Optics and Instruments 2015: Exercises on Foundations of Optics (Due on 16 September 2015 at 13:45)

C.U.Keller

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1 Interaction between Electromagnetic Wave and Matter

Show that the interaction between an electromagnetic wave and matter (assume electrons moving at speed v) is a factor of v/c smaller for the magnetic field component of the electromagnetic wave as compared to the electric field component.

2 Energy Densities of an Electromagnetic Wave

Show that the energy densities of the electric and magnetic field components of an electromagnetic wave are equal.

3 Harmonic Spherical Waves

Show that the wave equations for a dielectric $(\sigma = 0)$

$$\nabla^2 \vec{E} - \frac{\mu\epsilon}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} = 0 \tag{1}$$

derived from the Maxwell equations also have a solution that corresponds to purely spherical waves of the form

$$\psi(r,t) = \frac{A}{r} e^{i(kr - \omega t)}, \qquad (2)$$

where A is a constant and r the radial distance from the center/source of the wave.

4 Reflectivity

Use the Fresnel equations for normal incidence (incoming beam of light is perpendicular to interface) to calculate the intensity of the reflected light for

- 1. window glass with an index of refraction of 1.55,
- 2. diamond with an index of refraction of 2.42, and
- 3. aluminum with a complex index of refraction of 0.8 + i6.0.