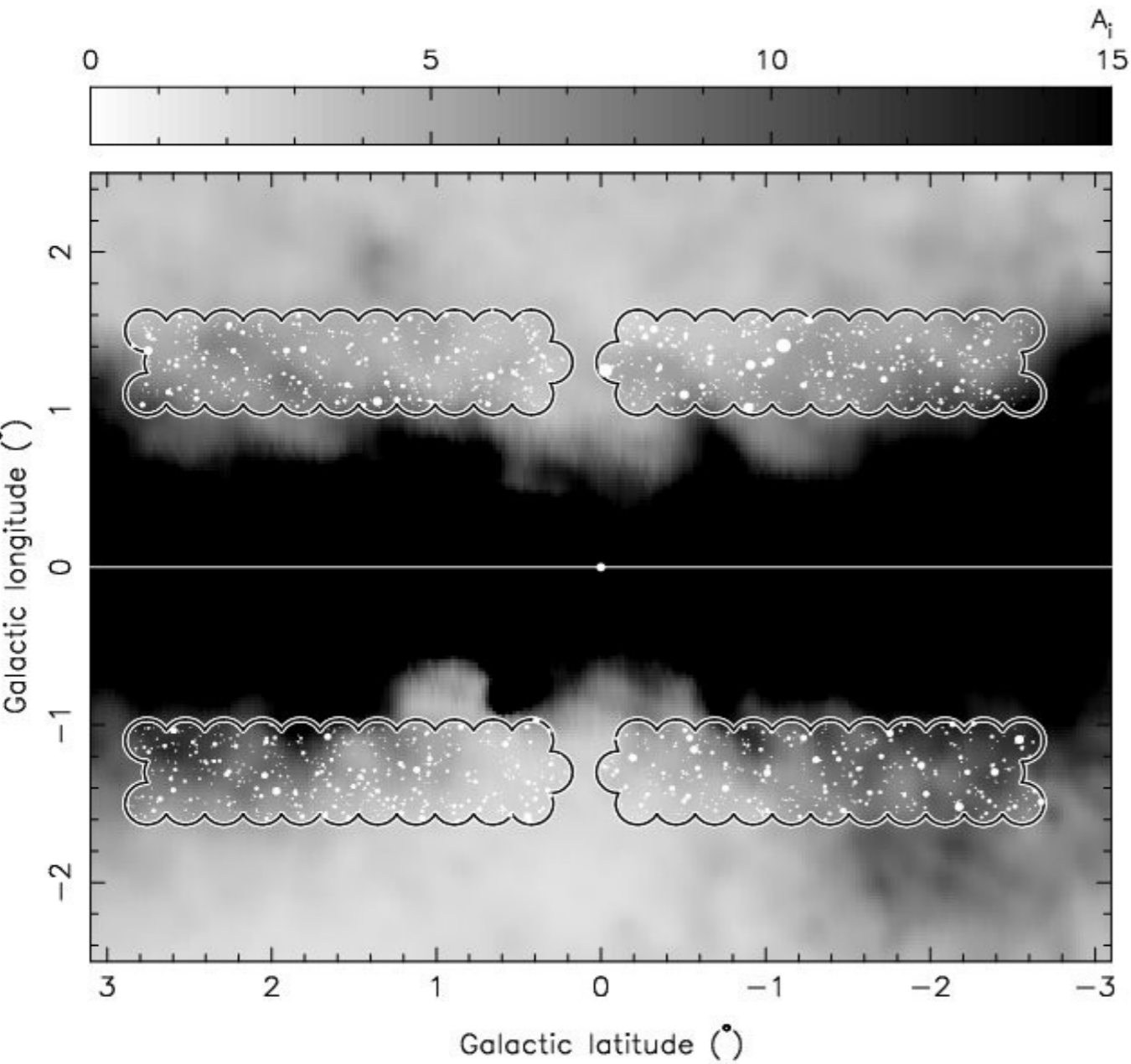
Jelle Kaastra: Clusters of galaxies, ISM studies

Elisa Costantini: ISM studies, AGN

Lucien Kuiper: pulsars, INTEGRAL sources

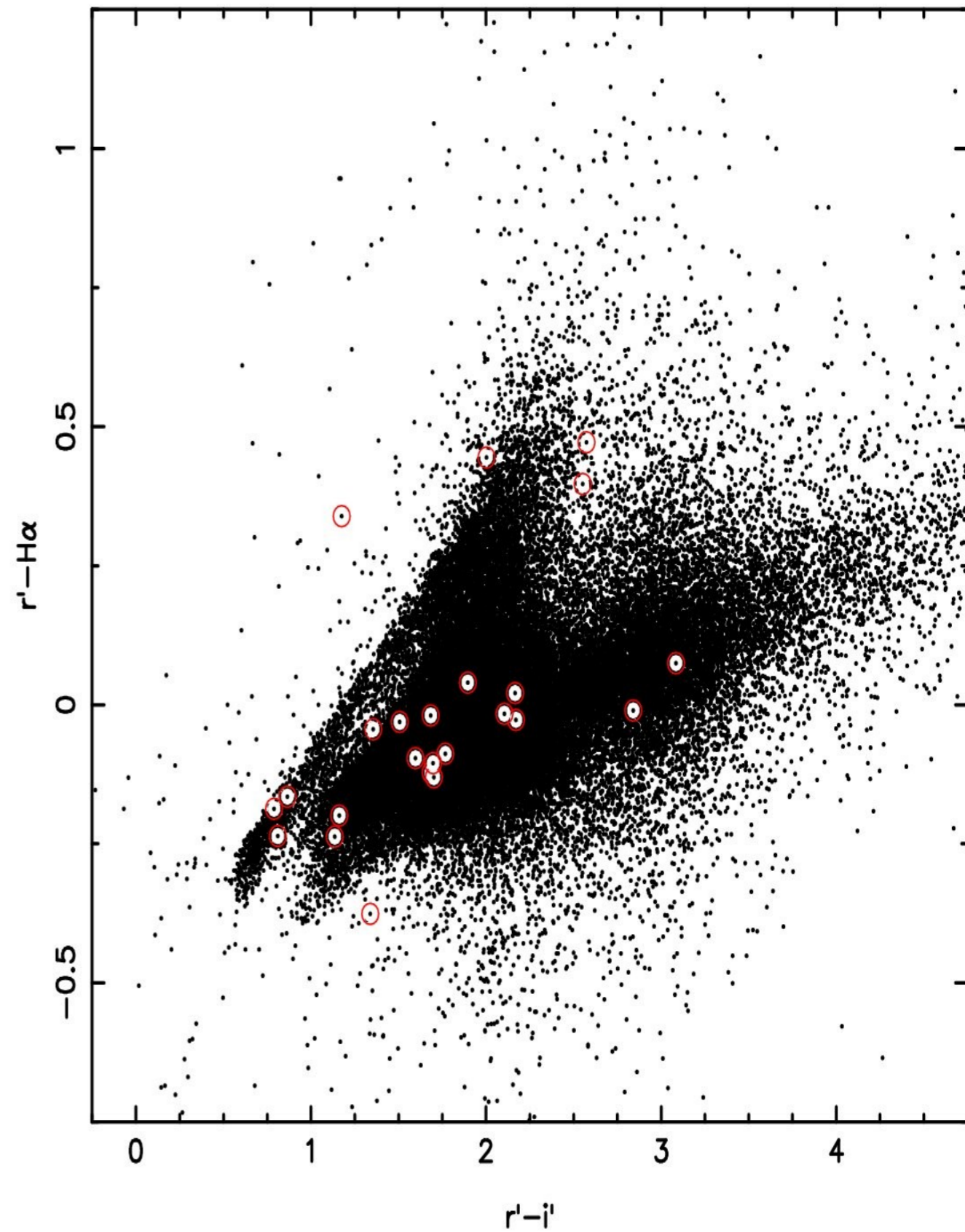
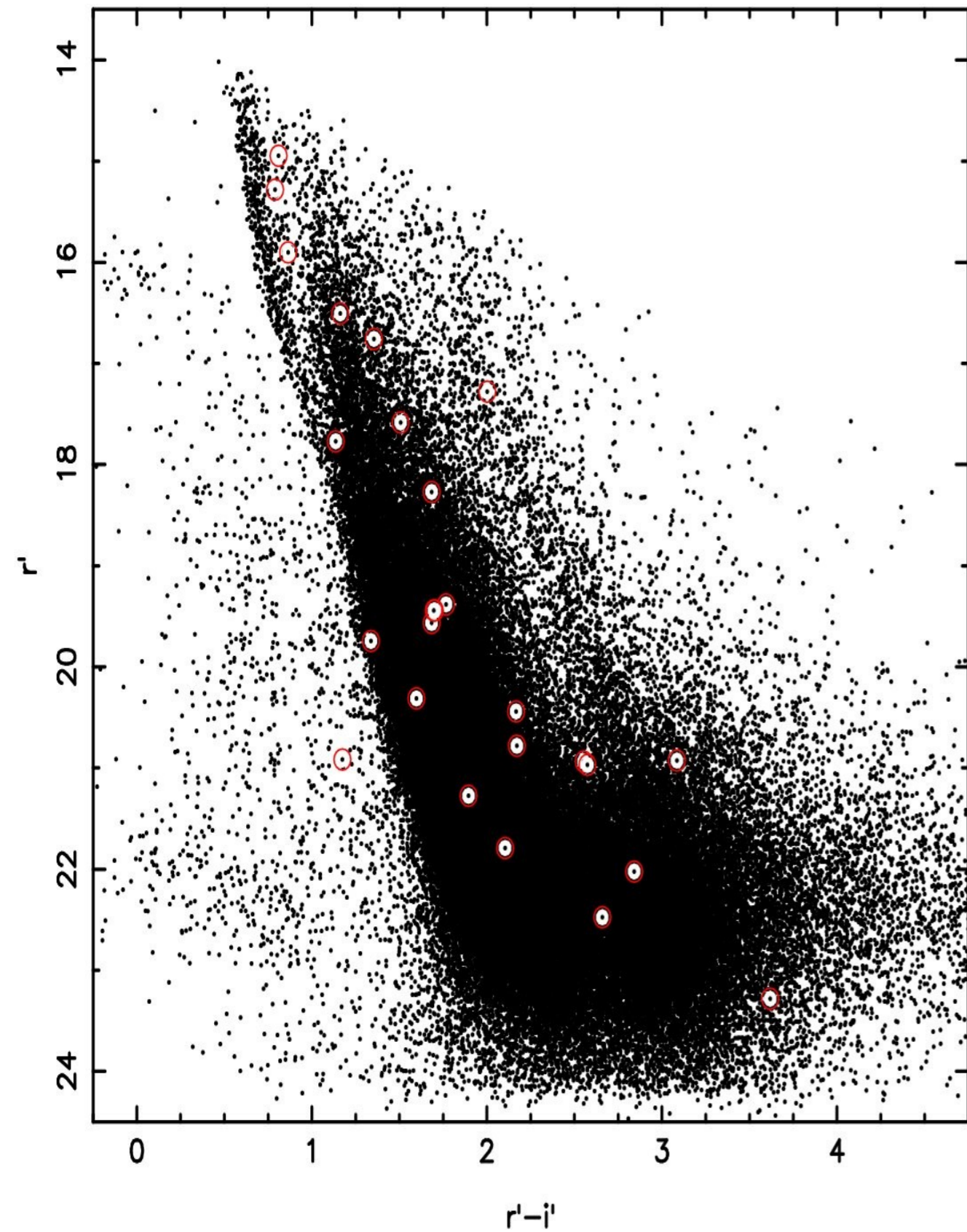
Peter Jonker: low-mass X-ray binaries,  
neutron stars & black holes

# Galactic Bulge Survey





# Galactic Bulge Survey



Core group of people working on the GBS:

**me** (PI)

**Cees Bassa** (post-doc)

**Eva Ratti** (new PhD student)

**Gijs Nelemans** (Nijmegen Univ)

**PhD student**

**Danny Steeghs** (Warwick Univ, UK)

**Manuel Torres** (Harvard-Smithsonian CfA)

Several student projects, including Bachelor student projects