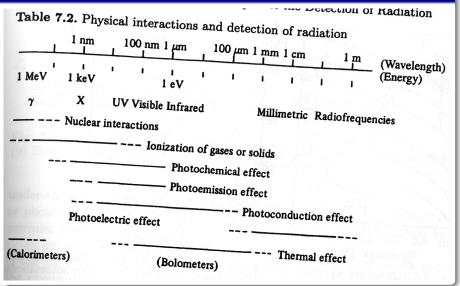
Outline

- Overview
- Photoconductive Detection
- Charge Coupled Devices
- CMOS Devices and CMOS Hybrid Devices
- Array Detector Data Reduction and Problems

Overview

Photon Detection at Different Wavelengths



Operation principle

- illumination changes conductance/resistance of photoconductor
- conductance σ₀ increases due to excess charge carriers in semiconductor
- charge carriers are electron-hole pairs in intrinsic semiconductors
- charge carriers are electrons (n-type) or holes (p-type) in extrinsic semiconductors
- spectral responsivity determined by energy/band gap
- only photons with energies greater than gap are absorbed
- create excess current flow

Responsivity of a photoconductor

• material with conductivity σ_0 produces current density \vec{j} given by

$$\vec{j} = \sigma_0 \vec{E}$$

- \vec{E} : electric field from bias voltage V_B accross photoconductor $(|\vec{E}| \text{ in Volt} \cdot \text{m}^{-1} \text{ and } \sigma_0 \text{ in Ohm}^{-1} \cdot \text{m}^{-1})$
- current density \vec{j} at microscopic scales

$$\vec{j} = Nq\vec{v}$$

- N: volume density of free charge carriers
- *q*: elementary charge
- \vec{v} : drift velocity of charges in applied electric field
- drift velocity $\vec{v} = \mu_c \vec{E}$, μ_c the mobility of charge carrier

Conductivity

 intrinsic semiconductor: distinction between electron conduction and hole conduction: mobilities μ_n for electrons and μ_p, μ_n ≈ 3μ_p

$$\vec{j} = -nq\vec{v_n} + pq\vec{v_p}$$

with *n*, *p* electron/hole densities, $\vec{v_n}/\vec{v_p}$ electron/hole drift velocities (opposite directions)

- q: elementary charge, positive sign
- therefore

$$\sigma_0 = q(n\mu_n + p\mu_p)$$

 reduces to σ₀ = qnμ_n and σ₀ = qpμ_p in case of heavily doped n-type, p-type extrinsic semiconductors

Light on Semiconductor

- monochromatic photon flux *F*(λ₀) on n-type semiconductor
- equilibrium between generation rate of excess conduction electrons and recombination rate:

$$\frac{d\Delta n}{dt} = g - \frac{\Delta n}{\tau_l} = 0$$

- Δn: equilibrium number of excess electrons per unit volume (= excess carrier concentration)
- *τ*_l lifetime of electrons against recombination
- generation rate g:

$$m{g} = rac{\eta_{\lambda_0} m{F}(\lambda_0)}{m{d}}$$

- η_{λ_0} : photon detection efficiency
- d thickness of photoconductor material

Light on Semiconductor (continued)

onductivity:

$$\sigma_0 = qn\mu_n$$

• equilibrium:

$$rac{d\Delta n}{dt} = g - rac{\Delta n}{ au_l} = 0$$

generation rate:

$$g = rac{\eta_{\lambda_0} F(\lambda_0)}{d}$$

• increase in conductivity $\Delta \sigma = \sigma - \sigma_0$ from:

$$\Delta \sigma = q \mu_n \Delta n = rac{q \mu_n \eta_{\lambda_0} F(\lambda_0) au_l}{d} = rac{q \mu_n \eta_{\lambda_0} au_l}{A d} \; rac{\lambda_0}{h c} \; \Phi(\lambda_0)$$

- Φ(λ₀): monochromatic radiation flux in Watt
- A: illuminated area of the photoconductor
- λ₀: wavelength of monochromatic photon flux

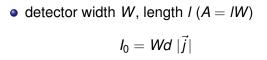
Photoconductive Gain

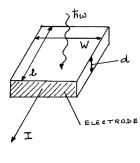
- fixed bias voltage V_B across photoconductors
- relative change in conductivity Δσ/σ related to relative change in current ΔI/I₀ and resistance ΔR/R₀:

$$\frac{\Delta\sigma_0}{\sigma_0} = -\frac{\Delta R}{R_0} = \frac{\Delta I}{I_0} = \frac{I_{pc}}{I_0}$$

- *I*₀, *R*₀ represent photoconductor DC-current/resistance without radiation
- $\Delta I = I_{pc}$ is photon-generated photo-current

Photoconductive Gain (continued)



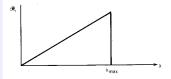


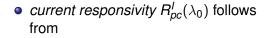
and hence

$$I_{pc} = I_0 \ \frac{\Delta \sigma_0}{\sigma_0} = \frac{\eta_{\lambda_0} q \lambda_0}{hc} \cdot \frac{\tau_I \mu_n V_B}{I^2} \cdot \Phi(\lambda_0)$$

- $\tau_I \mu_n V_B / I^2$ is photoconductive gain G
- transition time τ_{tr} of free charge carriers across photoconductor length *I* $(\tau_{tr} = \frac{l^2}{\mu_n V_B})$, *G* gives ratio between carrier life time against recombination in photoconductor and its transition time, i.e. $G = \tau_l / \tau_{tr}$

Responsivity





$${\it R}^{\prime}_{
m
ho c}(\lambda_0) = rac{{\it I}_{
m
ho c}}{\Phi(\lambda_0)} = {\it G} \eta q \ rac{\lambda_0}{{\it hc}}$$

in Ampere/Watt

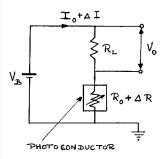
- in practice, photocurrent *I_{pc}* measured over load resistance *R_L* in series with photoconductor resistance *R*₀, translating *I_{pc}* into voltage *V*₀
- spectral voltage responsivity

$$R^V_{
ho c}(\lambda_0) = rac{R_L R_0}{R_L + R_0} \; G \eta_{\lambda_0} q \; rac{\lambda_0}{hc}$$

in Volt/Watt

ideal responsivity as function of wavelength

for constant η_{λ_0}



Responsivity (continued)

to raise responsivity of photoconductor, one should

- enhance quantum efficiency η_{λ_0} by minimizing reflection effects at entrance plane through anti-reflection coatings and by creating a larger cross-section for the internal photo-electric effect.
- increase the carrier life time, which raises the photoconductive gain *G*
- enlarge the carrier mobility μ_c (recall that n-type charge carriers have substantially higher mobility than p-type charge carriers)
- increase the operational bias voltage V_B , which lowers the value of the transition time τ_{tr} in the expression for the photoconductive gain *G*.

Charge Coupled Devices (CCD)

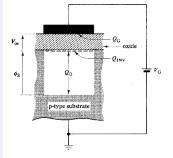
Operation Principle

- CCD is a an array of capacitors
- typically metal-oxide-semiconductor (MOS) capacitor made from silicon (Si) and silicon dioxide (SiO₂) as insulator
- charge position in capacitor is electrostatically controlled by voltage levels
- dynamical application of voltages and relative phases serves a dual purpose:
 - injected charges due to electron-hole pairs generated by photons are stored in capacitor
 - built-up charge (charge packet) can be transferred across semiconductor substrate
- CCD arrays for imaging in near-infrared up to 1.1 $\mu\text{m},$ visible, and X-ray range

Charge Storage in a CCD

- 2 types of charge coupled structures
 - charge packets stored very close to interface between semi-conductor (Si) and overlaying insulator (SiO₂) (surface channel CCDs, SCCDs)
 - charge packets stored some distance away from surface of semiconductor (bulk or buried channel CCDs, BCCDs)
- both devices are very similar
- discuss SCCDs since their concept is easier to understand

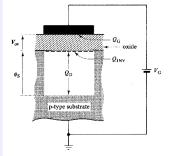
Single CCD Electrode

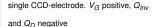


single CCD-electrode. V_G positive, Q_{Inv} and Q_D negative

- metal gate, separated by thin oxide layer (few 0.1 μm) from p-type semiconductor (hole-conduction)
- without voltage bias to gate, uniform distribution of holes (majority free charge carriers) in p-type semiconductor
- gate electrode positive, holes are repelled beneath gate
- *depletion layer* (devoid of free charge) is created
- increased gate voltage extends depletion region into semiconductor
- potential at semiconductor/insulator interface (φ_S) becomes increasingly positive

Single CCD Electrode (continued)





- voltage high enough ⇒ surface potential φ_S attracts electrons (i.e. minority charge carriers in the p-type material) to surface
- electrons form extremely thin (≈ 0.01 µm thick), but very (charge) dense layer, the *inversion layer*
- electrons reside in deep potential well at semiconductor surface, do not recombine with holes, since holes are repelled from depletion layer
- light on single CCD electrode creates electron-hole pair: electrons stored in inversion layer, holes repelled from depletion region

Potential Well

- calculate variation of surface potential φ_S with gate voltage V_G and surface-charge density Q_{Inv} in inversion layer
- p-type substrate is grounded:

$$V_{G} = V_{ox} + \phi_{S}$$

charge neutrality demands

$$Q_G = -(Q_{Inv} + Q_D)$$

- $Q_D = -qN_a x_D$ is surface charge density in depletion layer
- volume charge density -qN_a integrated over thickness of depletion layer x_D
- N_a is density of acceptor doping in p-type semiconductor, q is the elementary charge

Potential Well (continued)

voltage and charge balance from before

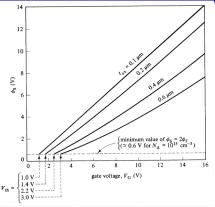
$$egin{array}{rcl} V_G &=& V_{ox} + \phi_S \ Q_G &=& -(Q_{Inv} + Q_D) \end{array}$$

- integration of Poisson equation (electrostatics), x_D = 2εφ_s/qN_a, with ε the dielectric constant (ε = ε₀ε_r).
- substituting in Q_D and writing $Q_G = V_{ox}C_{ox}$ (C_{ox} is oxide capacitance per unit area ($C_{ox} = \epsilon/t_{ox}$ with oxide thickness t_{ox})), surface potential is:

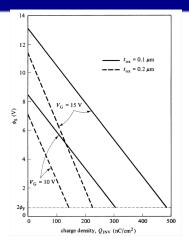
$$\phi_{\mathcal{S}} = V_{G} + V_{0} + \frac{Q_{lnv}}{C_{ox}} - \sqrt{2\left(V_{G} + \frac{Q_{lnv}}{C_{ox}}\right)V_{0} + V_{0}^{2}}$$

• V_0 is a constant $(q \in N_a / C_{ox}^2)$ in Volts

Potential Well (continued)



Surface potential ϕ_S as function of gate voltage V_G for different values of oxide thickness t_{ox} . charge in inversion layer Q_{Inv} is zero in all cases (from Beynon & Lamb, 1980)



Surface potential ϕ_S as function of inversion charge Q_{Inv} for two values of gate voltage V_G and of oxide thickness t_{ox} (from Beynon & Lamb, 1980)

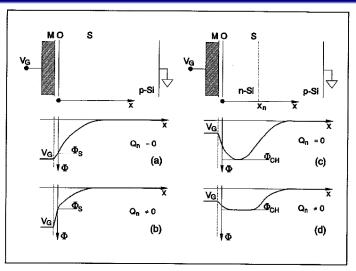
Potential Well (continued)

- surface potential ϕ_S interpreted as *potential well*
- well depth given by magnitude of inversion charge packet Q_{Inv}
- ϕ_s practically linear function of Q_{lnv} and V_G , since constant V_0 is small compared to typical values for V_G ; i.e. $V_0 = 0.14$ Volt for 0.1 μ m thick oxide layer
- since *V_G*= 10 15 Volt:

$$\phi_{\mathcal{S}} = V_{\mathcal{G}} + rac{Q_{\mathit{Inv}}}{C_{\mathit{ox}}}$$
 in good approximation

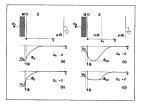
- storage of charge at the Si-SiO₂ interface introduces potential losses of accumulated charge during charge transport, owing to charge trapping in atomic surface states
- to prevent such losses, charge packet should be kept at potential minimum separate from Si-SiO₂ interface, i.e. minimum in bulk-silicon must be created
- can be achieved by adding n-type layer on top of p-type silicon.
 lonised positive ions of the n-type top layer raise positive gate

SCCD vs BCCD



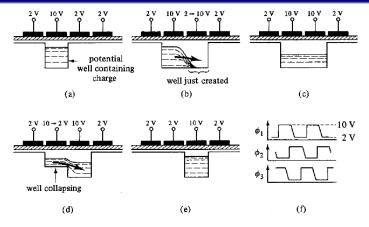
Surface and channel potential for a SCCD ((a) and (b)) and a BCCD ((c) and (d)), with empty ((a) and (c)) and filled ((b) and (d)) wells (from Theuwissen, 1995)

SCCD vs BCCD



- comparison of electron-potential minimum at interface and away from interface
- potential well in n-type Si has minimum deeper in bulk Si (BCCD)
- charge stored and transported in channel embedded in bulk silicon and is not anymore subject to charge loss at surface states
- comparison between empty and partly filled SCCD, (a) and (b), and empty and partly filled BCCD, (c) and (d)
- in BCCD, charge packet flattens minimum of potential well ("neutral layer" that increases in width if it becomes filled with charges)

Charge Transport in a CCD



charge packet transport and clocking waveforms (from Beynon & Lamb, 1980)

- all CCD electrodes at minimum bias (\approx 2 V) to ensure that each MOS capacitor operates in inversion-mode
- potential well under 10 V electrode is much deeper than those under the 2V electrodes

Charge Transfer Process

- equations for charge transfer process based on current density and continuity equation
- for n-type channel (electron charge):

$$j(x,t) = q\mu_n n(x,t) \frac{\partial \phi(x,t)}{\partial x} + qD_n \frac{\partial n(x,t)}{\partial x}$$
$$\frac{\partial n(x,t)}{\partial t} = \frac{1}{q} \frac{\partial j(x,t)}{\partial x}$$

- charge propagation in x direction (no vector treatment)
- n(x, t) is electron density, μ_n electron mobility, and D_n electron diffusion coefficient
- first right-hand term refers to drift of charge packet under gradient in electric potential
- second term refers to thermal diffusion under presence of a density gradient

Charge Transfer Process (continued)

diffusion coefficient related to mobility of charge carriers μ_n

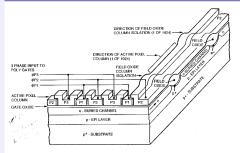
$$\frac{D_n}{\mu_n} = \frac{kT}{q}$$

- or drift due to
 - self-induced fields: in gradient in charge concentration, charges of same type will mutually repel and reshuffle concentration of charge carriers in such a way that gradient becomes zero
 - fringing fields: charges are forced to move due to the existence of electric fields generated by the various voltage levels on the gates
- equalizing of charge concentration under electrodes two and three governed by drift speed due to self-induced fields and thermal diffusion
- effective diffusion coefficient *D_{n,eff}* describes both processes
- for large charge packets mainly self-induced drift
- for small charge packets (e.g. < 1% of well charge capacity) mainly thermal diffusion dominates and slows the transfer

Charge Transfer Efficiency

- charge transfer mechanisms are not perfect
- charge transfer efficiency (CTE) is ratio of charge transferred to initial charge
- typical values of CTE are of the order 0.99999 for a good device

CCD Structure



- must limit extent of potential well in orthogonal direction
- *lateral confinement* with *channel-stop diffusion*, heavily doped region of semiconductor relative to neighboring regions
- region has large conductivity σ relative to surrounding material and quenches surfaces potential ϕ_S so that no depletion region can be formed
- 1-D columns or rows are implemented in CCD structure along which charge transfer occurs, isolated from neighboring columns (rows)

Charge capacity and transfer speed in CCD structures

- maximum amount of charge in CCD pixel depends mainly on clock voltages and electrode area
- considering an SCCD, full-well storage capacity is in good approximation given by oxide capacity under gate electrode (*A_{elec}C_{ox}*) and gate voltage *V_G*:

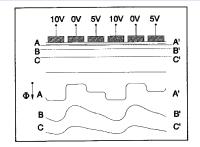
$$A_{elec}C_{ox} = rac{Q_{lnv}}{V_G} \implies Q_{lnv} = A_{elec}C_{ox}V_G$$

- *C*_{ox} is oxide capacitance per unit area, *A*_{elec} is electrode geometric area
- with $A_{elec} = 10 \times 20 \mu m^2$, $t_{ox} = 0.1 \mu m (C_{ox} = \epsilon_{ox}/t_{ox})$ and $V_G = 10$ V: in that case $Q_{Inv} = 0.6 \text{ pC} \approx 3.6 \cdot 10^6$ electrons.

Charge Transport

- intrinsic speed of charge transport in CCD governed by transport equation, depending on the time constants for self-induced drift, thermal diffusion and fringe field drift.
- in SCCD: time constant for self-induced drift is a function of charge density, *C*_{ox} and the interelectrode spacing.
- For $C_{ox} = 1$ pF, $Q_{Inv} = 10^{12}$ cm² and spacing 25 μ m, the time constant $\tau_{Si} = 0.14 \ \mu$ s
- time constant for thermal diffusion of an electron packet (D_n ≈ 10 cm²⋅s⁻¹) amounts to 0.25 μs
- high frequency limit would appear to be a few MHz, however the fringing field of the neighboring gate electrodes aid the transfer considerably, especially when thermal diffusion is dominant and clocking frequencies up to 15 MHz can be used for SCCDs

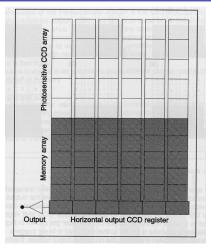
Fringing Fields





- for BCCD, speed dominated by fringing field of neighboring gate due to depth of charge channel
- potential levels do not exhibit flat structure of Si-SiO₂ interface but have continuous gradient along which charge can drift
- BCCDs, with usually smaller charge packets, can be read out at much higher frequencies, up to 300 MHz, with acceptable CTE

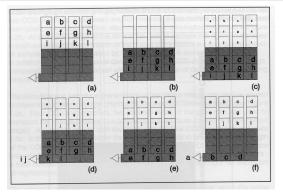
Focal plane architectures



Architecture of frame-transfer CCd array (from Theuwissen, 1995)

- astronomical CCD imaging arrays can be subdivided into full-frame and frame-transfer arrays
- interline-transfer arrays are often used in commercial CCD cameras
- CCD has photosensitive array and a memory array coupled to a linear output register
- *full-frame* device lacks storage section
- shutter interrupts illumination during readout

Frame Transfer Operation



Working principle of frame-transfer CCD (from Theuwissen, 1995)

- transfer needs to be done quickly to prevent disturbance by light falling on the image section during read-out
- during readout, all CCD cells in image array are again biased in integration mode

Modulation Transfer Function

- pixel size Δx , sampling of image is array of normalized window functions $\frac{1}{\Delta x} \prod \left(\frac{x}{\Delta x}\right)$
- spatial frequencies (s) associated with window function from its Fourier transform sinc(sΔx)
- pixel pitch in image plane $x_0 \Rightarrow$ Nyquist frequency $s_N = \frac{1}{2x_0}$
- normalizing spatial frequency s with s_N yields geometrical MTF for linear array of pixels Δx with pitch x₀ (s₀ = s/s_N)

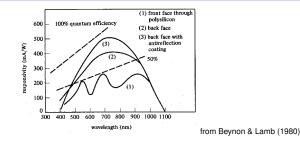
$$\textit{MTF}_{\textit{geo}} = \mathsf{sinc} rac{s_0 \Delta x}{2 x_0}$$

• for contiguous pixels (e.g. frame-transfer CCD array), $\Delta x \approx x_0$ yielding:

$$MTF_{FT} = \operatorname{sinc} \frac{s_0}{2}$$

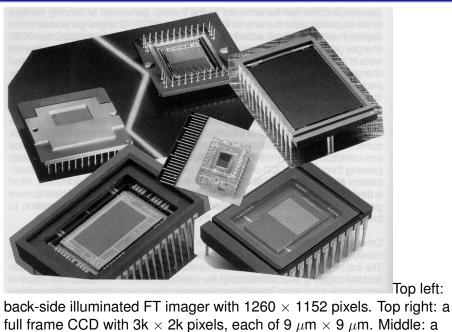
with $MTF_{FT} = 0$ for $s_0 = 2$, i.e. $s = 2s_N$

Wavelength response of CCDs



- at optical wavelengths: illumination through front surface or back-surface (back-illumination)
- front illumination:
 - poly-silicon gate electrodes that transmit light
 - strongly wavelength dependent absorption and interference effects occurring in thin poly-silicon gate layer (\approx 0.5 μ m) and thin oxide layer (\approx 0.1 0.2 μ m)
 - blue-responsivity strongly suppressed by absorption in poly-silicon gate

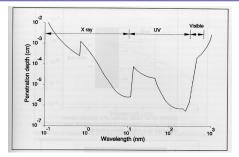
CCDs



CCD Response

- back-illumination requires thinning of silicon substrate for photon-generated charges to reach potential wells
- charge transport can be aided by building an electric field gradient into the semi-conductor by increasing substrate doping concentration in regions close to silicon surface
- this accelerates photon-generated carriers towards front surface and potential wells
- particularly useful for increasing blue-responsivity where charge carriers are generated close to rear silicon surface
- response can be further improved by minimizing the reflection of light from back surface employing a λ/4 thick layer of silicon monoxide at wavelength of interest
- quantum efficiency of about 50 % with back-illumination can be raised to a peak efficiency of about 90% by using the proper antireflection coating

CCDs from X-rays to the Infrared



Penetration depth of silicon as a function of wavelength (from Theuwissen, 1995)

- wavelengths longer than 1 μ m, for which the photo-electric absorption coefficient in silicon is too low ($h\nu_{IR}$ < bandgap) and all photons pass through silicon without being absorbed
- for wavelengths shorter that 0.4 μm and longer than 10 nm the opposite is the case as compared to the IR range: the absorption is very high since not only silicon, but also the silicon oxide layer has a very high absorption coefficient in this wavelength regime

Infrared CCDs

- wavelengths longer than 1 μ m, for which the photo-electric absorption coefficient in silicon is too low ($h\nu_{IR}$ < bandgap) and all photons pass through silicon without being absorbed
- infrared photons need to be converted first into electrons, e.g. by means of so-called Schottky-barrier structures in which pixels are used made out of platinum-silicide (PtSi)
- array of these detectors is then coupled to a CCD read-out system
- responsivity in the thermal IR can theoretically be extended in this way to approximately 5.6 μ m
- however, quantum efficincy of PtSi CCD detectors is only about 1%

CCDs at Ultraviolet Wavelengths

- UV-sensitive phosphor on top of active area down-converts energy of UV-photons to longer wavelengths
- back-illumination is an option. However, due to the high absorption, the substrate of the CCD has to be thinned to typically 10 μm, which is a very expensive process and requires subsequently very delicate handling of the device
- deep depletion of a lightly-doped, high-resistivity substrate, such that the depletion region under the CCD gates extends to the back of the siliconwafer
- charge carriers generated by the UV illumination are swept to the front side into the potential wells by the electric field of the deep depletion layer. This approach does not require the extreme thinning mentioned above for conventional high-doped material, a thickness of 50 μm still allows adequate collection of charge owing to the deep depletion field.

CCDs for X-ray Astronomy

- CCDs useful for X-ray astronomy where X-ray photon flux is sufficiently low to register the (small) charge packet associated with a single X-ray photon
- in contrast to the optical application, exposures yielding no more than one X-ray photon per 100 pixels is pursued before read-out, since in this case both spectral an spatial information can be obtained simultaneously
- magnitude of charge packet represents the energy of absorbed X-ray photon.
- deep depletion CCDs (30 50 μ m) provide a high quantum efficiency (> 90%) over a wide X-ray range (0.2 10 nm)
- ideally suited as imaging spectrometer behind grazing incidence X-ray telescope
- back-illumination avoids problem of penetrating the gate structure and the oxide layer, gives quite superior response to low-energy X-rays (2 – 10 nm)
- deep depletion layer minimizes effect of charge diffusion of the

Complementary Metal Oxide Semiconductor (CMOS) Detectors

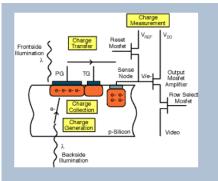
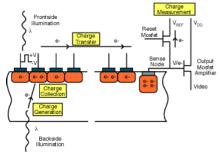
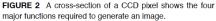


FIGURE 1 A cross-section of a CMOS pixel shows the four major functions required to generate an image.

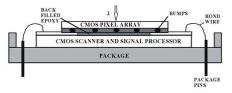




CMOS vs. CCD

- advantages:
 - standard semiconductor processing
 - low power consumption (\approx 1% of CCD)
 - random access to regions of interest
 - blooming and streaking much reduced compared to CCDs
 - additional electronics can be integrated on chip and in pixel (smart sensor)
 - non-destructive readout
- o disadvantages:
 - small geometric fill factor (microlenses can help)
 - typically larger read noise

CMOS Hybrid Detectors



- combine CMOS readout multiplexer bonded to a photosensitive material layer pixel by pixel
- combines sensitivity of CCD with CMOS readout flexibility
- can also use HgCdTe or InSb for infrared sensitivity
- disadvantages:
 - expensive due to pixel-by-pixel bonding
 - differential thermal expansion of materials
 - image lag

Typical Array Detector Data Reduction

- science frame S, exposure time t_S
- dark frame *D*, exposure time *t*_D
- bias frame *B*, zero exposure time
- flat field frame F, exposure time t_F
- corrected (calibrated) image

$$S' = rac{S - rac{t_S}{t_D}(D-B) - B}{F - rac{t_F}{t_D}(D-B) - B}$$

Array Detector Problems: Read Noise

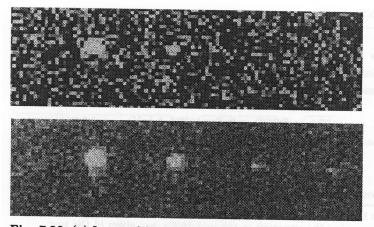
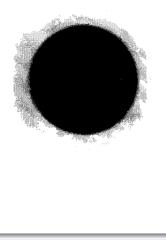


Fig. 7.28. (a) Image of four source points, by a CCD with $\sigma_{\rm R} = 7.6 \, {\rm e}^-$ rms. (b) The same image in multiple readout (N = 64), where $\sigma_{\rm R} = 0.97 \, {\rm e}^-$ rms. The faintest source corresponds to a signal of 3.5 photocharges. (After Janesik et al., in *The CCD in Astronomy*, ASP Conf. Ser. 8, 1989)

Array Detector Problems: Bias Shift





Array Detector Problems: Cross Talk

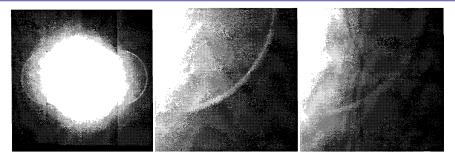


Figure 2: (left) Image similar to Figure 1 except shown in positive contrast and a range from 0 to 0.005 of the maximum illumination level. (center) Detail of left image channel 4 exposed at low light level. (right) Detail of channel 4 exposed at high light level.

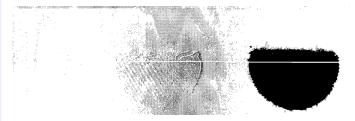
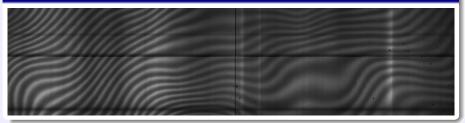


Figure 5: Negative contrast display of cross talk among four quadrants of a Rockwell Scientific Company HyViSI-1024 camera. The range shown is 0 to 5% of the maximum illumination level. This image has been dark-corrected. Large-scale shading is scattered light.

Array Detector Problems: Blooming



Array Detector Problems: Fringes



Other Array Detector Problems

- o photon (shot) noise
- dark current noise; dark current is reduced by factor of 2 for every 7 K of cooling
- non-linearity of electronic amplification
- image lag