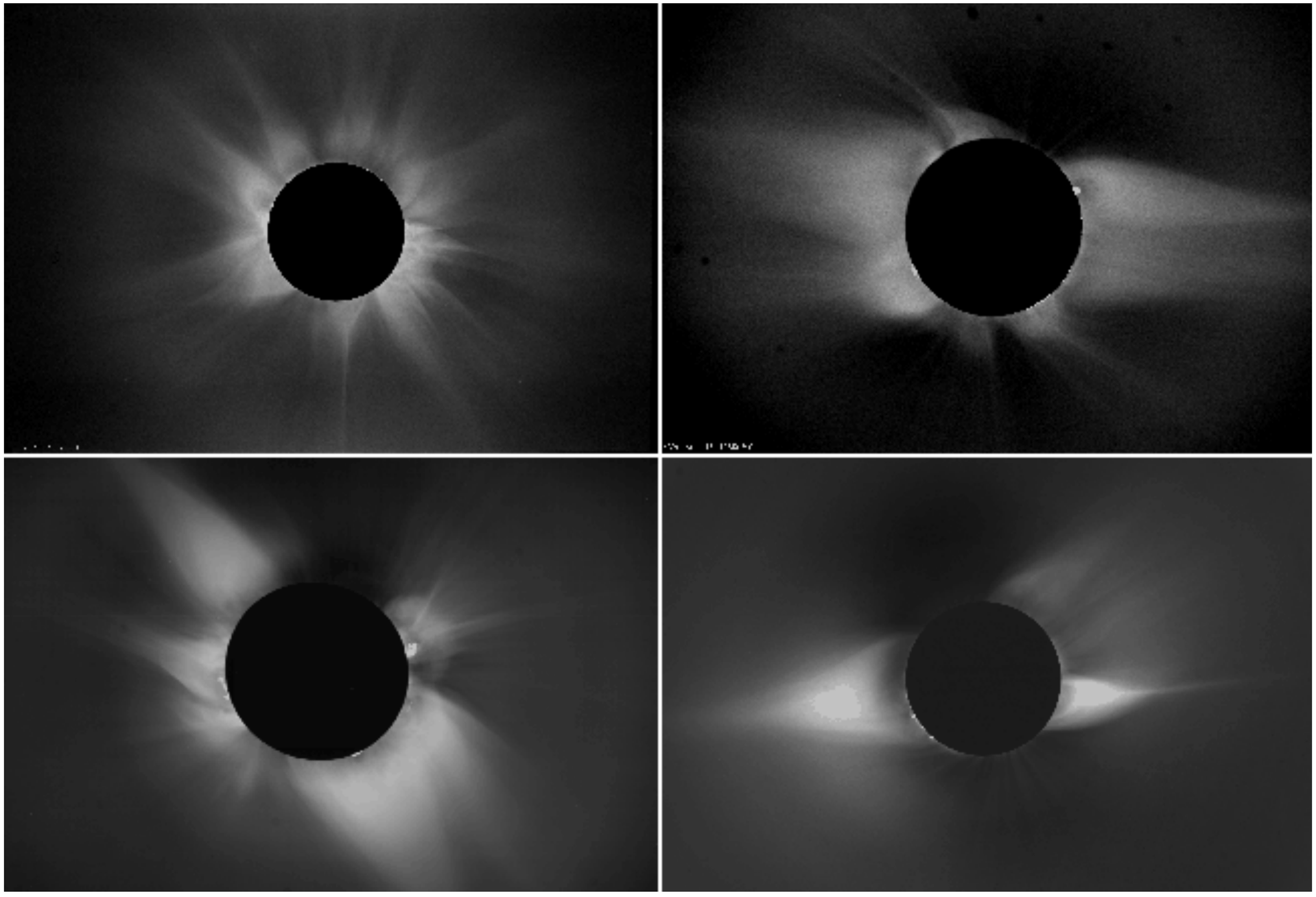
Coronagraphs

ATI 2017 - Lecture 11

Matthew Kenworthy // Leiden Observatory

Solar Corona

Solar eclipses revealed wealth of structure in outer layers of Sun



http://celebrating200years.noaa.gov/breakthroughs/coronagraph/welcome.html

Bernard Lyot

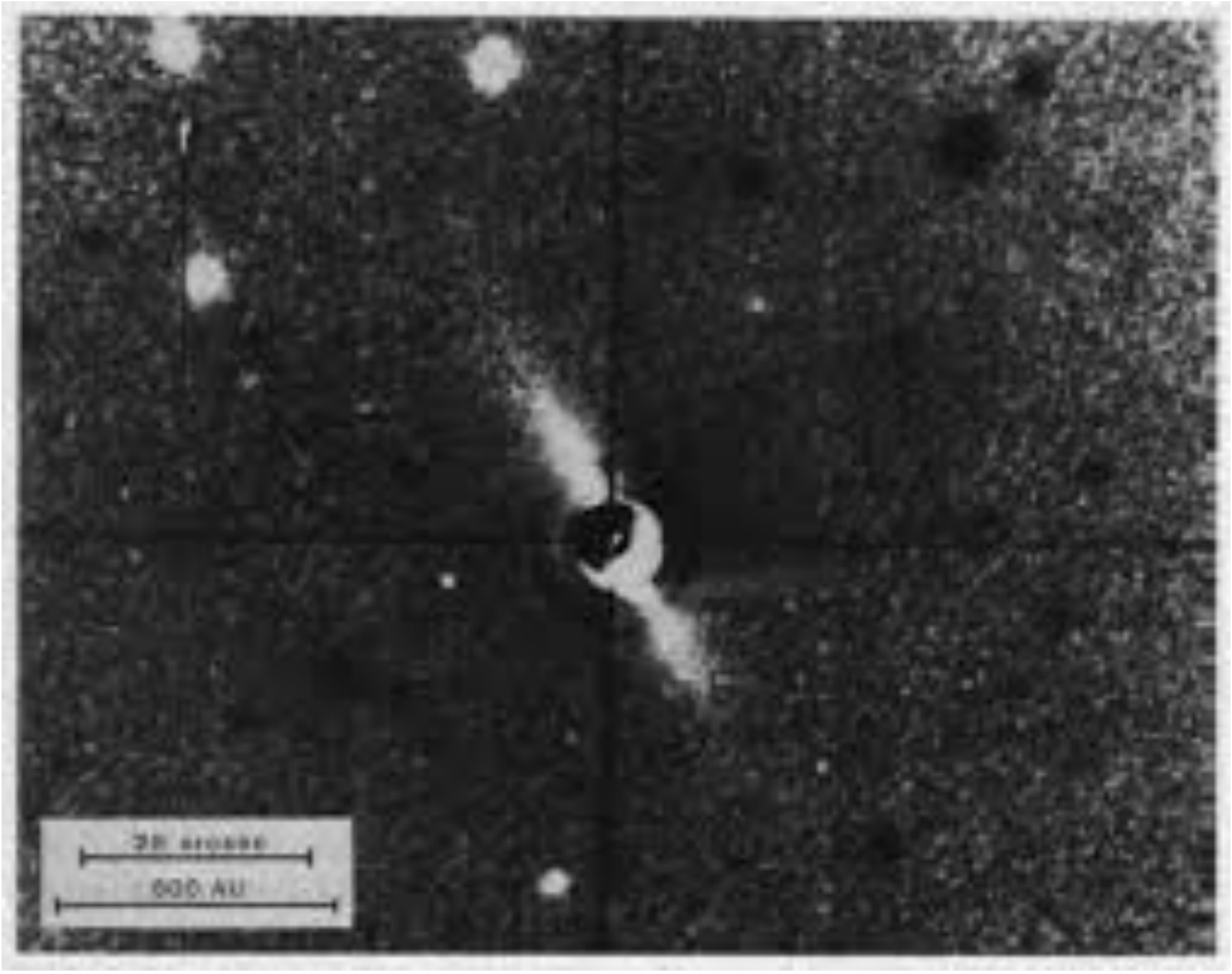
Bernard Lyot sitting at his Coronagraph at the Pic du Midi observatory in France ca. 1939.

French astronomer and instrument maker

Wanted to study the Sun's corona without waiting for an eclipse

Invented the CORONAGRAPH in 1939 to block sunlight and take photos of the corona.

First circumstellar disk imaged in 1984



Smith and Terrile 1984

Fomalhaut Debris Disk

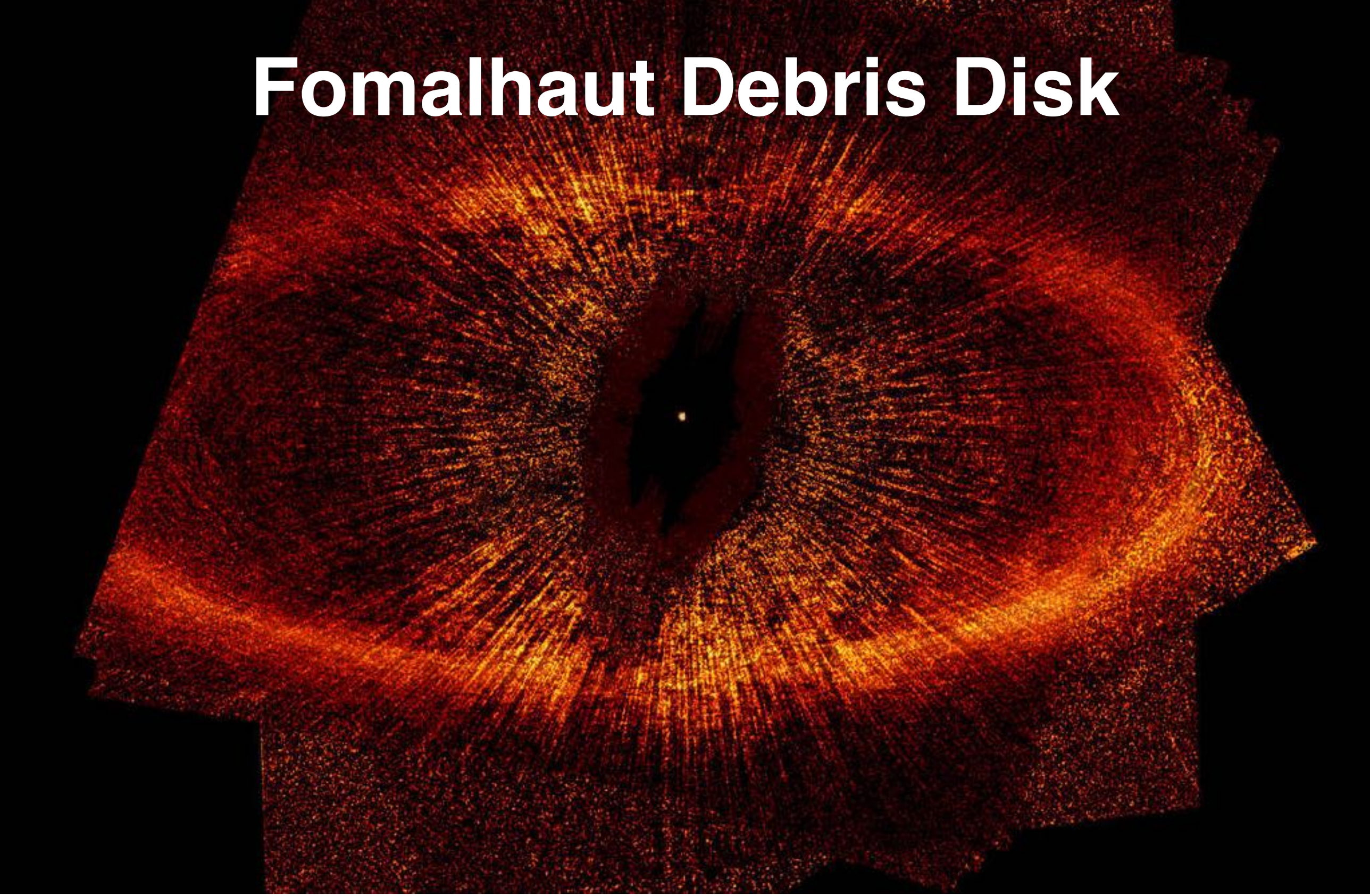
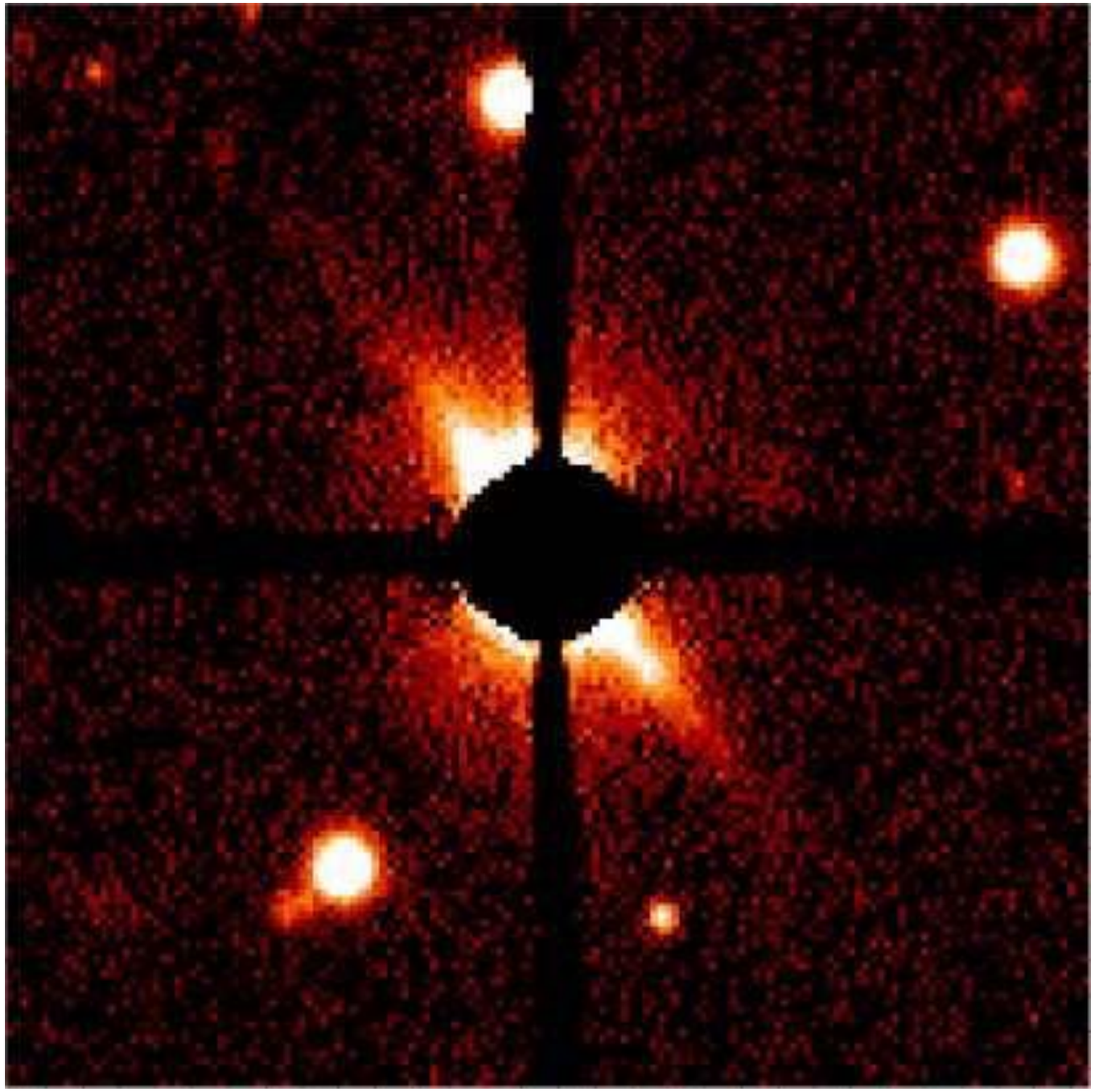


Image Credit: NASA, ESA, P. Kalas and J. Graham (University of California, Berkeley) and M. Clampin (NASA/GSFC)

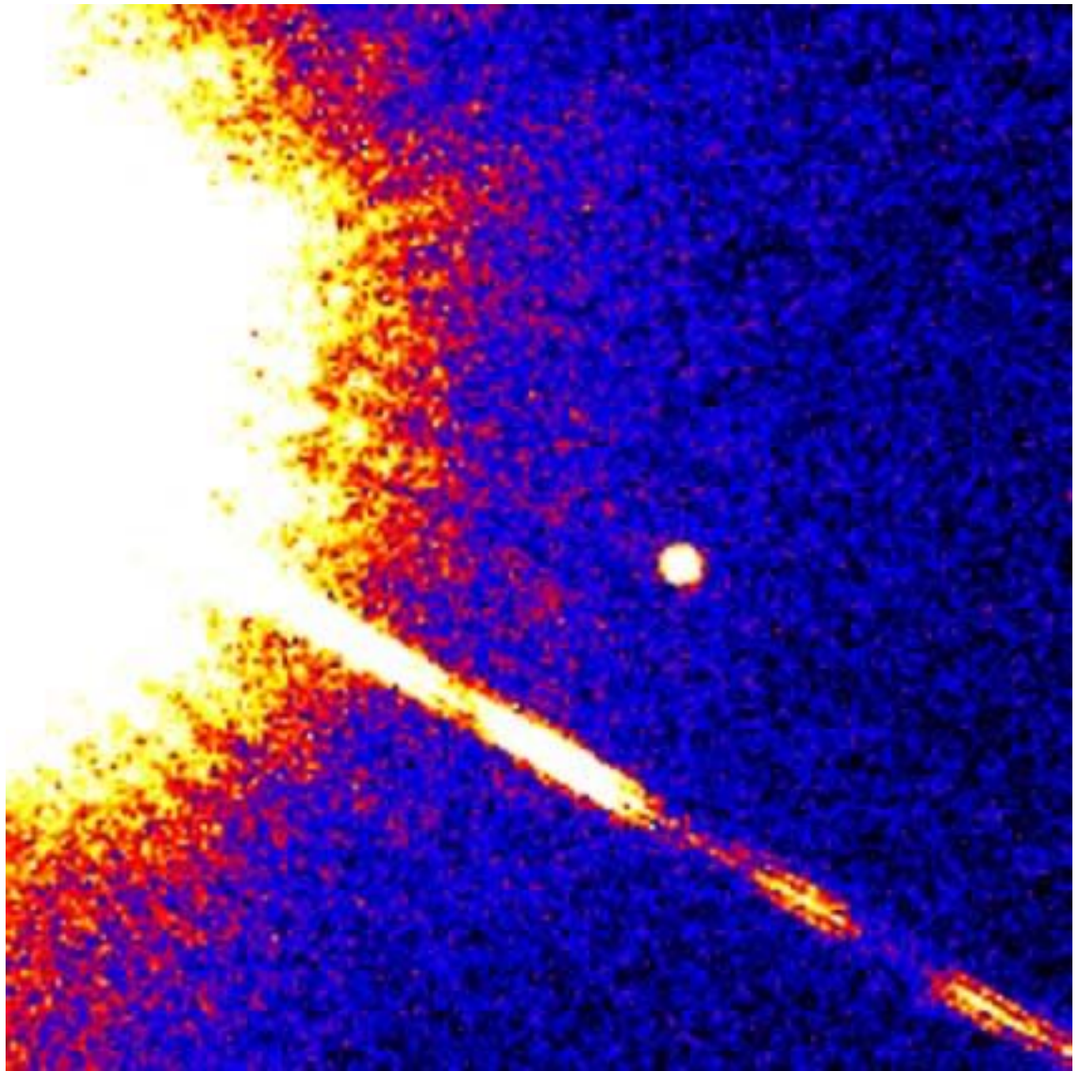
AU Mic



Paul Kalas 1990

First Brown Dwarf

Discovered in 1994 from Palomar 60 inch telescope

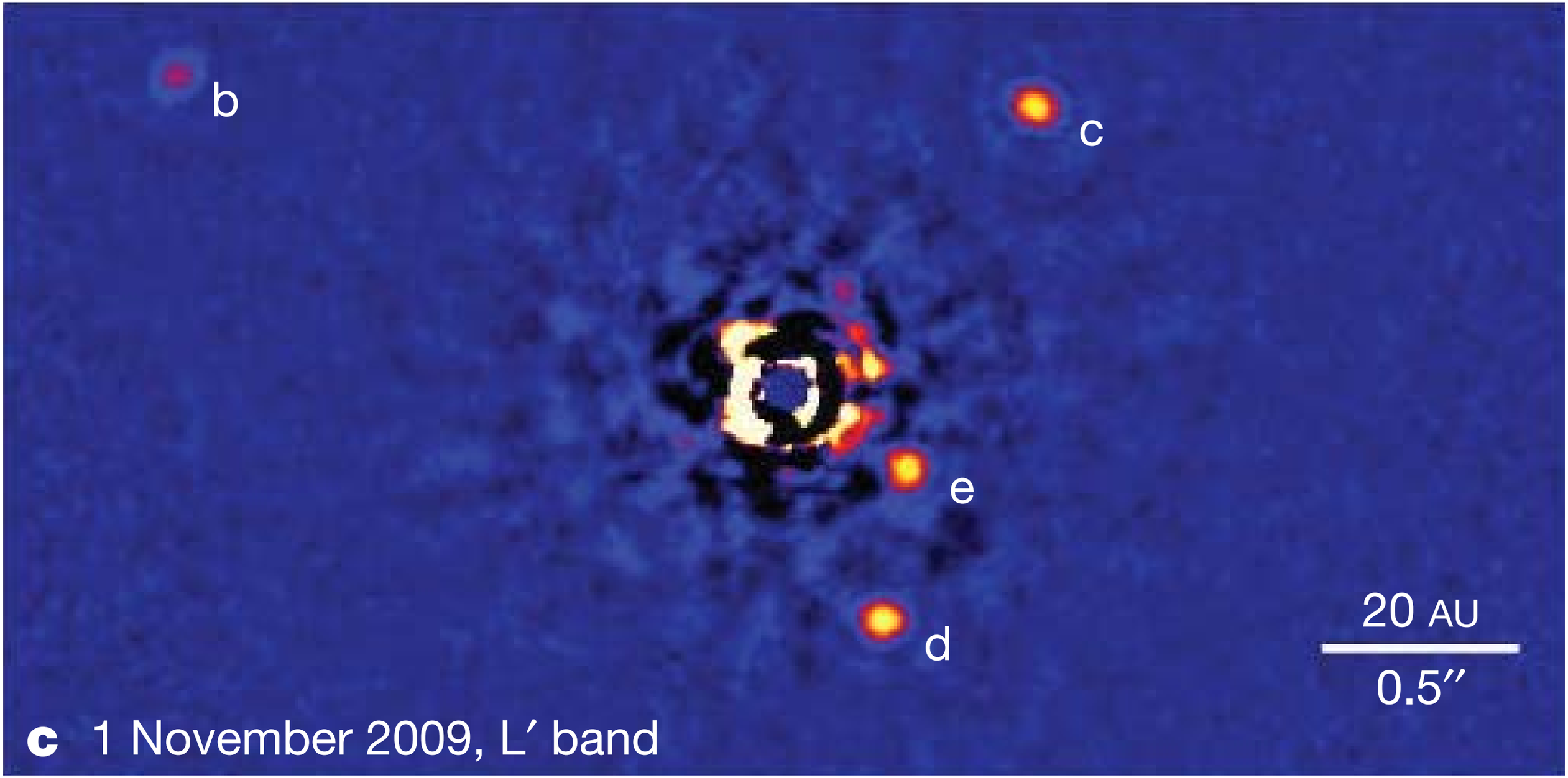


Gliese 229B - taken with HST

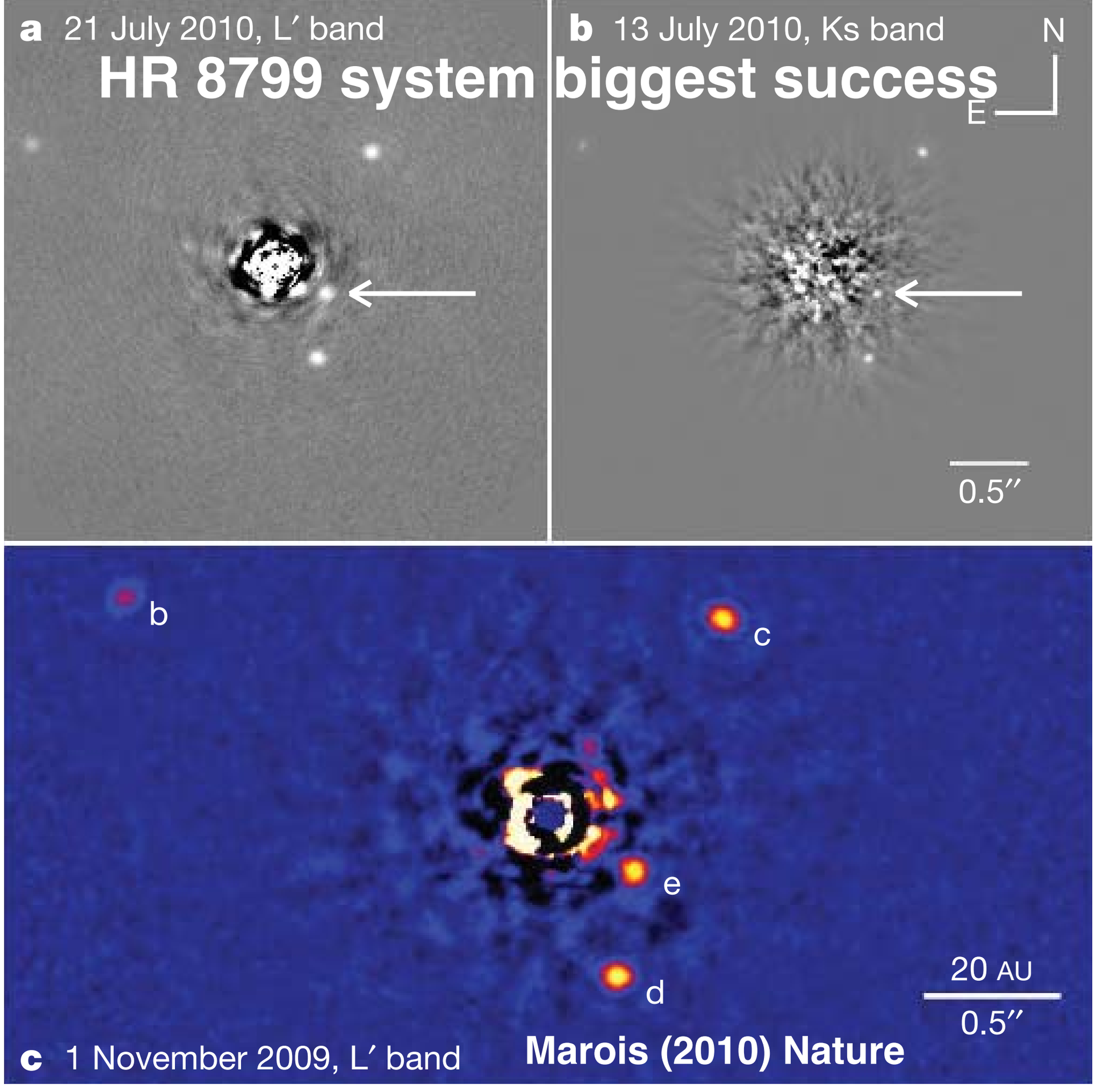
Credit: S. Kulkarni (Caltech), D.Golimowski (JHU) and NASA

…to planets

HR 8799



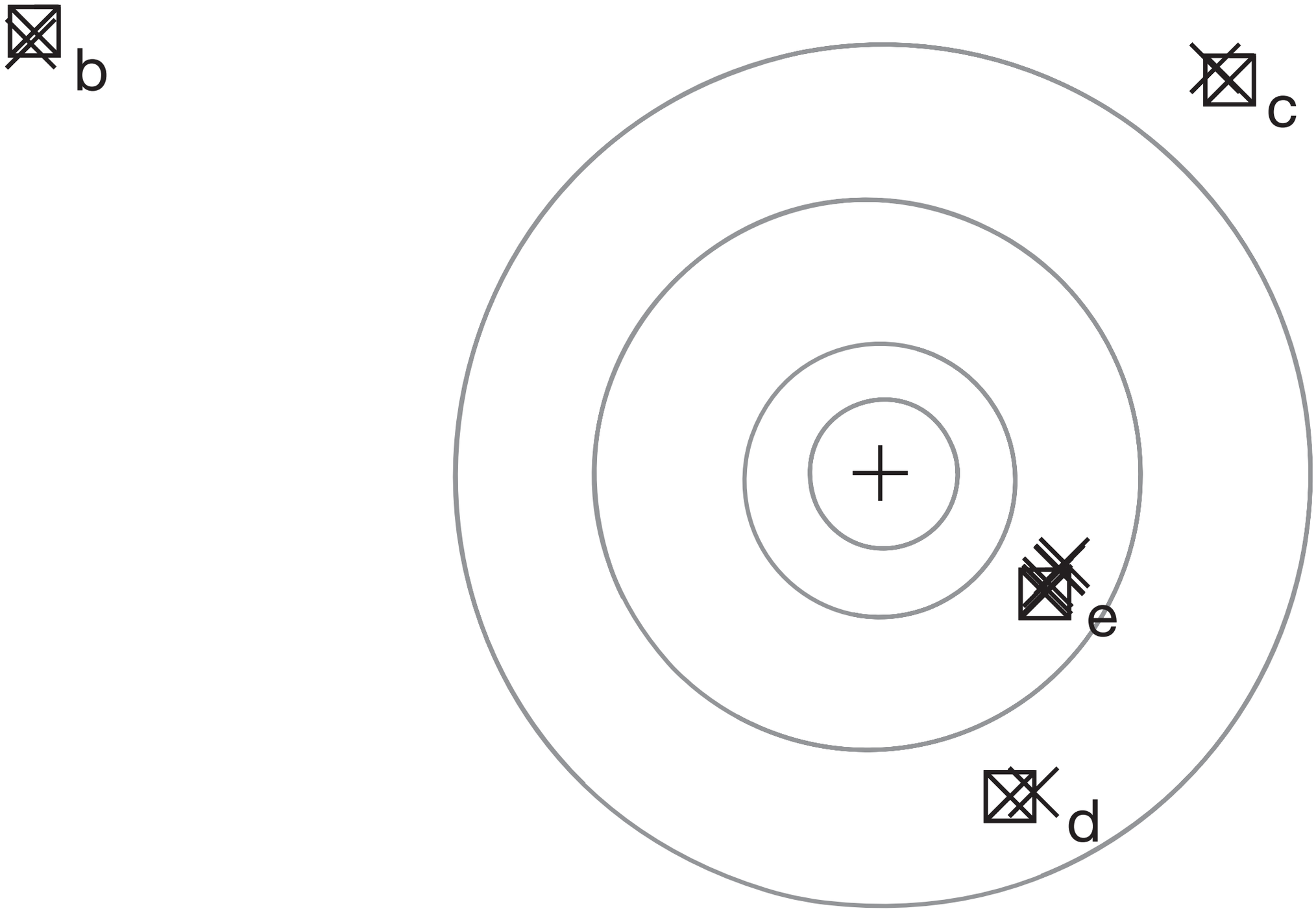
Marois et al. (2010)



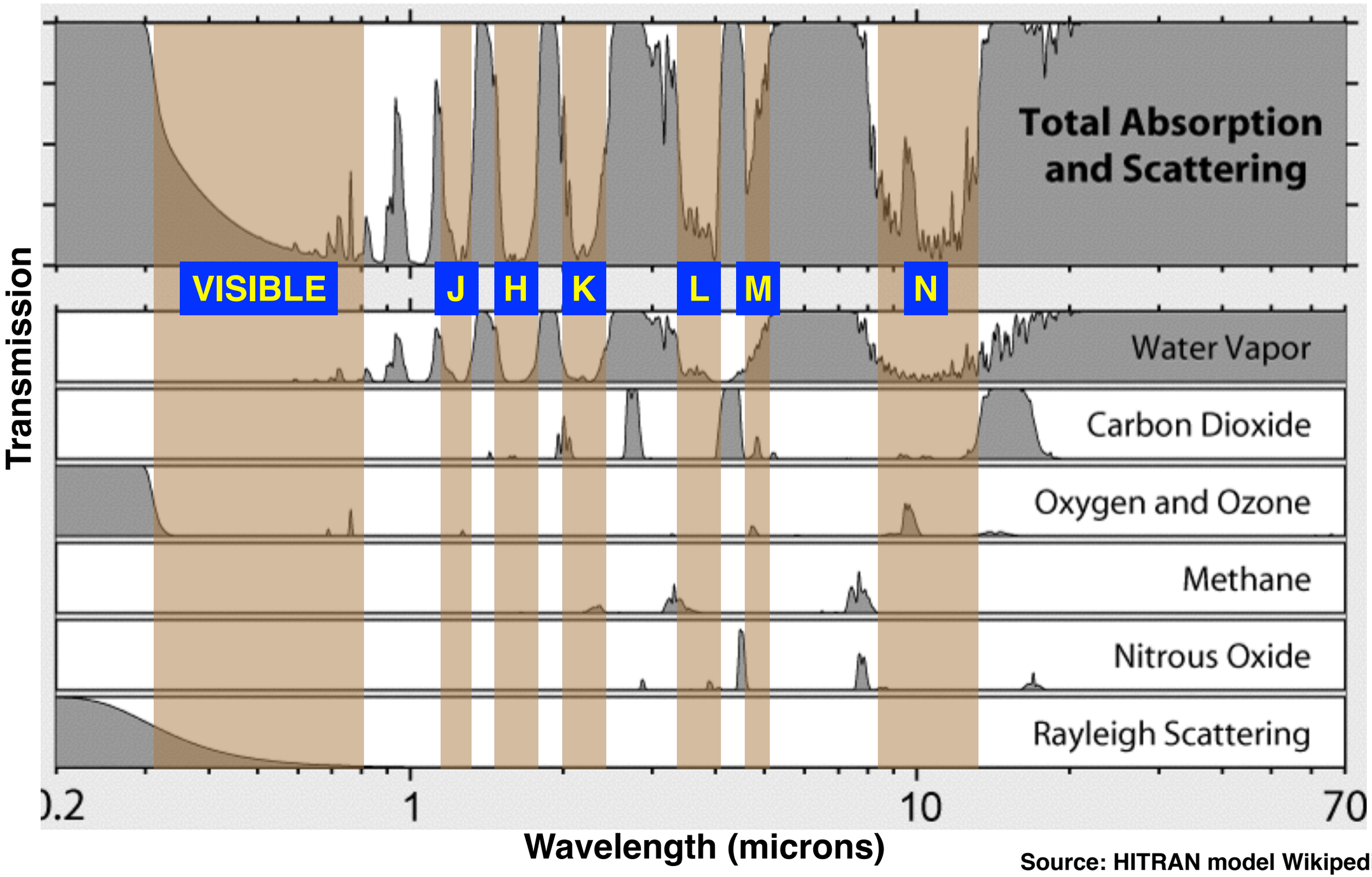
HR 8799 system biggest success

Marois (2010) Nature

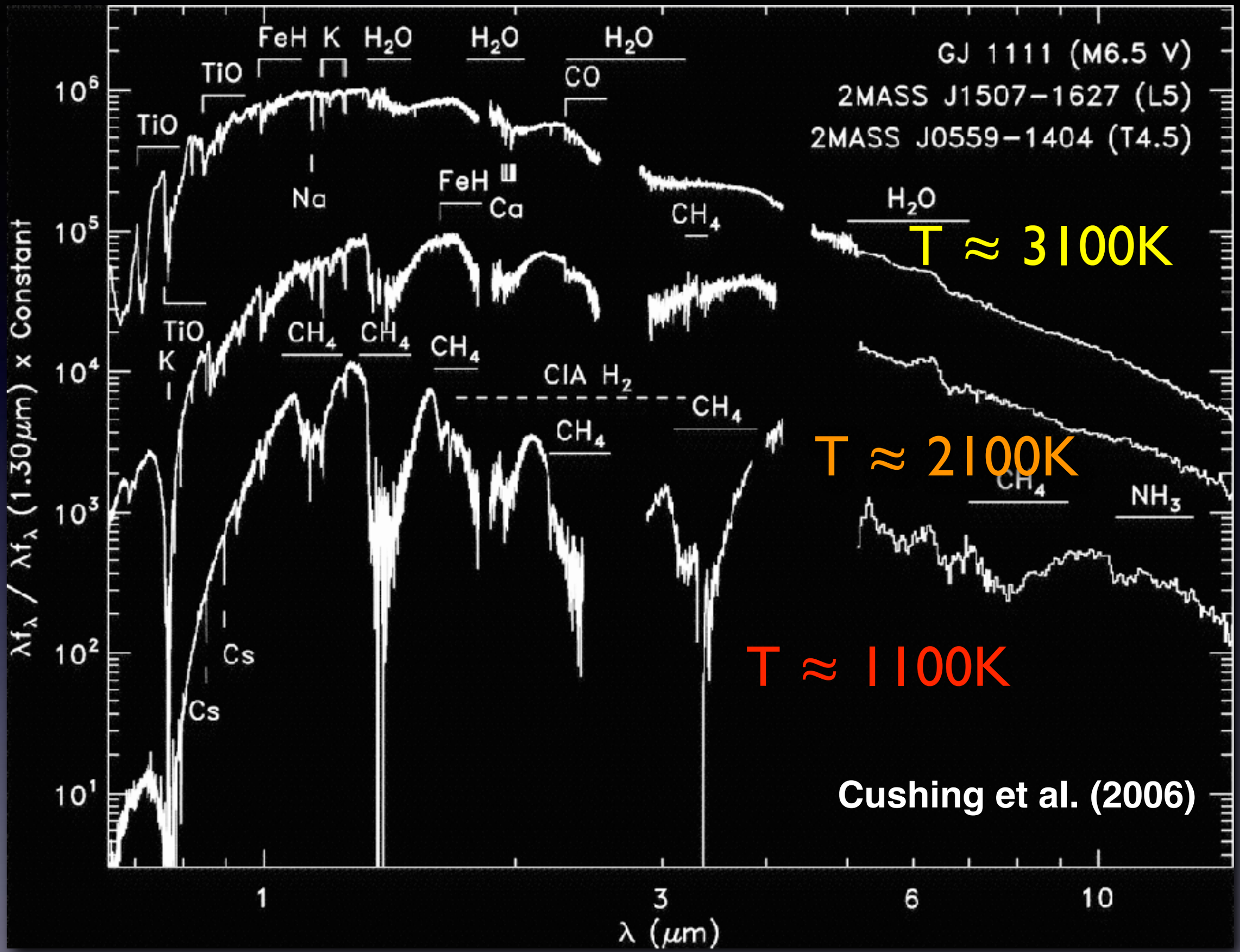
Orbital Motion seen over several years



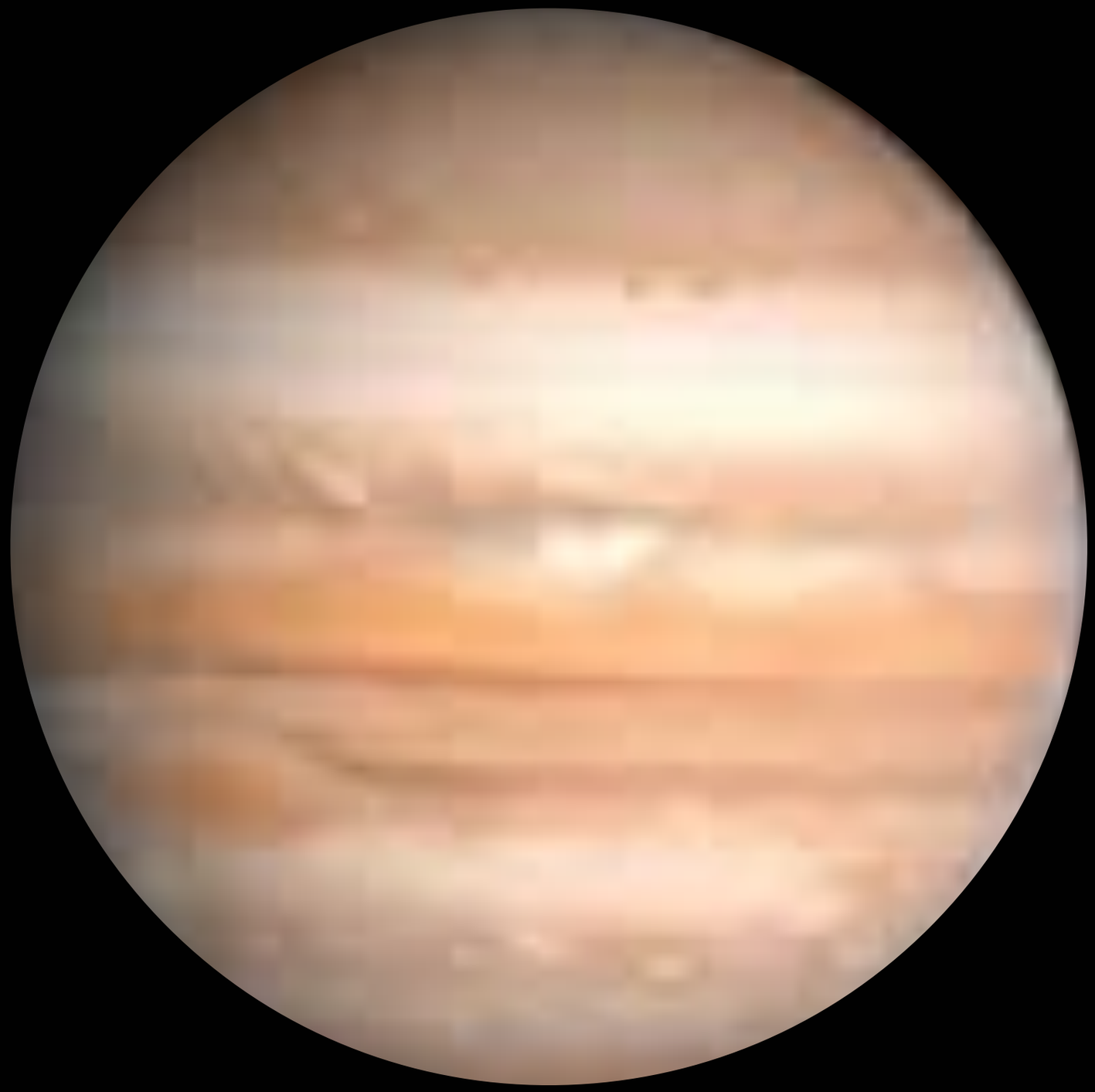
Atmospheric Transmission



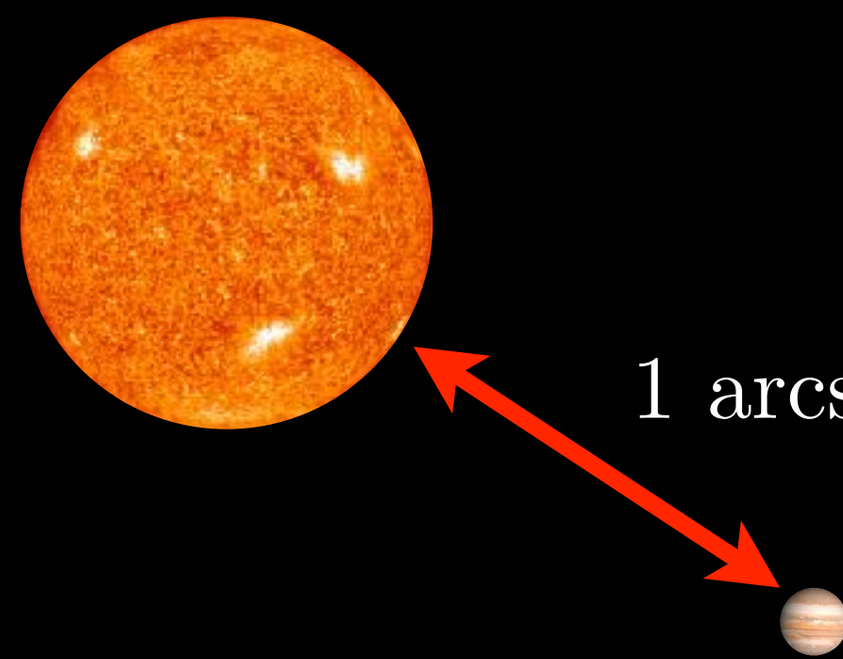
Source: HITRAN model Wikipedia


GJ 1111 (M6.5 V)
2MASS J1507−1627 (L5)
2MASS J0559−1404 (T4.5)
T ≈ 3100K
T ≈ 2100K
T ≈ 1100K
Cushing et al. (2006)
FeH
K
H2O
H2O
H2O
TiO
TiO
CO
Na
FeH
Ca
CH4
H2O
TiO
K
CH4
CH4
CH4
CIA H2
CH4
CH4
CH4
NH3
Cs
Cs
λfλ / λfλ (1.30μm) x Constant
λ (μm)
1
3
6
10

We’d like to see...

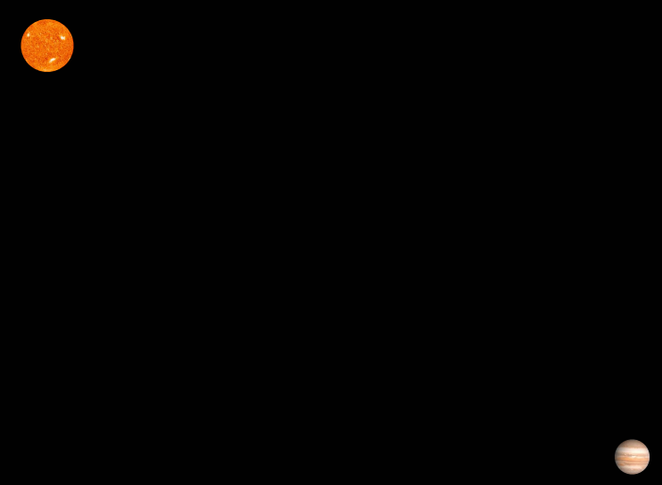


10^9 to 10^6 times brighter



1 arcsec or less

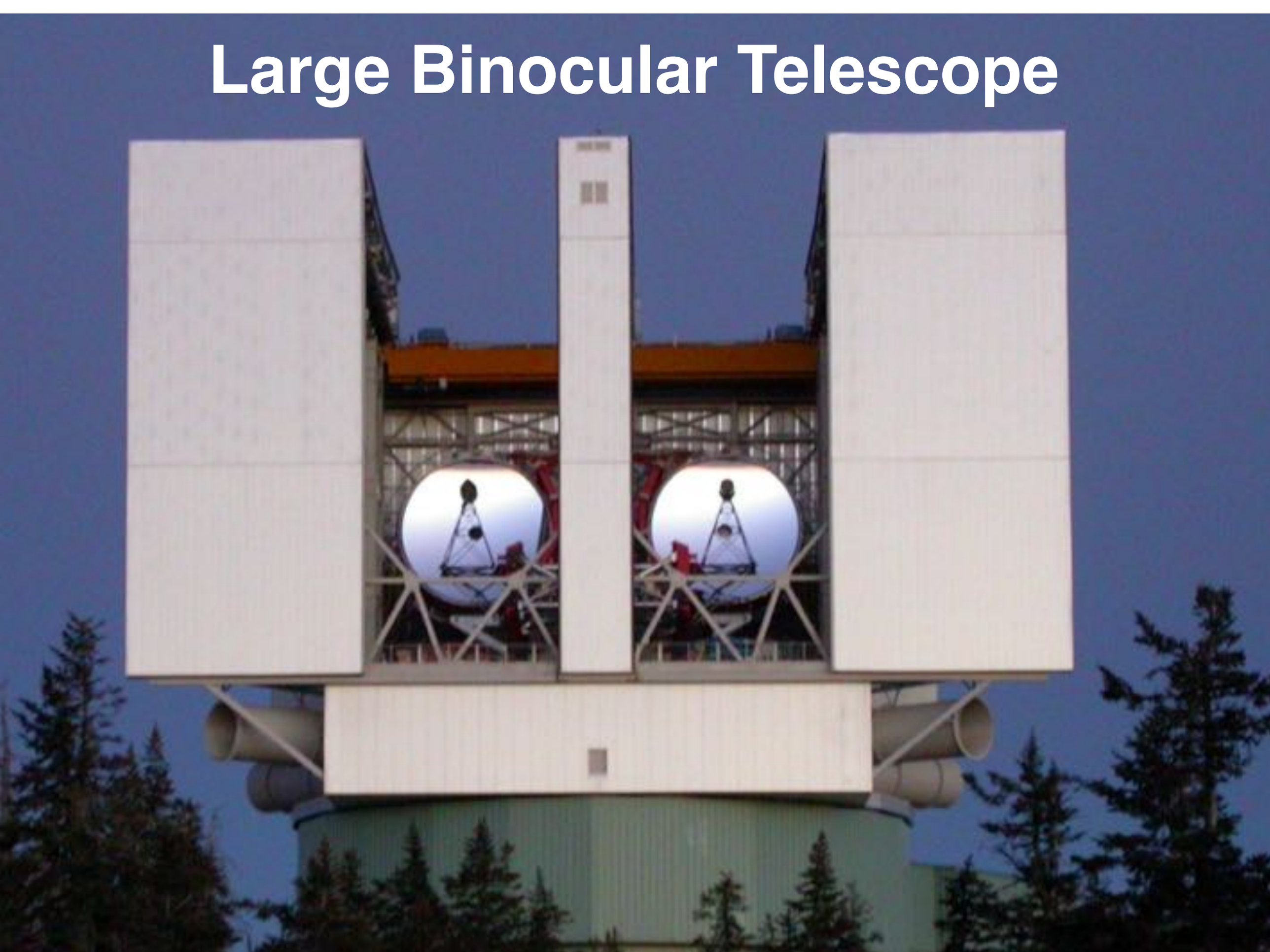
both are unresolved sources (maybe not the star though...)



Telescopes - VLT in Chile

Large Binocular Telescope

Large Binocular Telescope



The Lingo

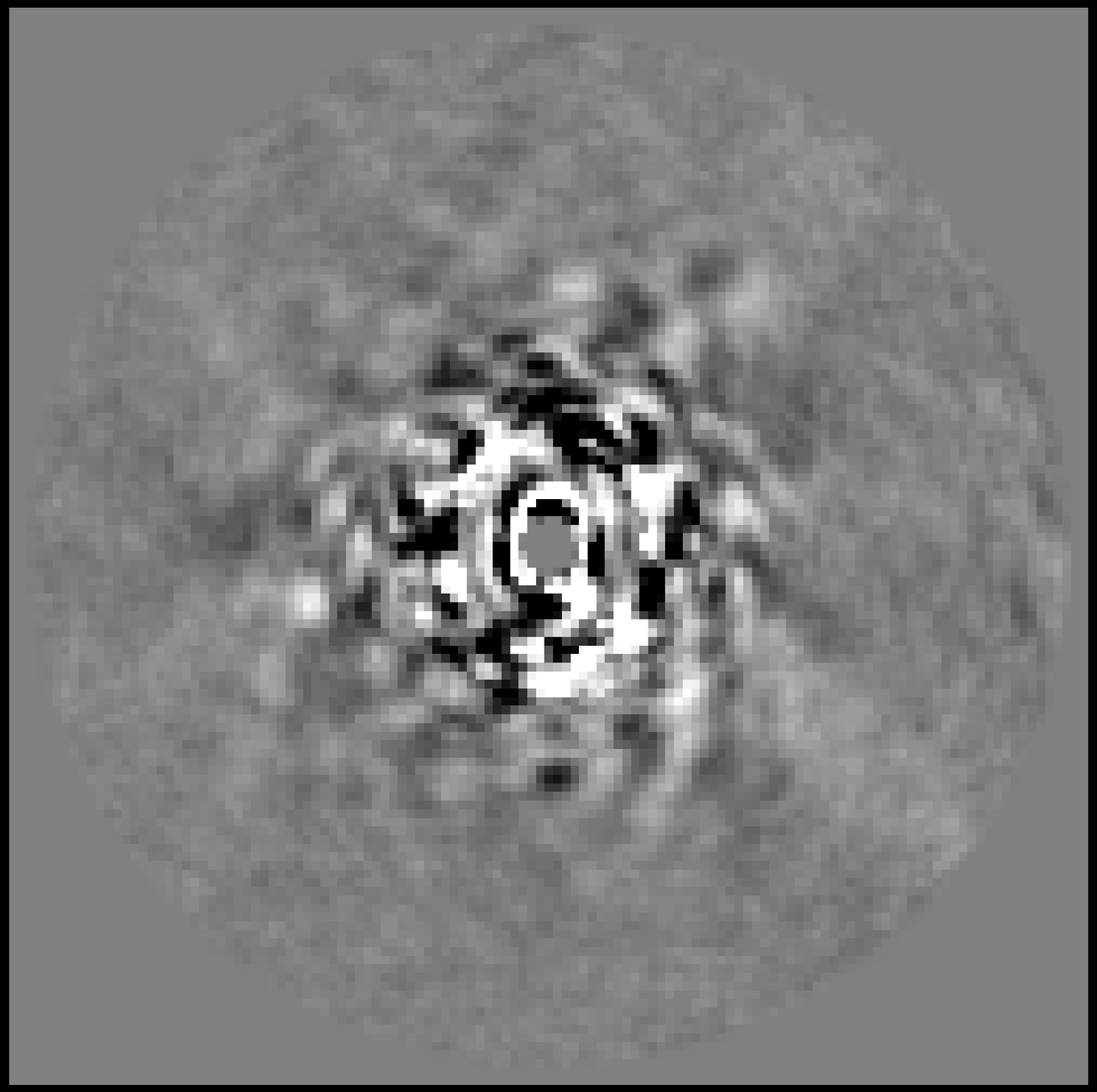
Inner Working Angle (IWA) and Outer Working Angle (OWA):
Specify in units of lambda/D the range of angles that the coronagraph effectively works with >50% planet transmission

Contrast (specified in delta magnitudes or number of decades):
this is the RAW contrast as seen in the PSF.
Space based coronagraphs aim for 10 decades, ground based fo 5 to 6 decades.

Null order (specified as 2nd, 3rd, 4th, 5th….):
expresses how sensitive the coronagraph is to tip tilt error with the star
Higher orders are more immune to tip tilt, but have larger IWAs

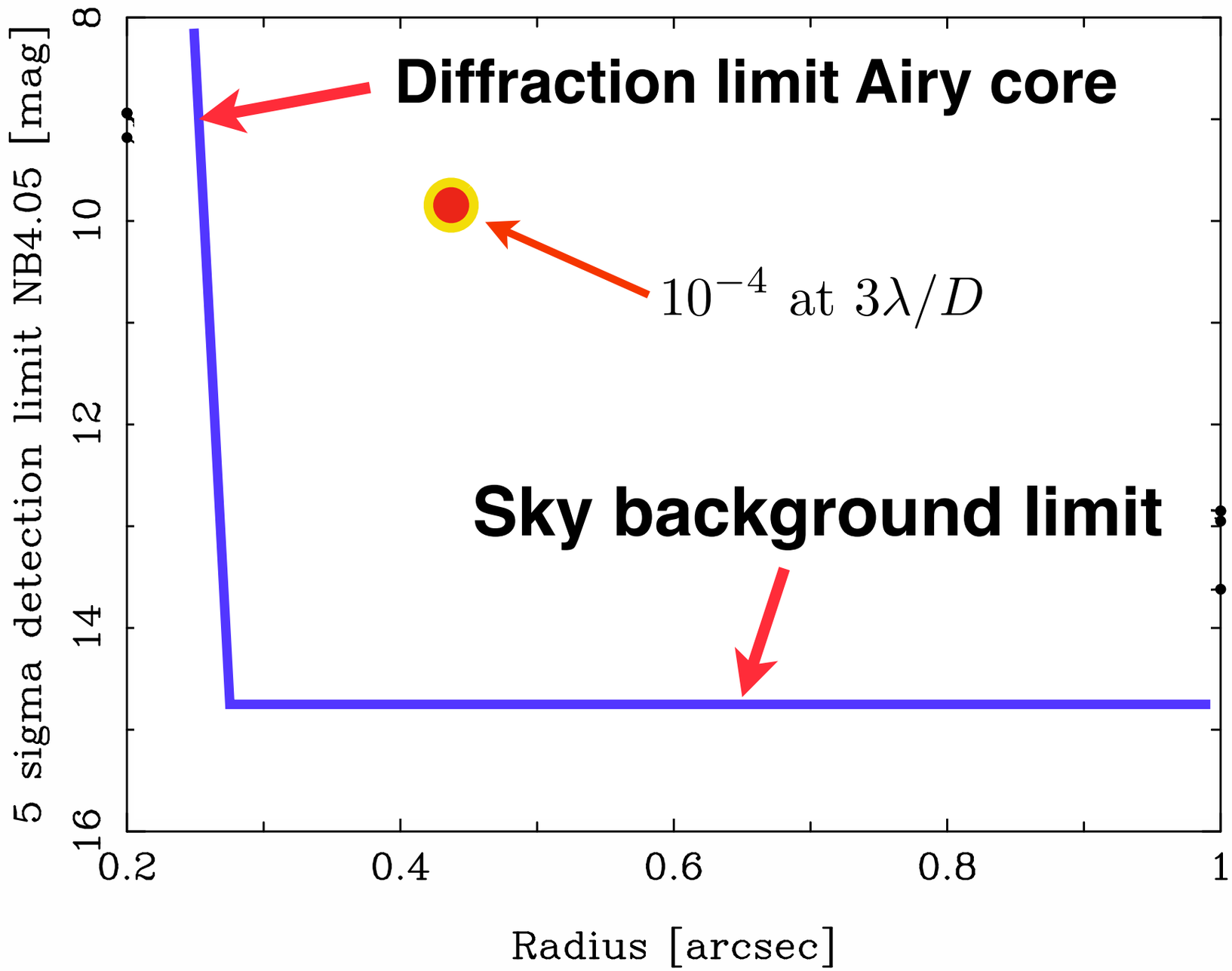
(adapted from Olivier Guyon's slides)

Subtracting off a reference image leaves “speckles”



the telescope and and camera “flex”

An ideal contrast curve



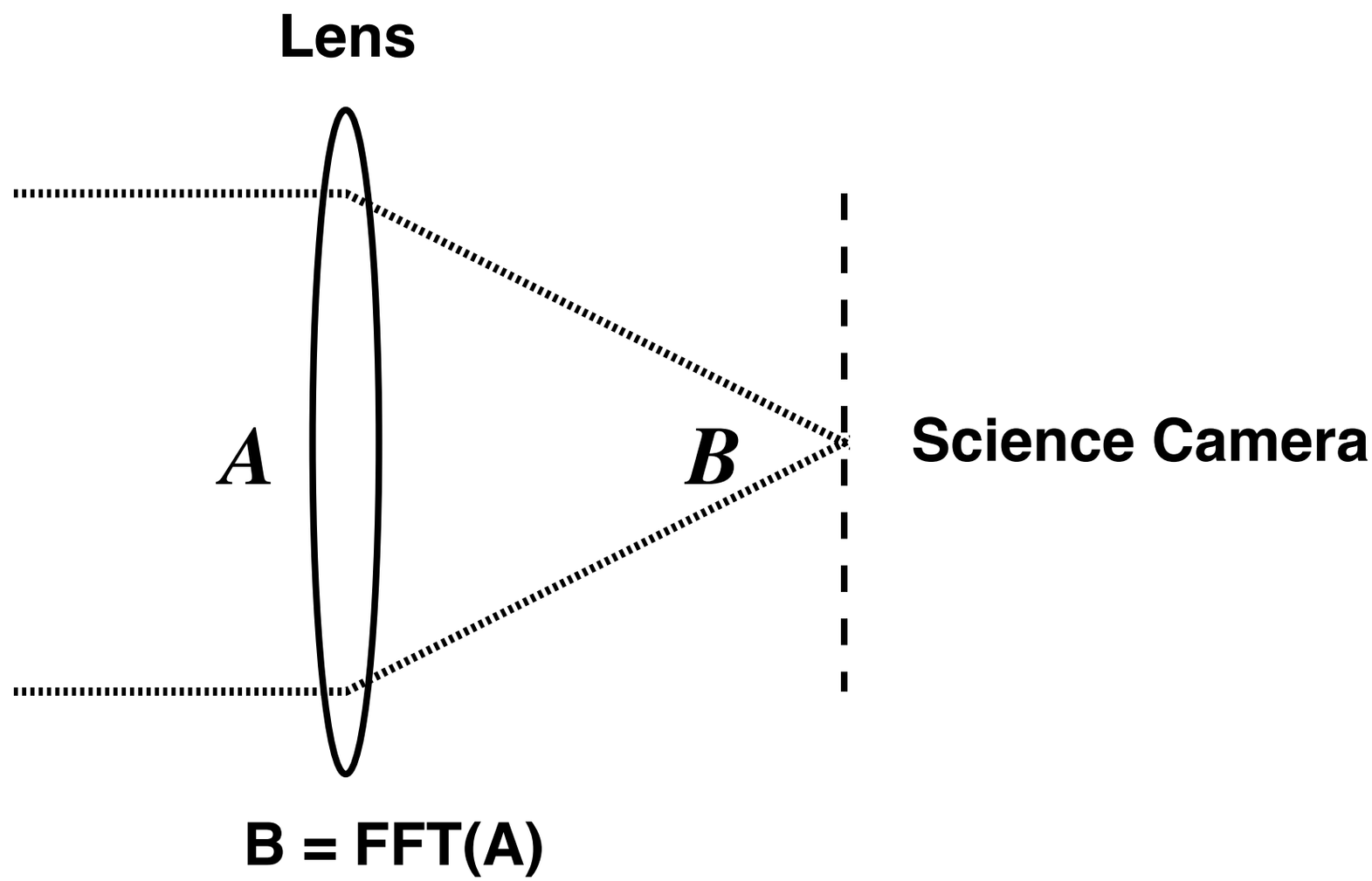
Coronagraphs are angular filters

They apodize the telescope PSF

(“apodization” is Greek for ‘chopping off the foot’)

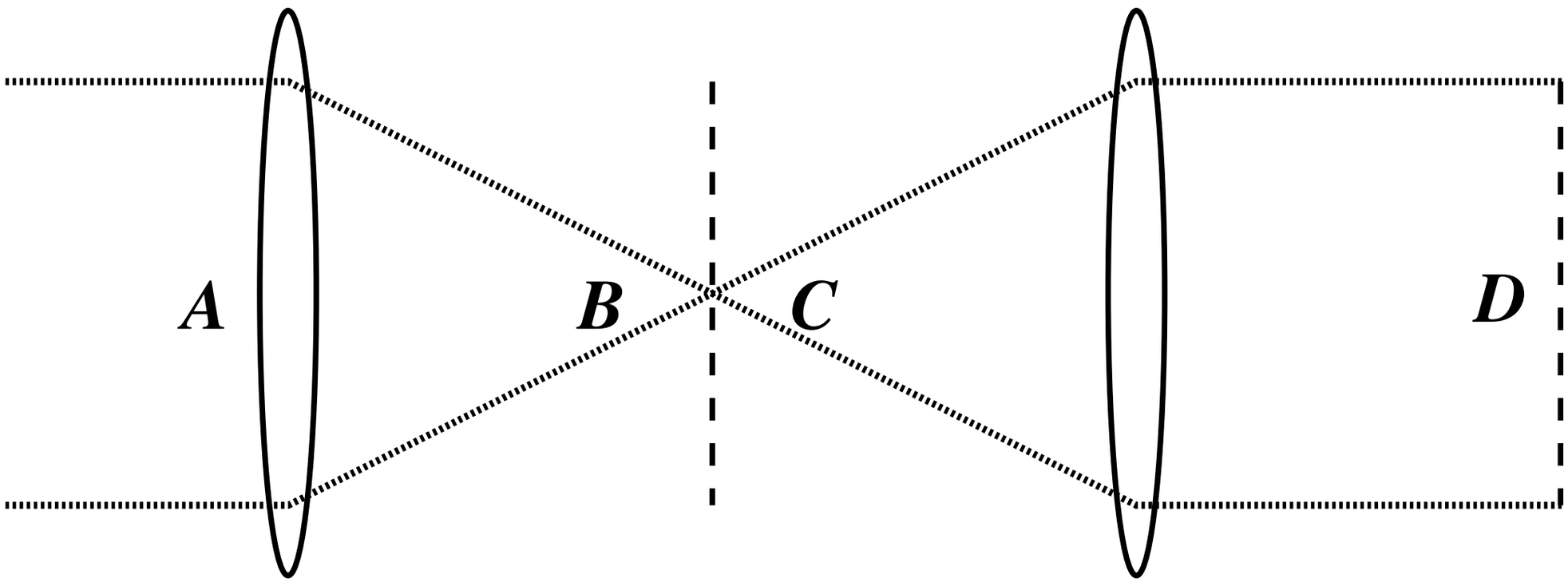
Lenses are Fourier Transform machines

Wavefront angles are converted to linear positions



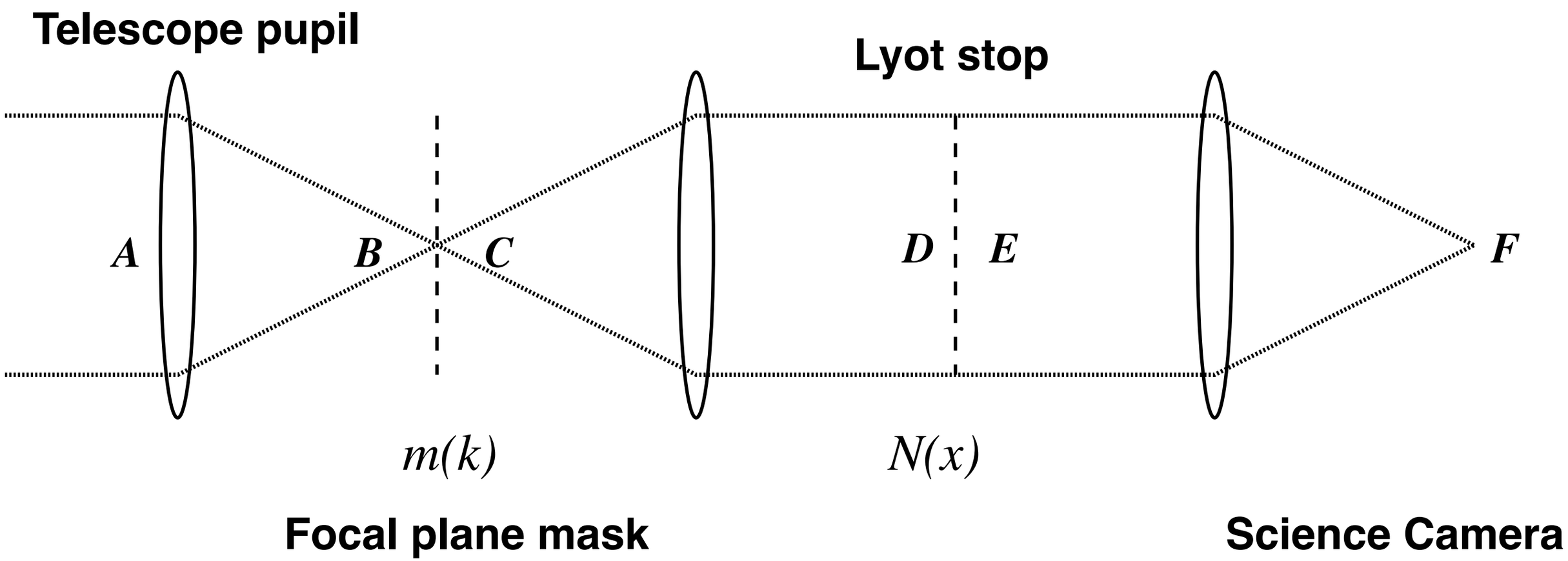
Detector signal $\propto$ Energy $\propto B^2$

…and you go from Pupil Plane to Image Plane and back again

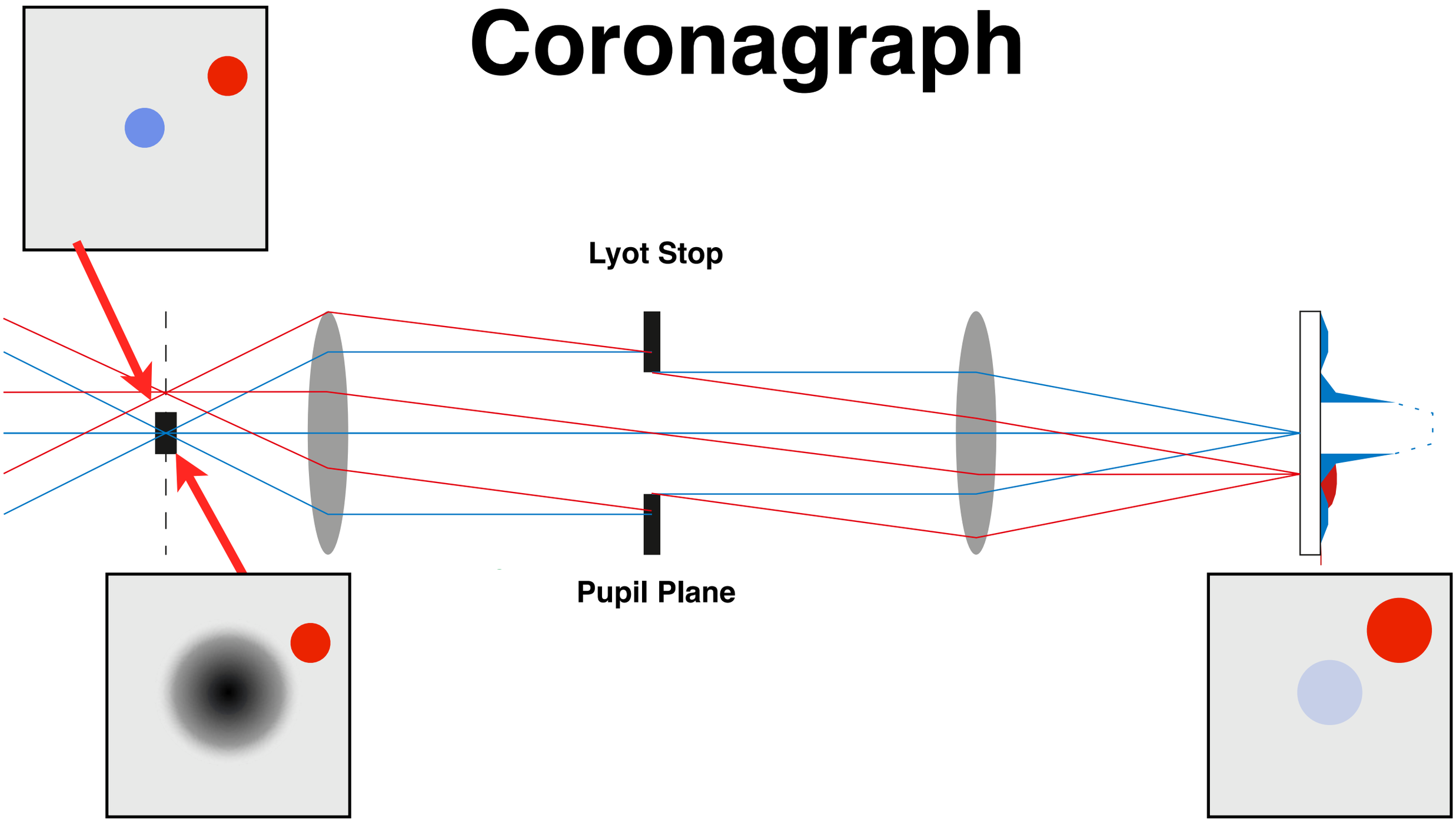


Pupil Plane => FFT => Focal Plane => I FFT => Pupil Plane

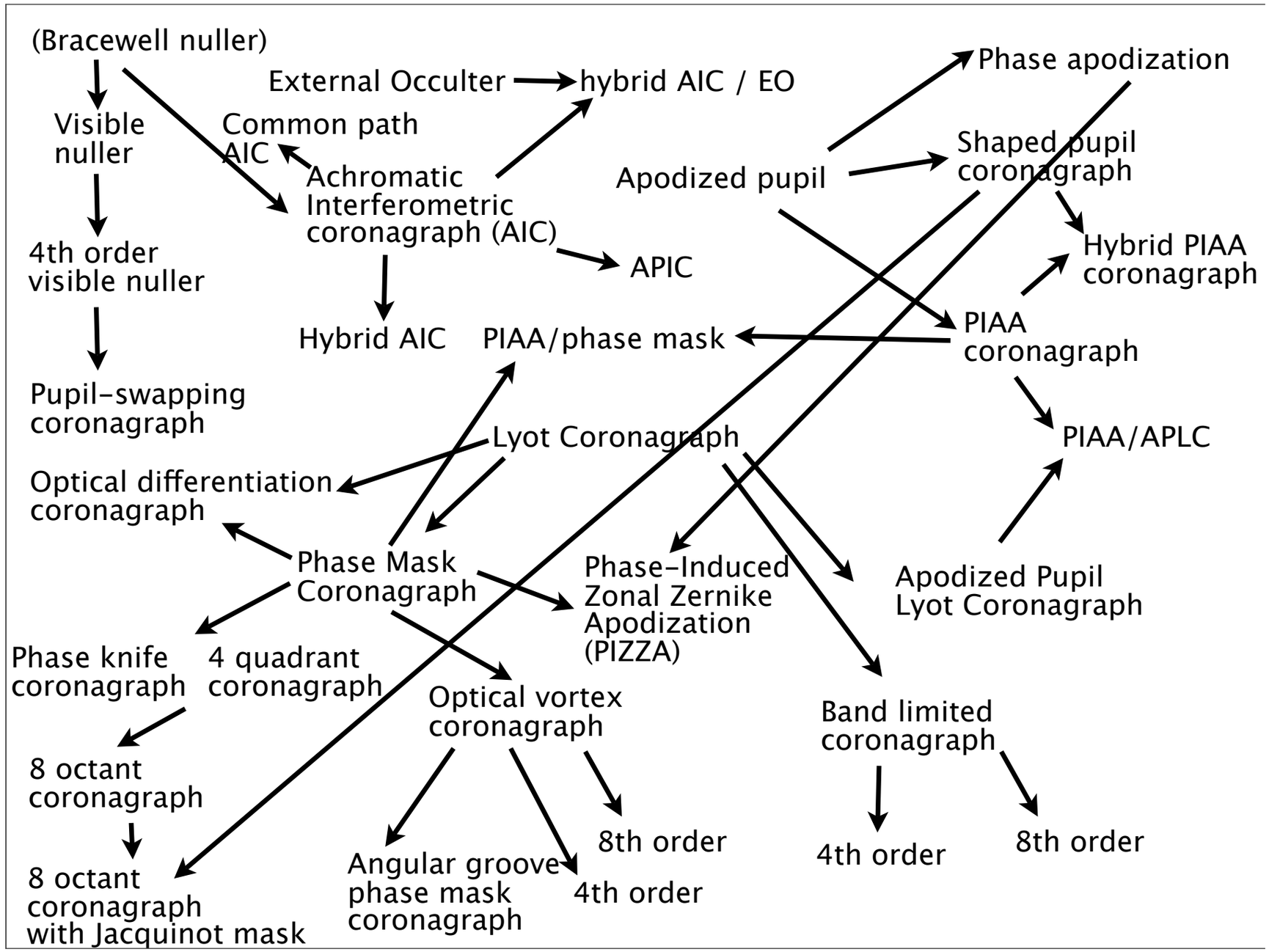
Layout of a basic coronagraph



Classical/Apodized Lyot Coronagraph

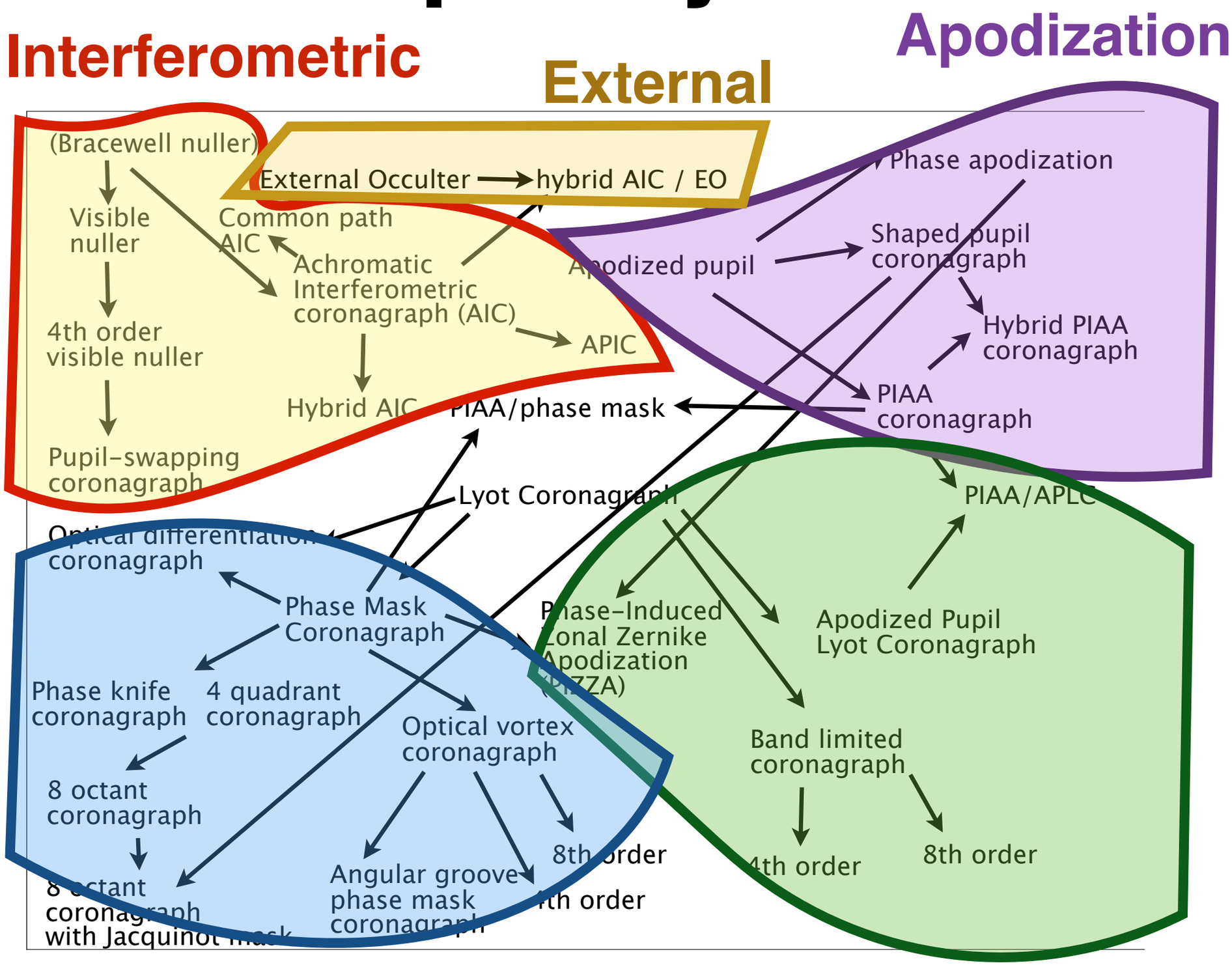


By 2007, many types of coronagraph developed



(adapted from Olivier Guyon's slides)

Can be split by method



Phase Lyot

Amplitude Lyot

Phase Lyot - 4 Quadrant Phase Mask (4QPM)

Phase shift

2nd order null

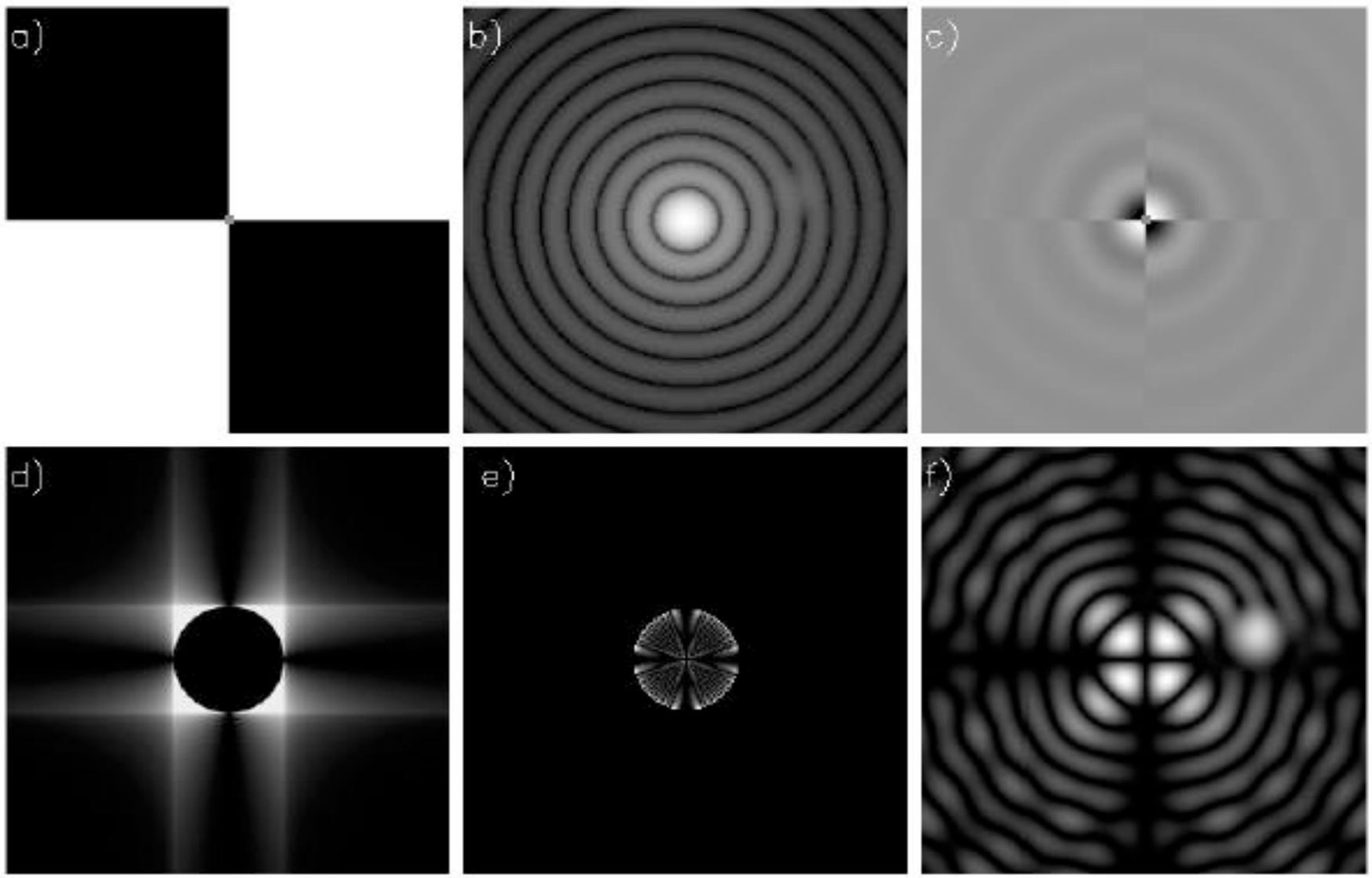


FIG. 2.—Numerical simulation illustrating the principle of the four-quadrant coronagraph. A companion 15 mag fainter (flux ratio of 10^6) is locate
λ/D away from the star. The individual images show (*a*) the shape of the phase mask (white for 0 phase shift, black for π phase shift), (*b*) the Airy patten
splayed in intensity, (*c*) the complex amplitude of the star phase shifted by the mask, (*d*) the exit pupil, (*e*) the exit pupil through the Lyot stop (95% of th
pil diameter), and (*f*) the coronagraphic image where the companion is clearly visible. Images are displayed with nonlinear scale.

Amplitude Lyot - Band Limited Mask Lyot (BL4, BL8)

A focal plane mask that moves star light into thin crescents at edge of pupil

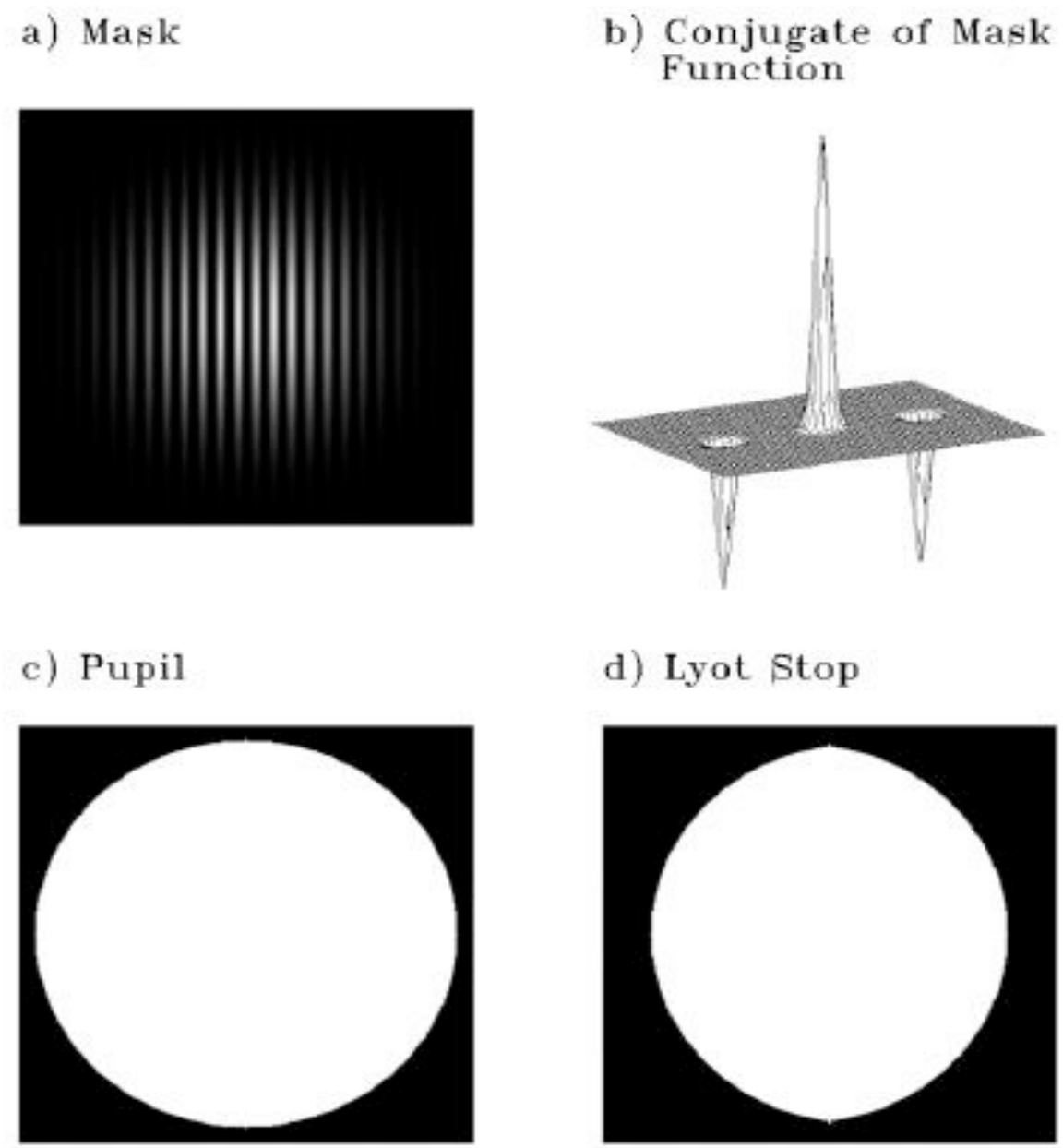
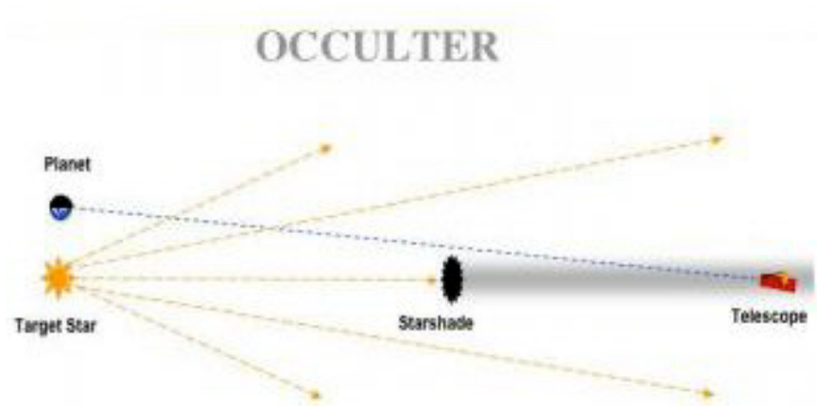


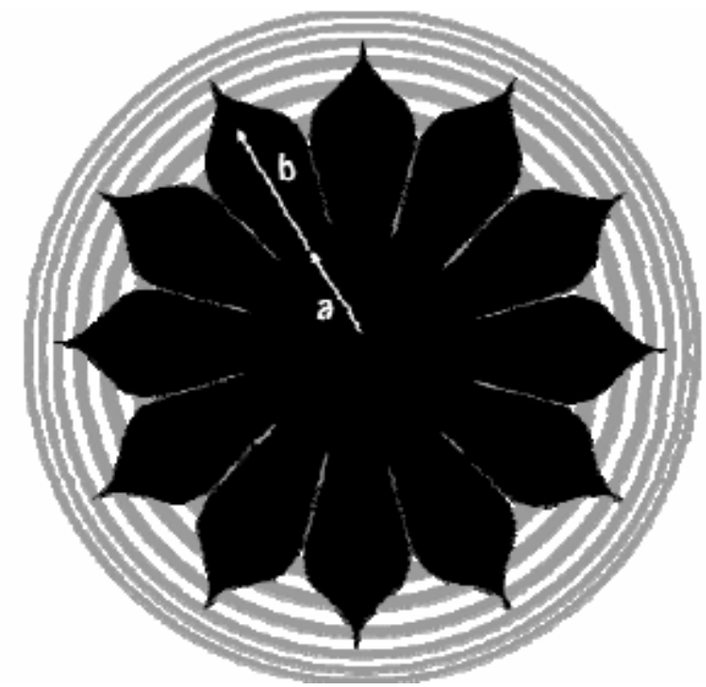
FIG. 4.—Simplest band-limited mask, analogous to a single-baseline nulling interferometer. (*a*) Mask ITF $\sin^4(x)$ multiplied by a slow taper. Dark areas are opaque. (*b*) Conjugate of the mask ATF (eq. [13]). This occulting mask can be used with any aperture shape, but for the circular aperture shown in (*c*), the corresponding Lyot stop is (*d*).

Kuchner and Traub 2002
Kuchner 2005

External Occulter - Flying Sunshades



A properly placed and shaped occulter can drop a deep shadow of starlight over a telescope while allowing planet light to pass unimpeded.



Cash et al. 2005 SPIE 5899 274
Cash 2006, Nature

A paper by Olivier Guyon in 2006 changed the development of coronagraphs…..

Guyon et al. (2006) ApJSS 167 81

The Astrophysical Journal Supplement Series, 167:81–99, 2006 November

THEORETICAL LIMITS ON EXTRASOLAR TERRESTRIAL PLANET DETECTION WITH CORONAGRAPHS

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Received 2006 May 25; accepted 2006 July 7

ABSTRACT

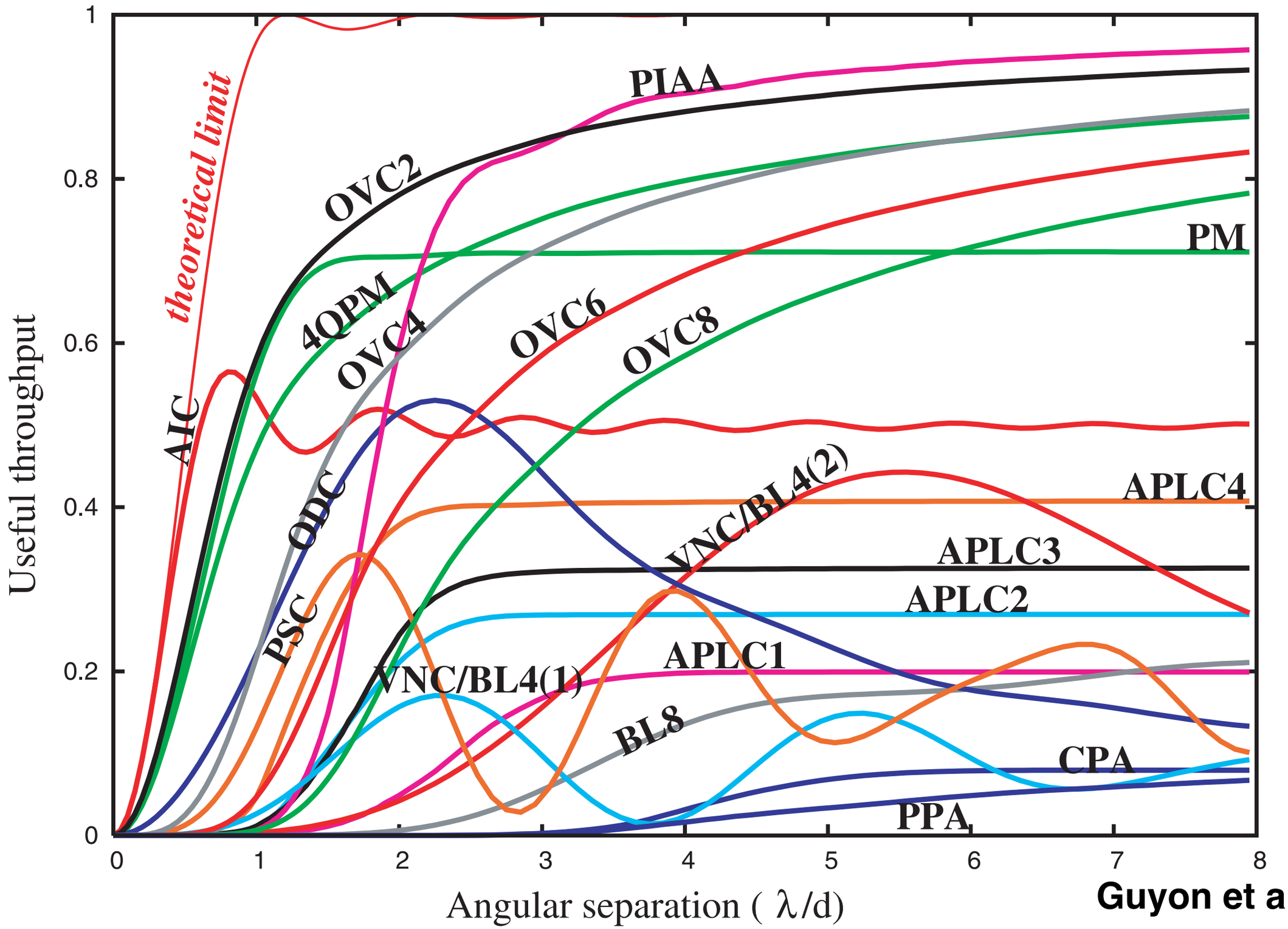
Many high-contrast coronagraph designs have recently been proposed. In this paper, their suitability for direct imaging of extrasolar terrestrial planets is reviewed. We also develop a linear algebra based model of coronagraphy that can both explain the behavior of existing coronagraphs and quantify the coronagraphic performance limit imposed by fundamental physics. We find that the maximum theoretical throughput of a coronagraph is equal to 1 minus the nonaberrated noncoronagraphic PSF of the telescope. We describe how a coronagraph reaching this fundamental limit may be designed, and how much improvement over the best existing coronagraph design is still possible. Both the analytical model and numerical simulations of existing designs also show that this theoretical limit rapidly degrades as the source size is increased: the "highest performance" coronagraphs, those with the highest throughput and smallest inner working angle (IWA), are the most sensitive to stellar angular diameter. This unfortunately rules out the possibility of using a small IWA ($<\lambda/d$) coronagraph for a terrestrial planet imaging mission. Finally, a

Small IWA means we are looking closer to the stars
OR
We can use a smaller telescope aperture

Coronagraph	Abbreviation	Reference
	"Interferometric" Coronagraphs	
Achromatic Interferometric Coronagraph	AIC	Baudoz et al. (2000)
Common-Path Achromatic Interferometer-Coronagraph	CPAIC	Tavrov et al. (2005)
Visible Nulling Coronagraph, X-Y shear (fourth-order null)[a]	VNC	Mennesson et al. (2003)
Pupil Swapping Coronagraph	PSC	Guyon & Shao (2006)
	Pupil Apodization	
Conventional Pupil Apodization and Shaped-Pupil[b]	CPA	Kasdin et al. (2003)
Achromatic Pupil Phase Apodization	PPA	Yang & Kostinski (2004)
Phase Induced Amplitude Apodization Coronagraph	PIAAC	Guyon (2003)
Phase Induced Zonal Zernike Apodization	PIZZA	Martinache (2004)
	Improvement on the Lyot Concept with Amplitude Masks	
Apodized Pupil Lyot Coronagraph	APLC	Soummer et al. (2003a, 2003b)
Apodized Pupil Lyot Coronagraph, *N* steps	APLC*N*	Aime & Soummer (2004)
Band-limited, fourth-order[a]	BL4	Kuchner & Traub (2002)
Band-limited, eighth-order	BL8	Kuchner et al. (2005)
	Improvement on the Lyot Concept with Phase Masks	
Phase Mask	PM	Roddier & Roddier (1997)
4 Quadrant Phase Mask	4QPM	Rouan et al. (2000)
Achromatic Phase Knife Coronagraph	APKC	Abe et al. (2001)
Optical Vortex Coronagraph, topological charge *m*	OVC*m*	Palacios (2005)
Angular Groove Phase Mask Coronagraph	AGPMC	Mawet et al. (2005)
Optical Differentiation	ODC	Oti et al. (2005)

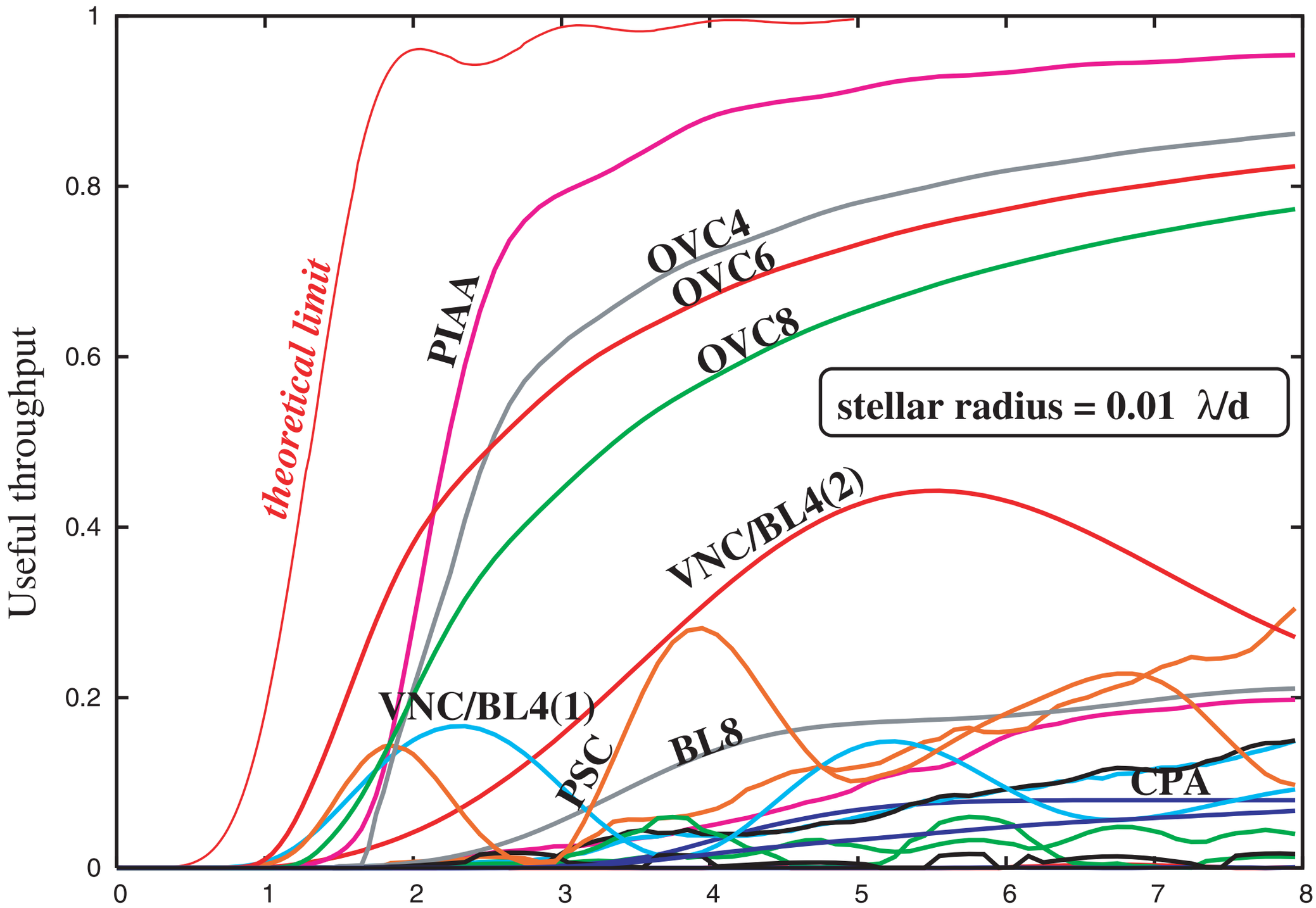
Guyon et al. (2006)

Guyon developed the idea of a 'theoretical limit' coronagraph



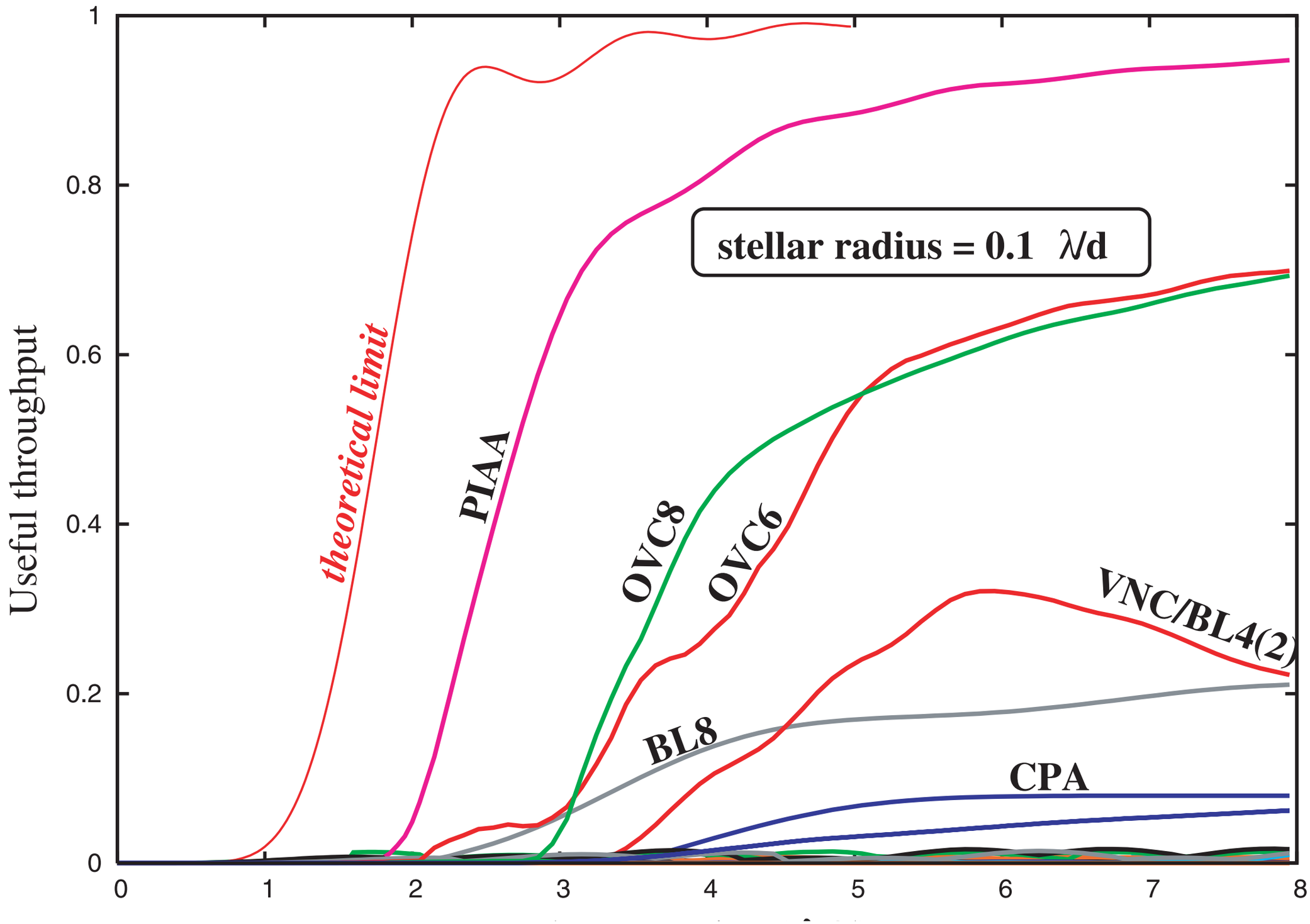
Guyon et al. (2006)

…but nearby stars are not point sources



Guyon et al. (2006)

…and many lose their effectiveness rapidly



Guyon et al. (2006)

We now focus on a much smaller family which can give high contrast at IWA of less than 5 diffraction widths

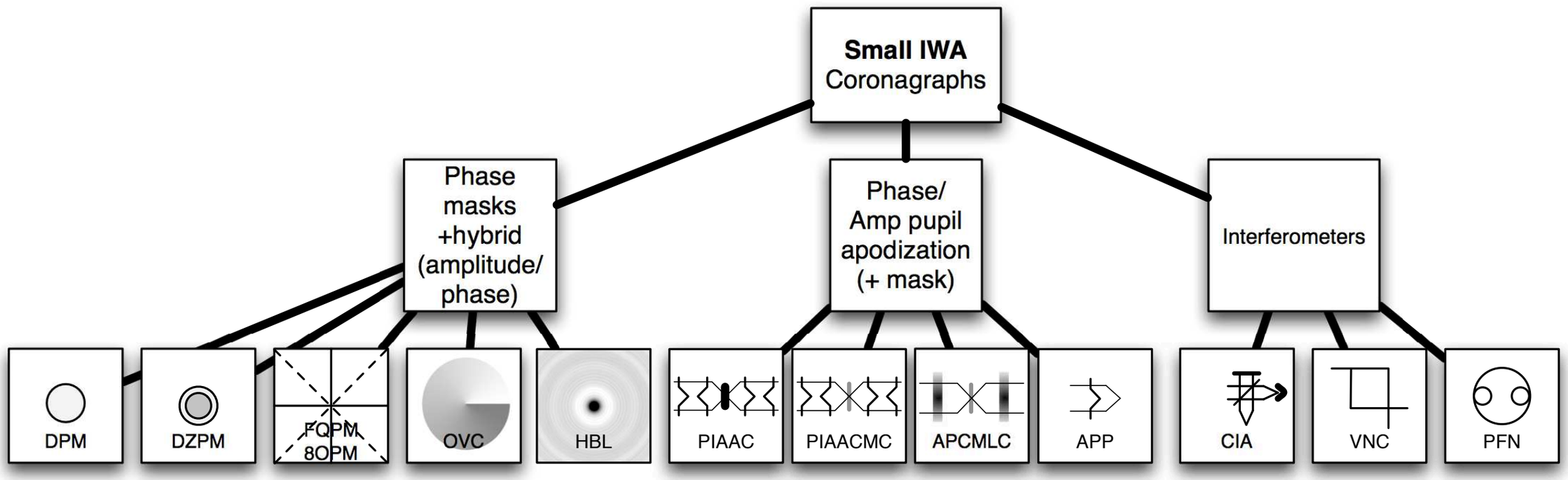
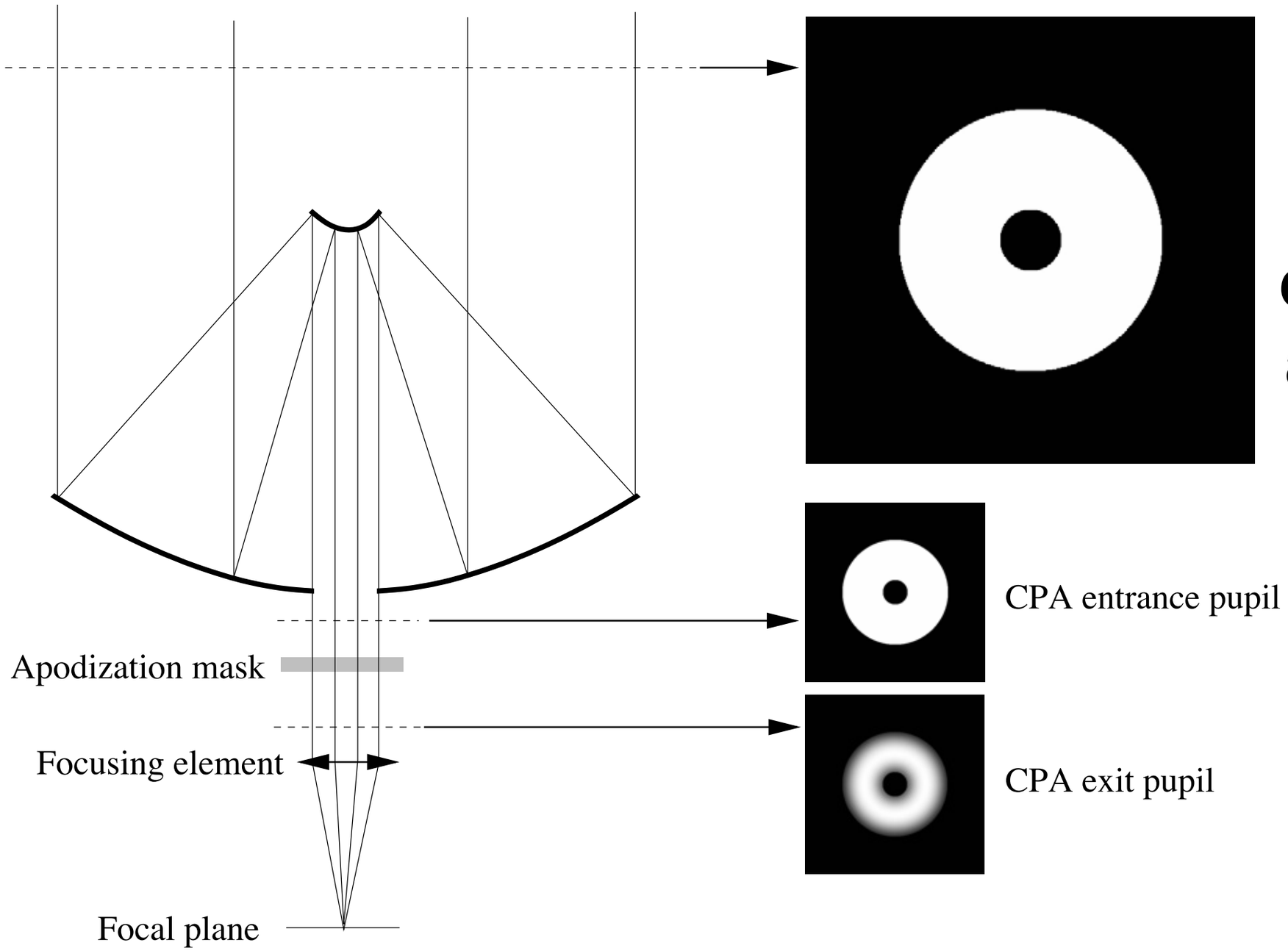


Figure 4. The family tree of small-angle coronagraphs (representative cases included). DPM: disk phase mask. DZPM: dual zone phase mask. FQPM/8OPM: four-quadrant phase mask, 8 octant phase mask. OVC: optical vortex coronagraph. HBL: hybrid band-limited. PIAAC: phase induced amplitude apodization. APP: apodizing phase plate. CIA: "coronagraphe interferentiel achromatique". VNC: visible nuller coronagraph. PFN: Palomar fiber nuller. Common to all these concepts is some sort of phase manipulation, either in the focal plane or in the pupil plane, or both. Three main families can be pointed out: phase masks, phase/amplitude pupil apodization + focal plane masks (phase and/or amplitude), and interferometers.

Mawet et al. (2012) SPIE Review paper

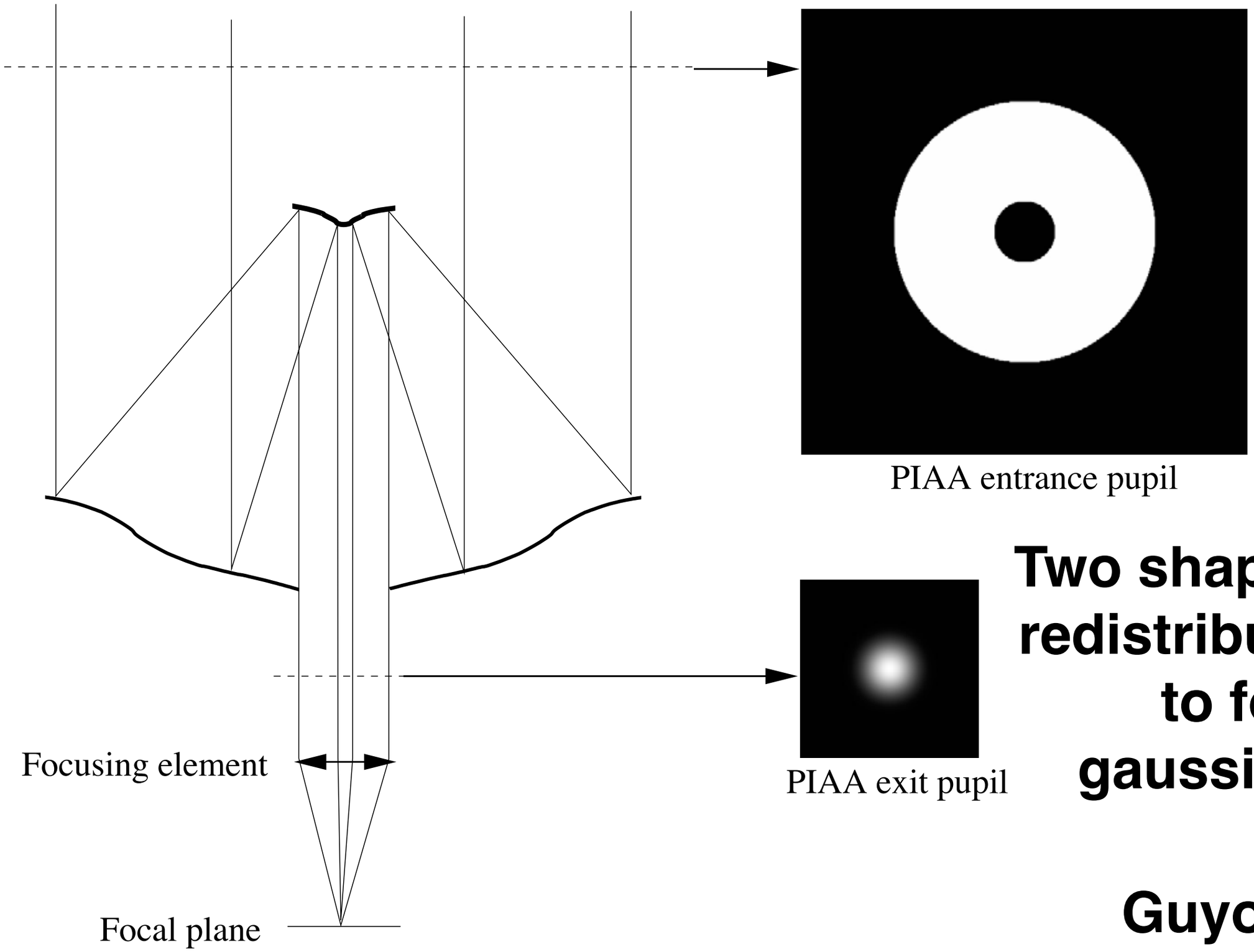
Classical Pupil Apodization



Apodization is done with an optic and lens to form a focused image

Guyon 2003

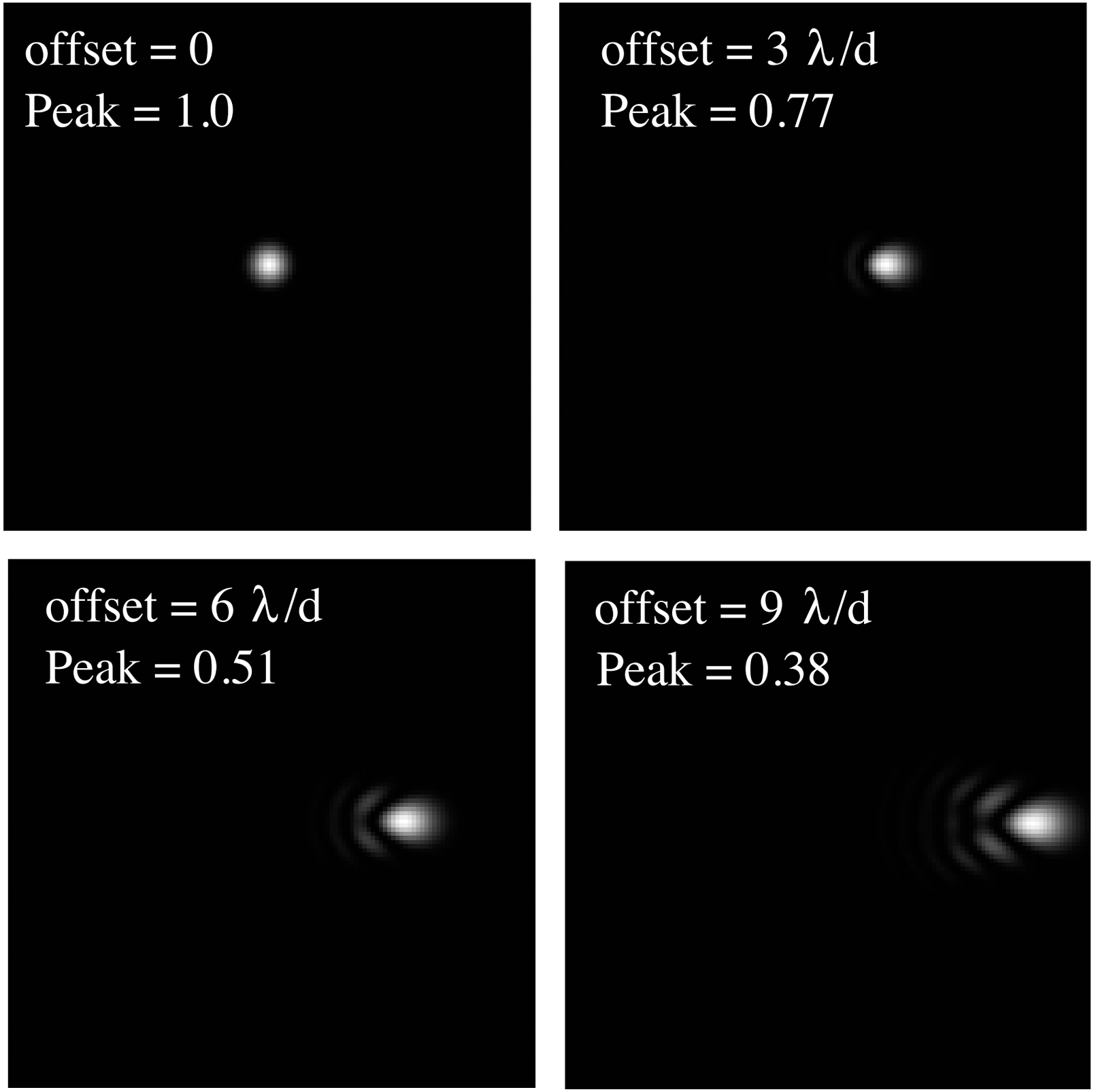
Phase Induced Amplitude Apodization



Two shaped mirrors redistribute the flux to form a gaussian beam

Guyon 2003

Phase Induced Amplitude Apodization



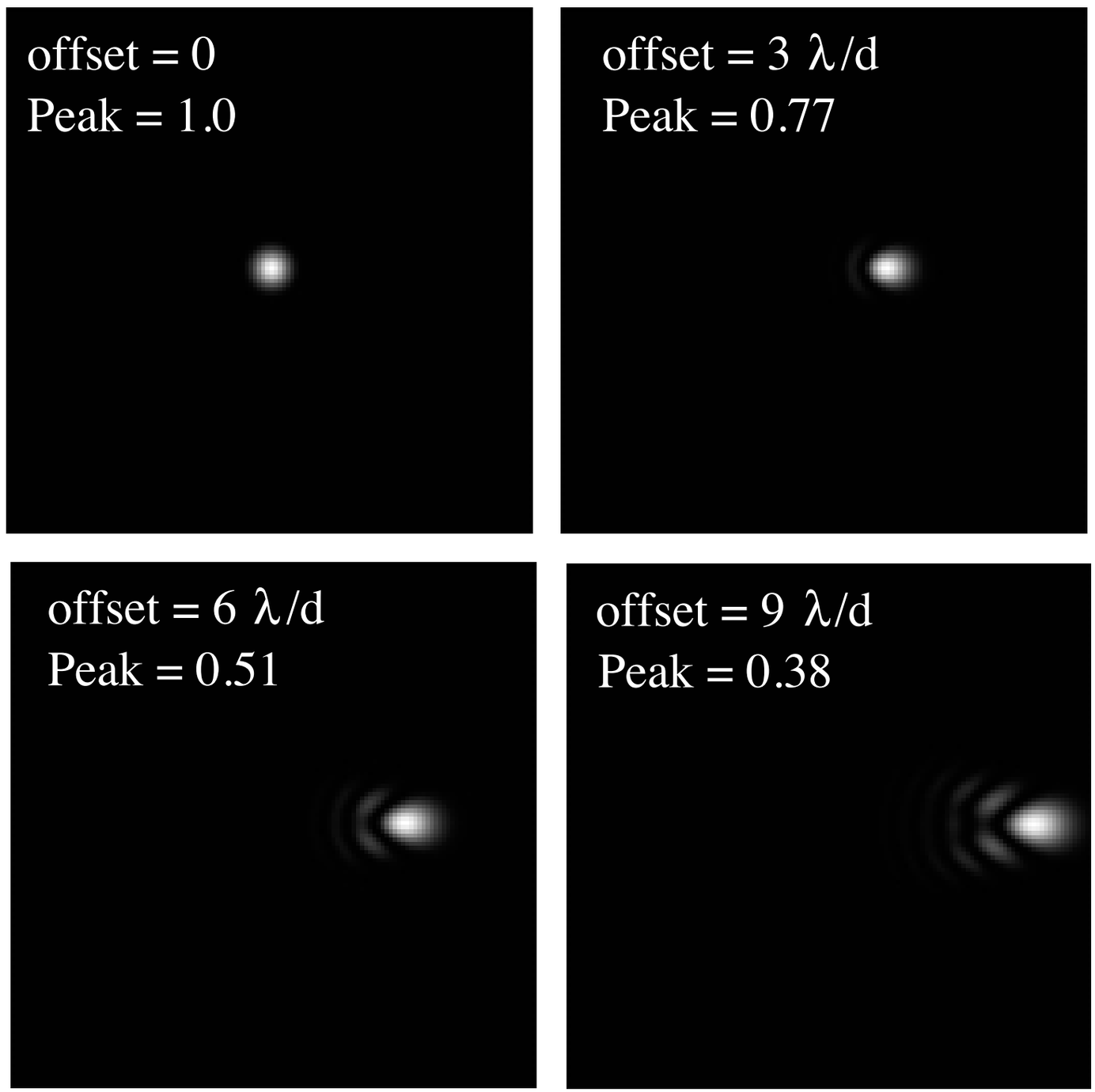
On-axis PSF is GAUSSIAN

Off-axis is very aberrated

Guyon 2003

Phase Induced Amplitude Apodization

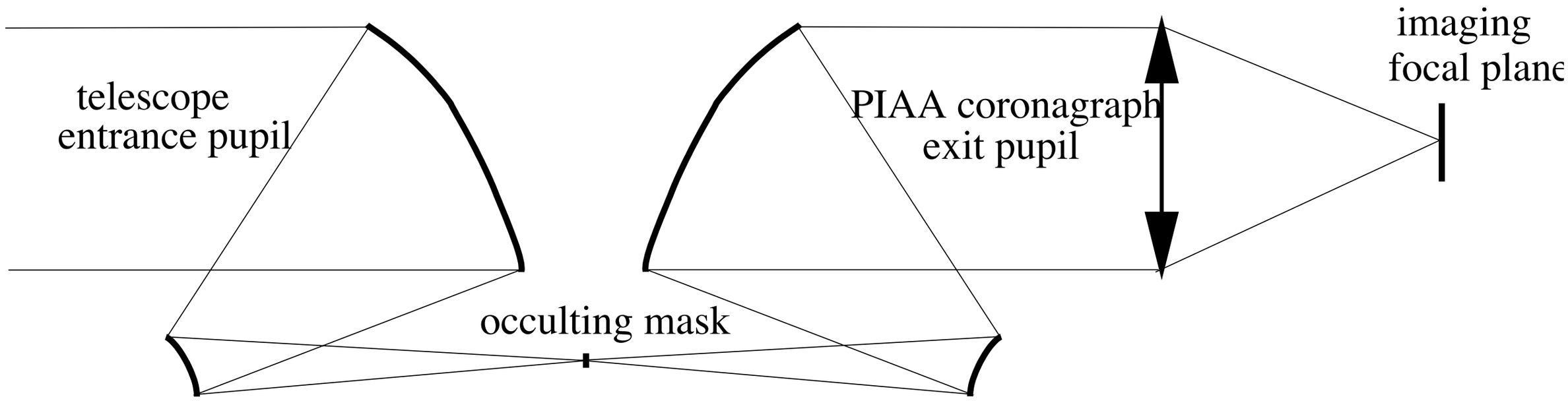
Mask off the central PSF and then an inverse PIAA recombines the planet images



Guyon 2003

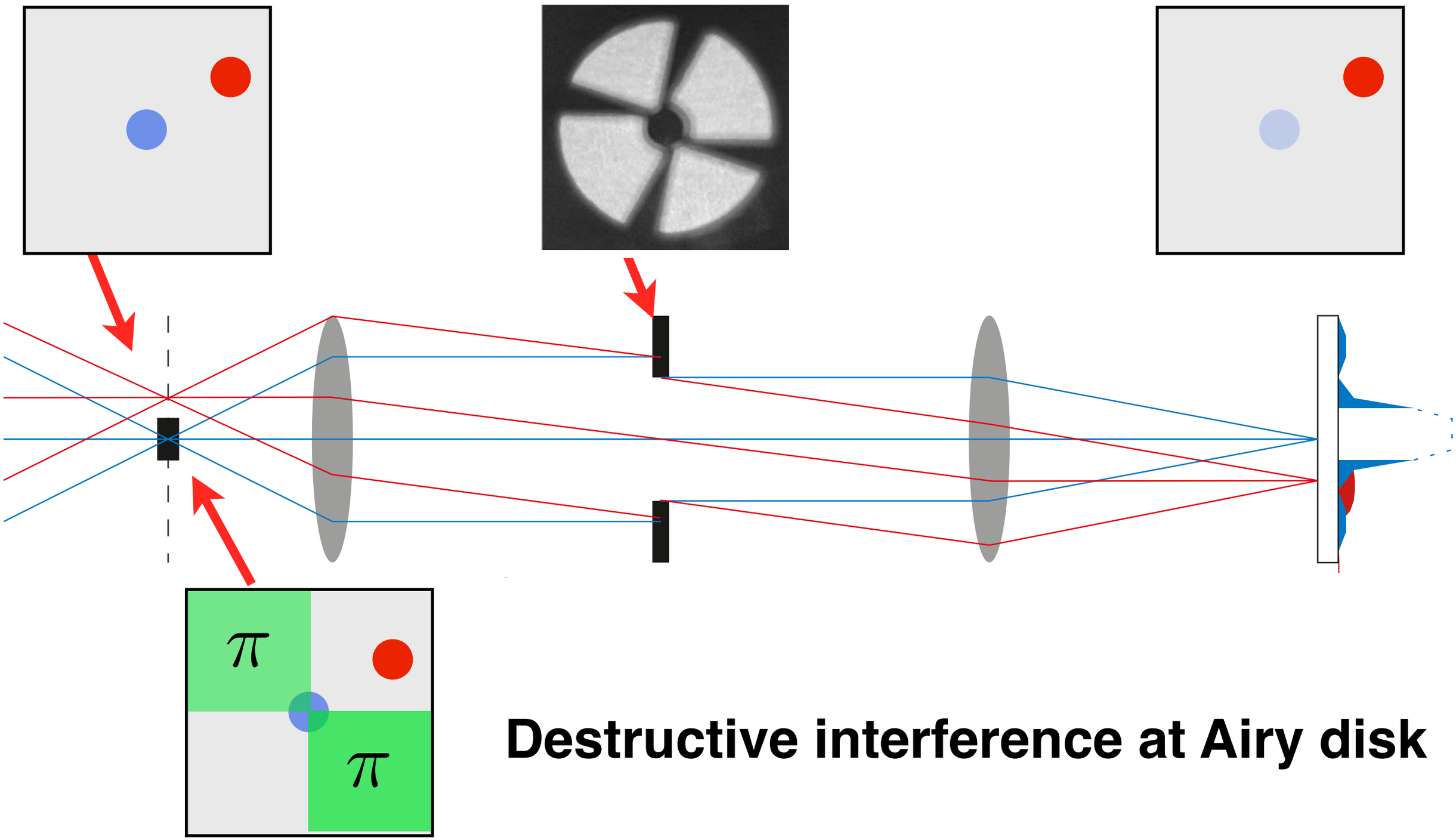
Phase Induced Amplitude Apodization

Mask off the central PSF and then an inverse PIAA recombines the planet images



Guyon 2003

Four Quadrant Phase Mask (4QPM)



Destructive interference at Airy disk

Boccaletti (2004) PASP 116 1061

PSF with 2 and 4 Quadrant Mask

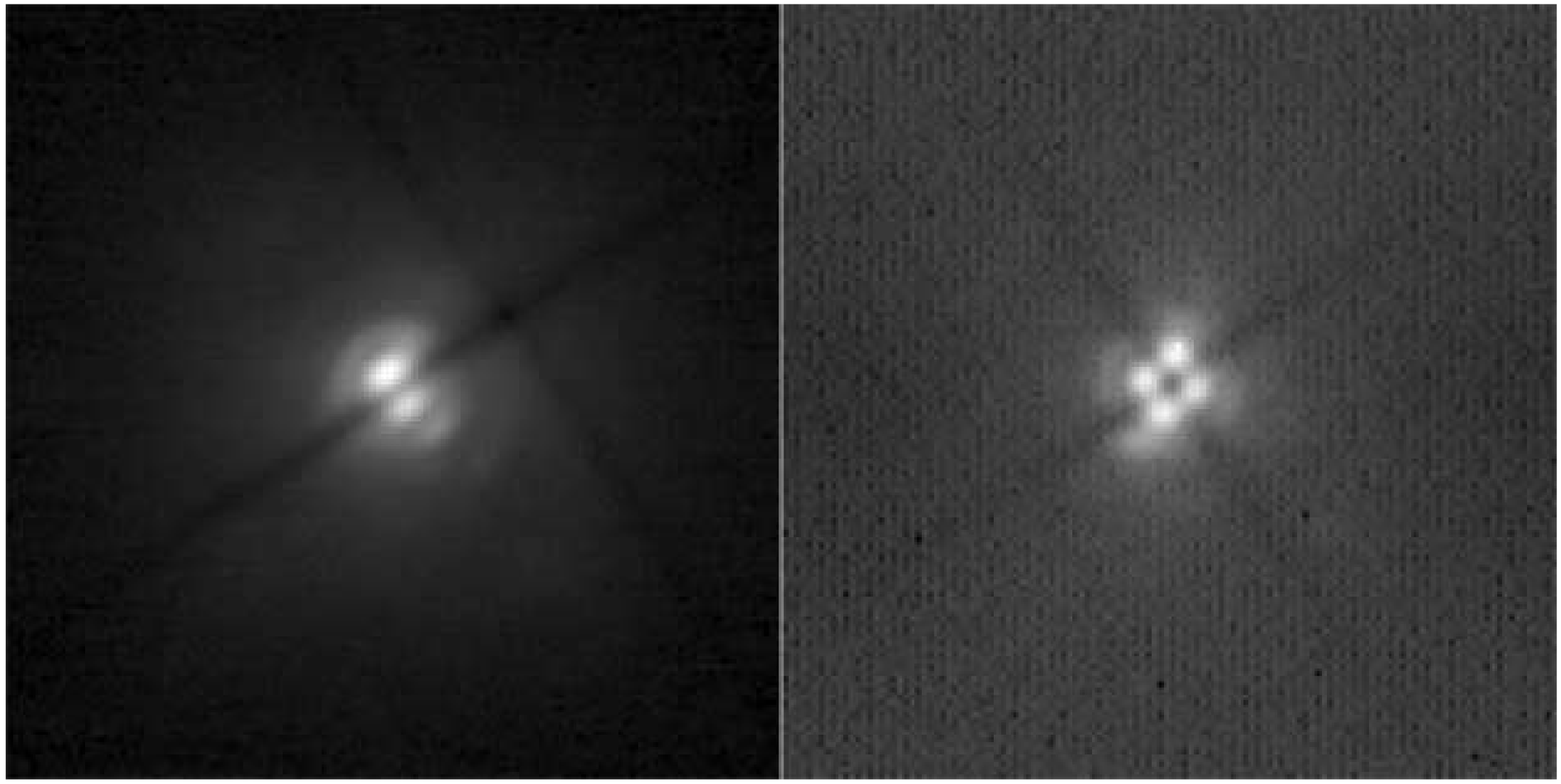
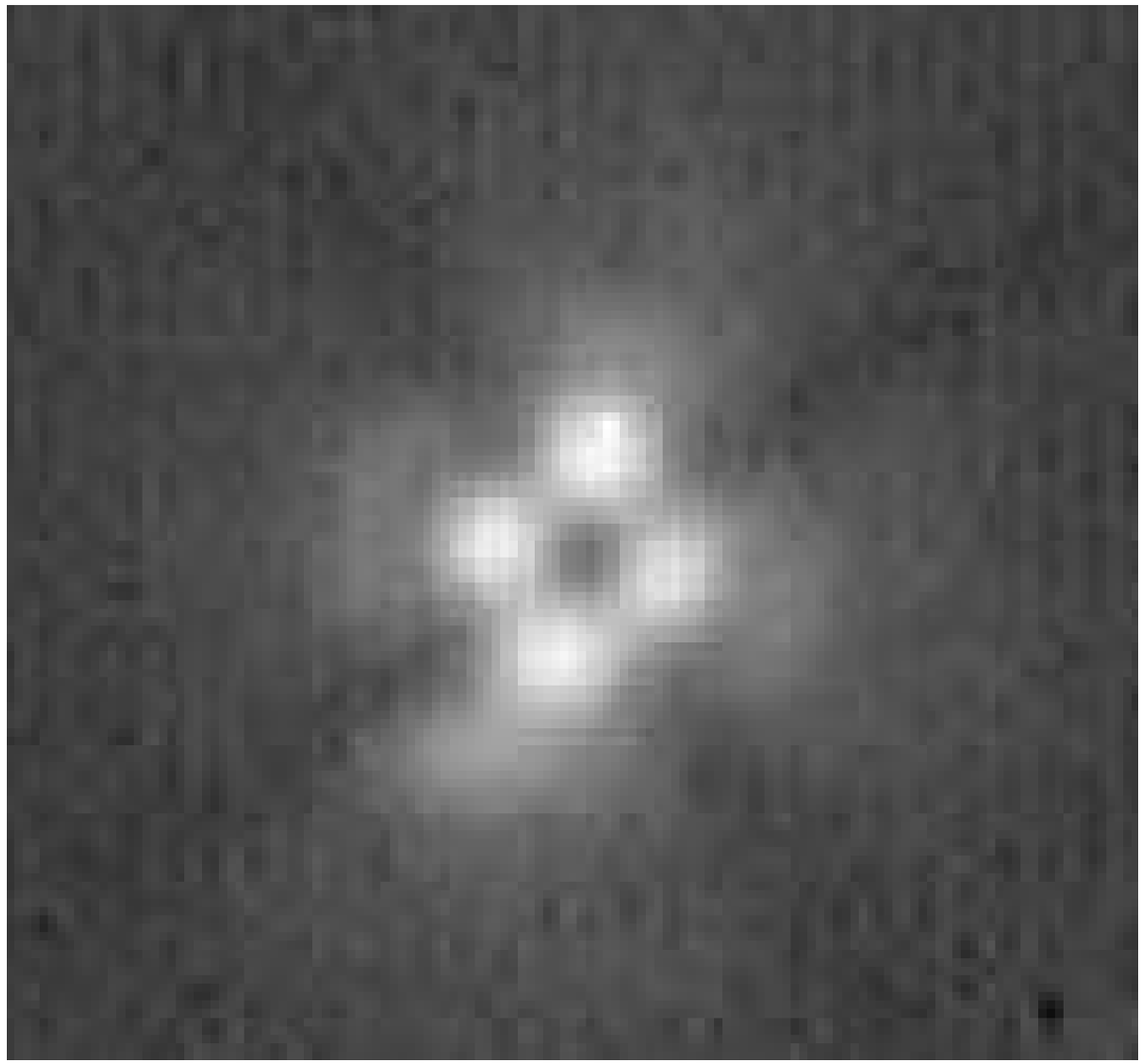


FIG. 3.—Two-quadrant (*left*) and four-quadrant (*right*) images of residuals for HD 32305 obtained in the K_s band. The intensity scale is not identical on both images. For comparison, the PSF peak attenuation is 3.9 on the two-quadrant image and 8.1 on the four-quadrant image.

Boccaletti 2004 PASP

Problems: PSF has blank edges



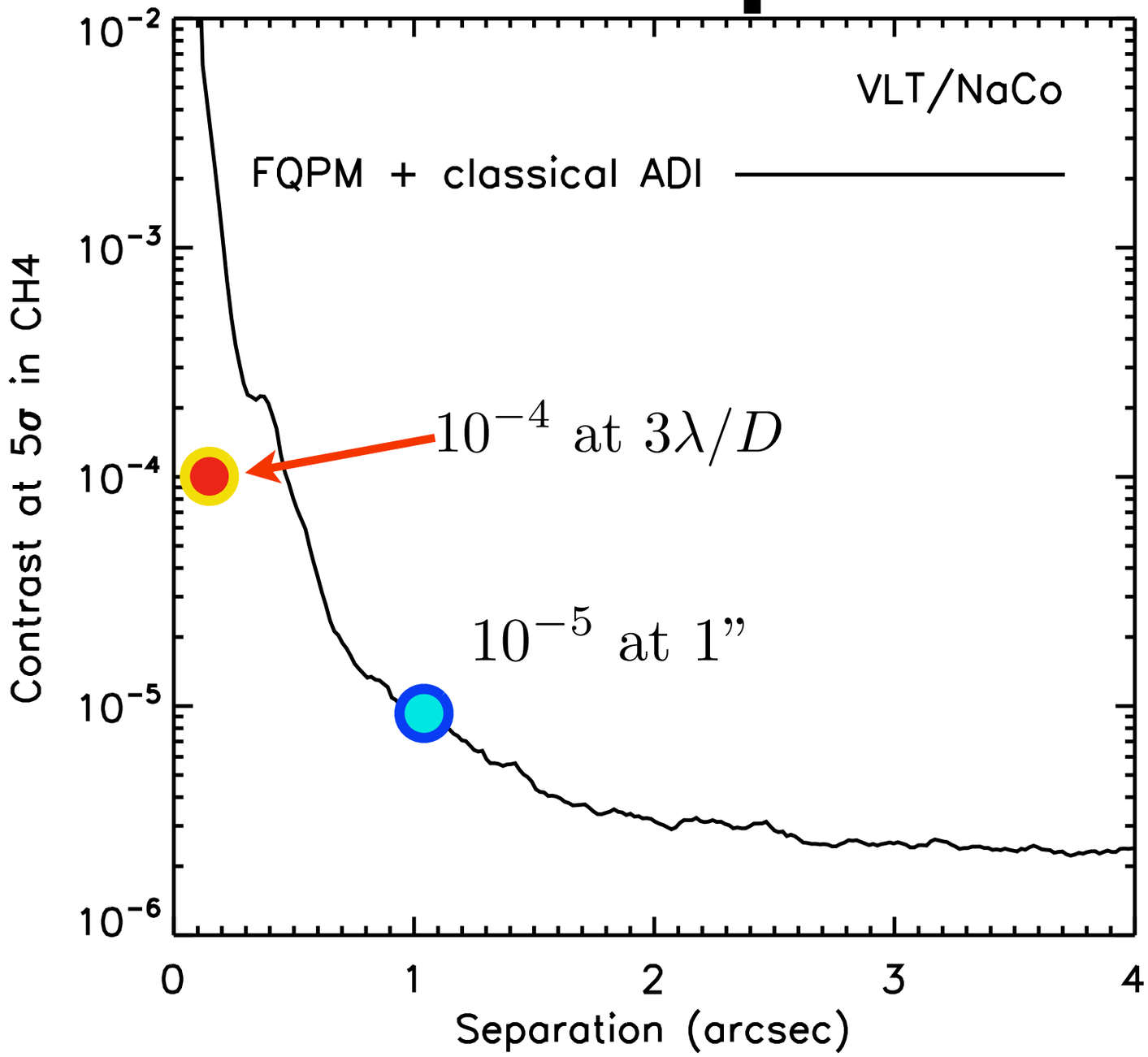
Boccaletti 2004 PASP

4QPM on a double star

FIG. 9.—HIP 1306 PSF (*left*) and FQPM image (*right*). The exposure time is 60 s for the coronagraphic image and 4 s for the PSF. Not a linear intensity scale ($I^{0.5}$). FOV is 1″.25. North is up.

Boccaletti 2004 PASP

4QPM measured performance

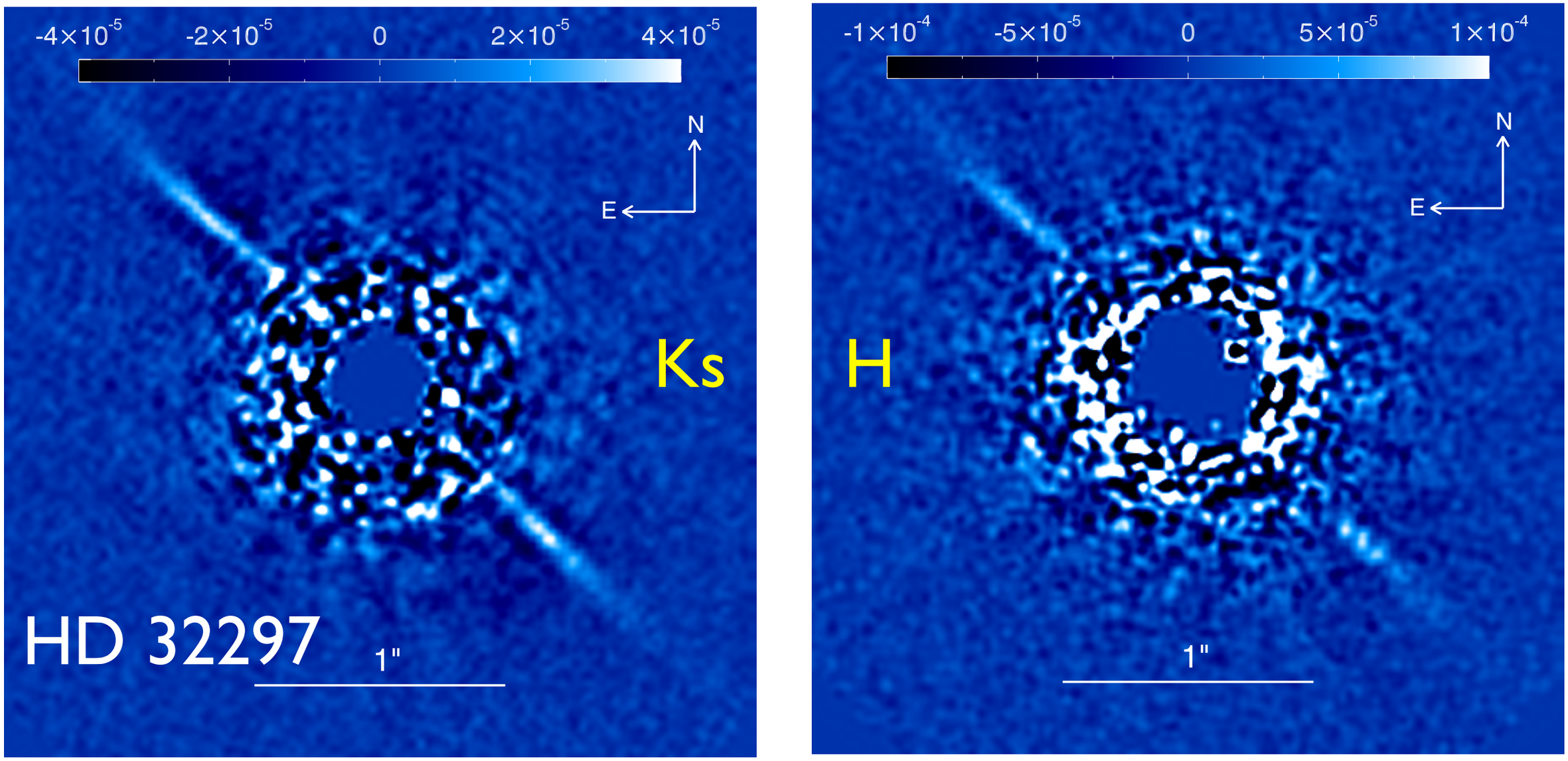


Anne-Lise Maire PhD Thesis (2012)

Observatoire de Paris

Characterisation des exoplanetes par imagerie depuis le sol et l’espace

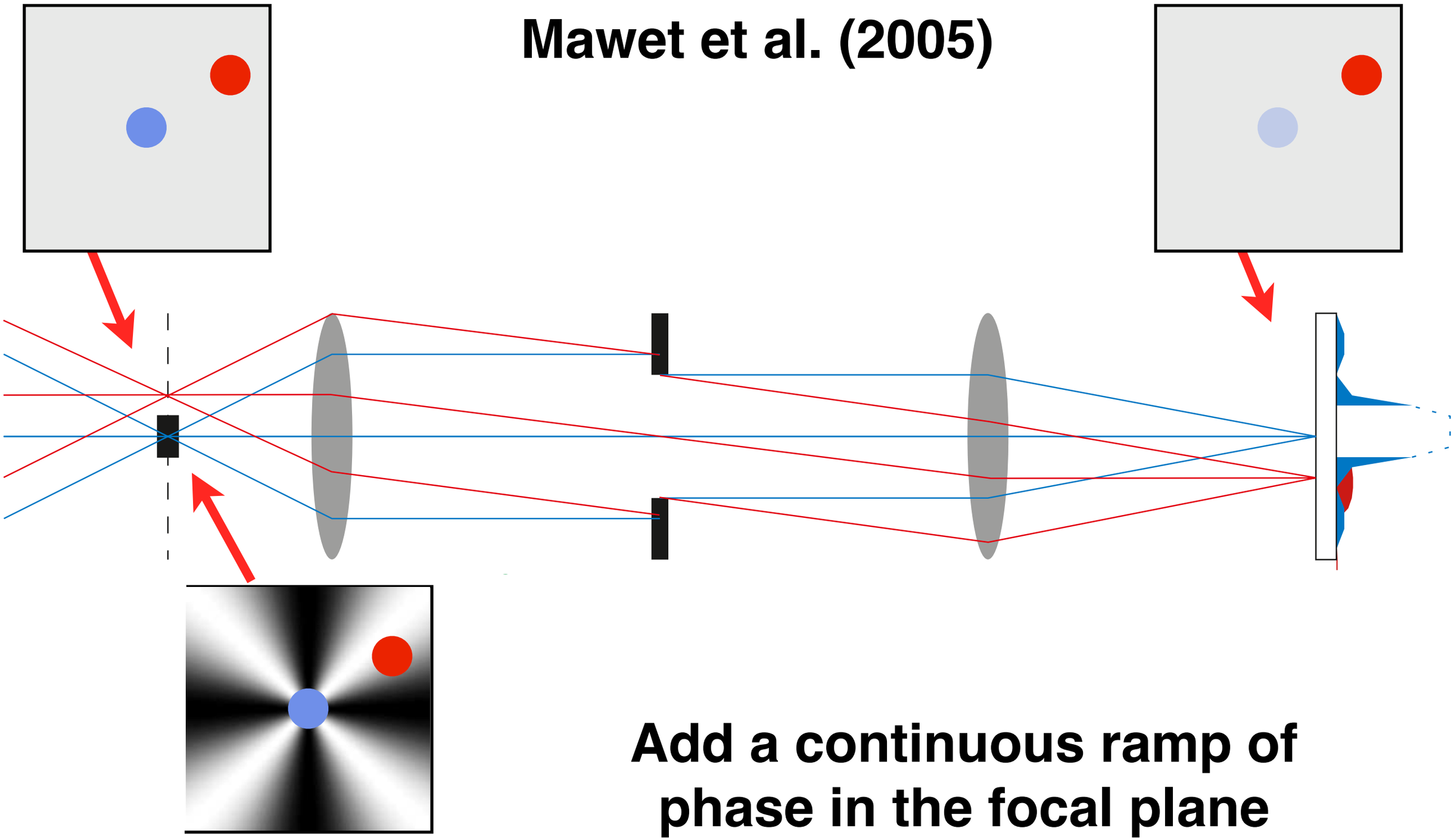
Imaging Disks



Boccaletti et al. (2012)

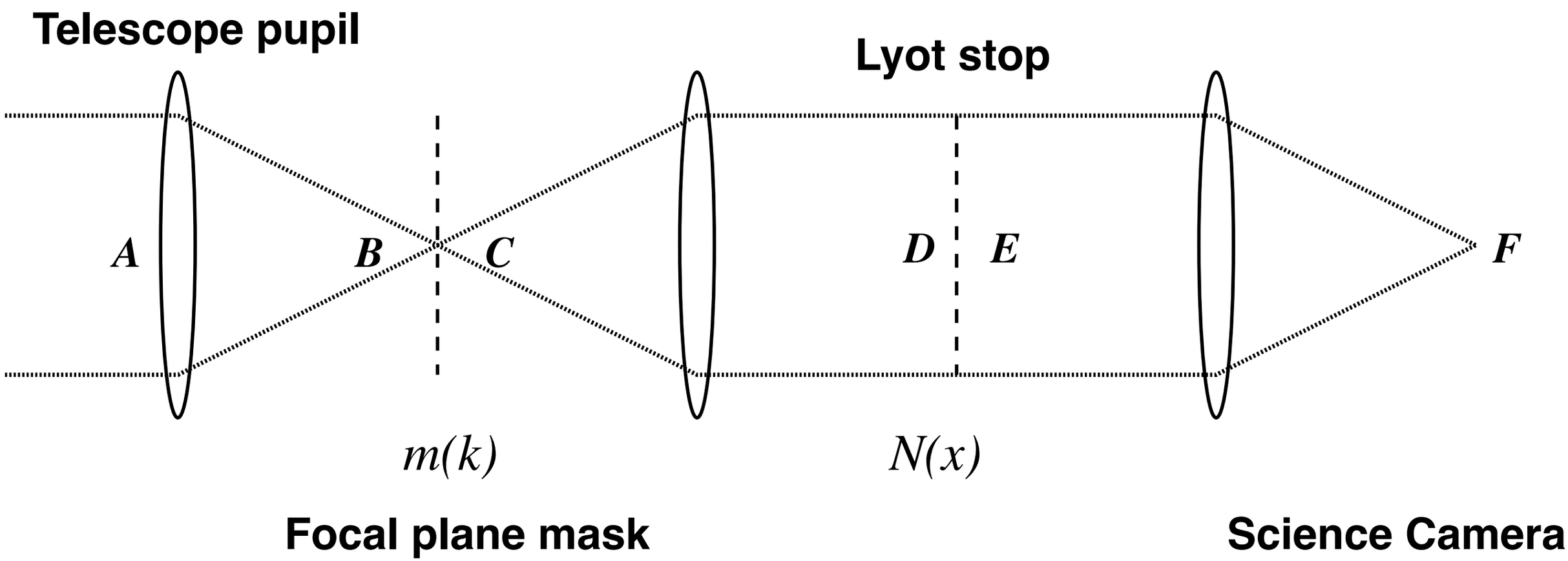
Annular Groove Phase Mask

Mawet et al. (2005)



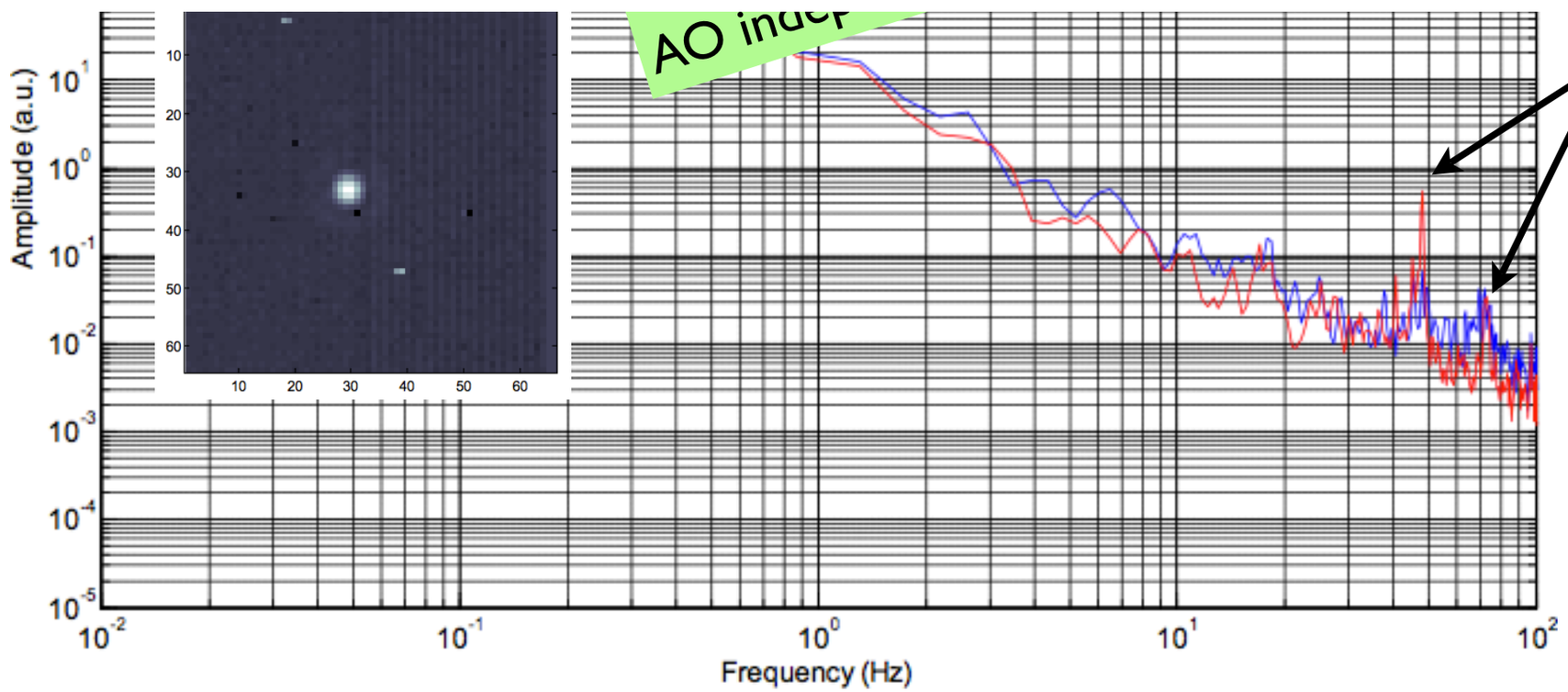
Add a continuous ramp of phase in the focal plane

Focal plane coronagraphs are sensitive to telescope shake



Telescope Vibrations

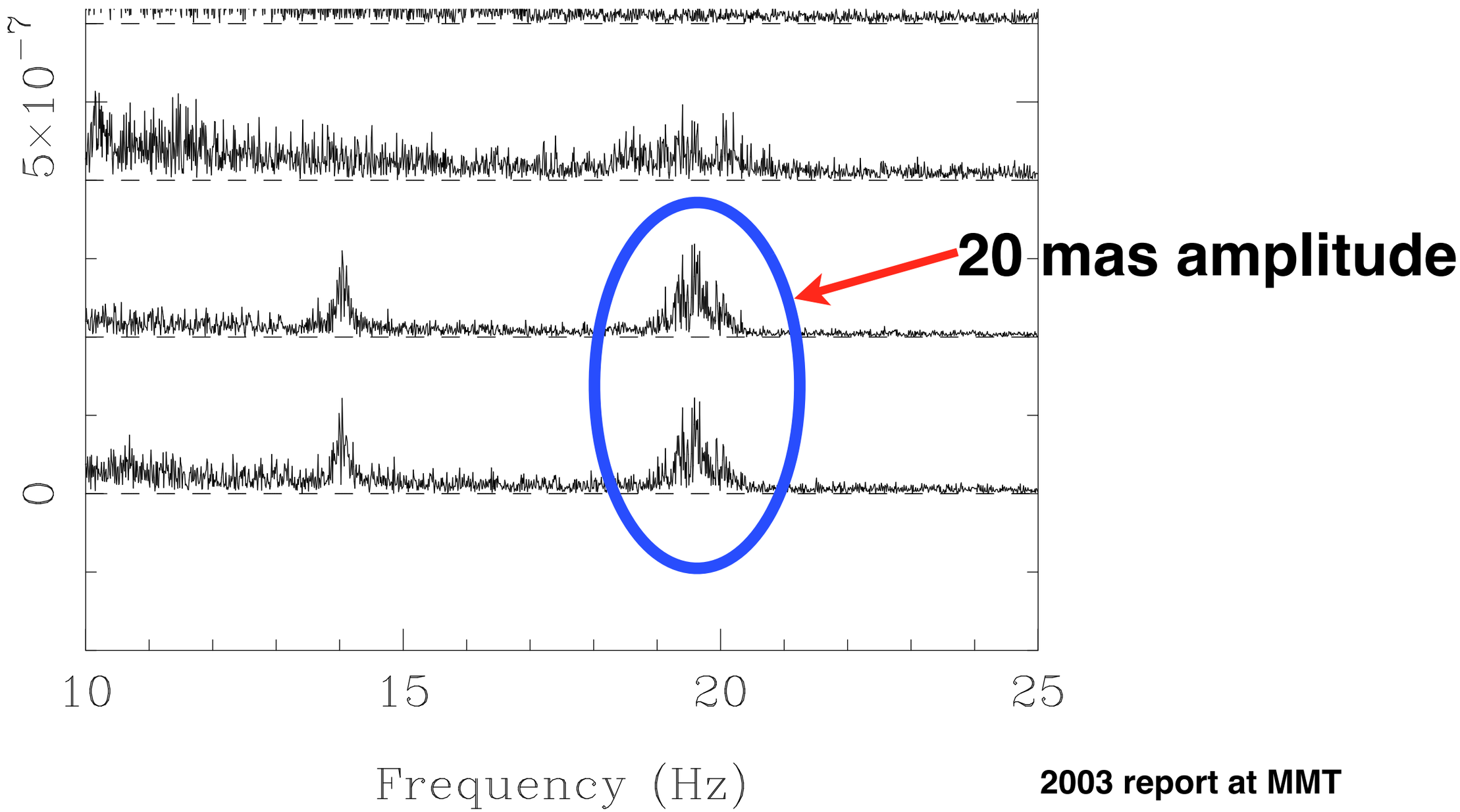
CONICA
L' imaging
200 Hz
(5 ms)



Peaks
@
48 Hz
~70Hz

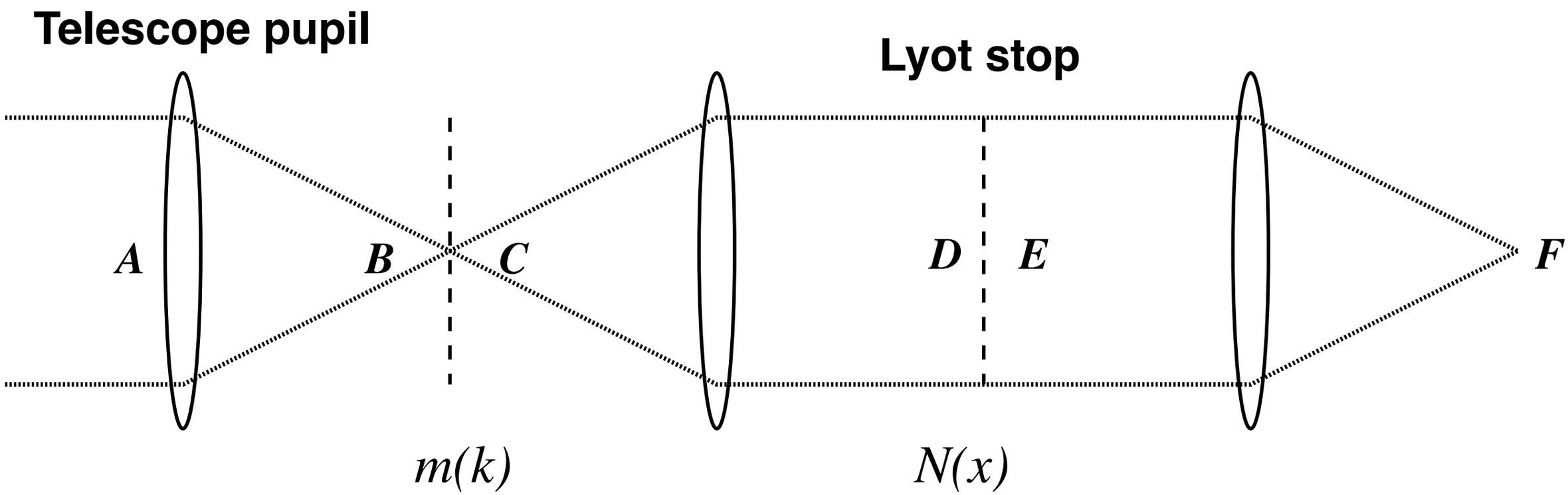
Girard et al. (2012) SPIE

Telescope Vibrations



2003 report at MMT

Pupil plane coronagraphs are NOT sensitive to shake!



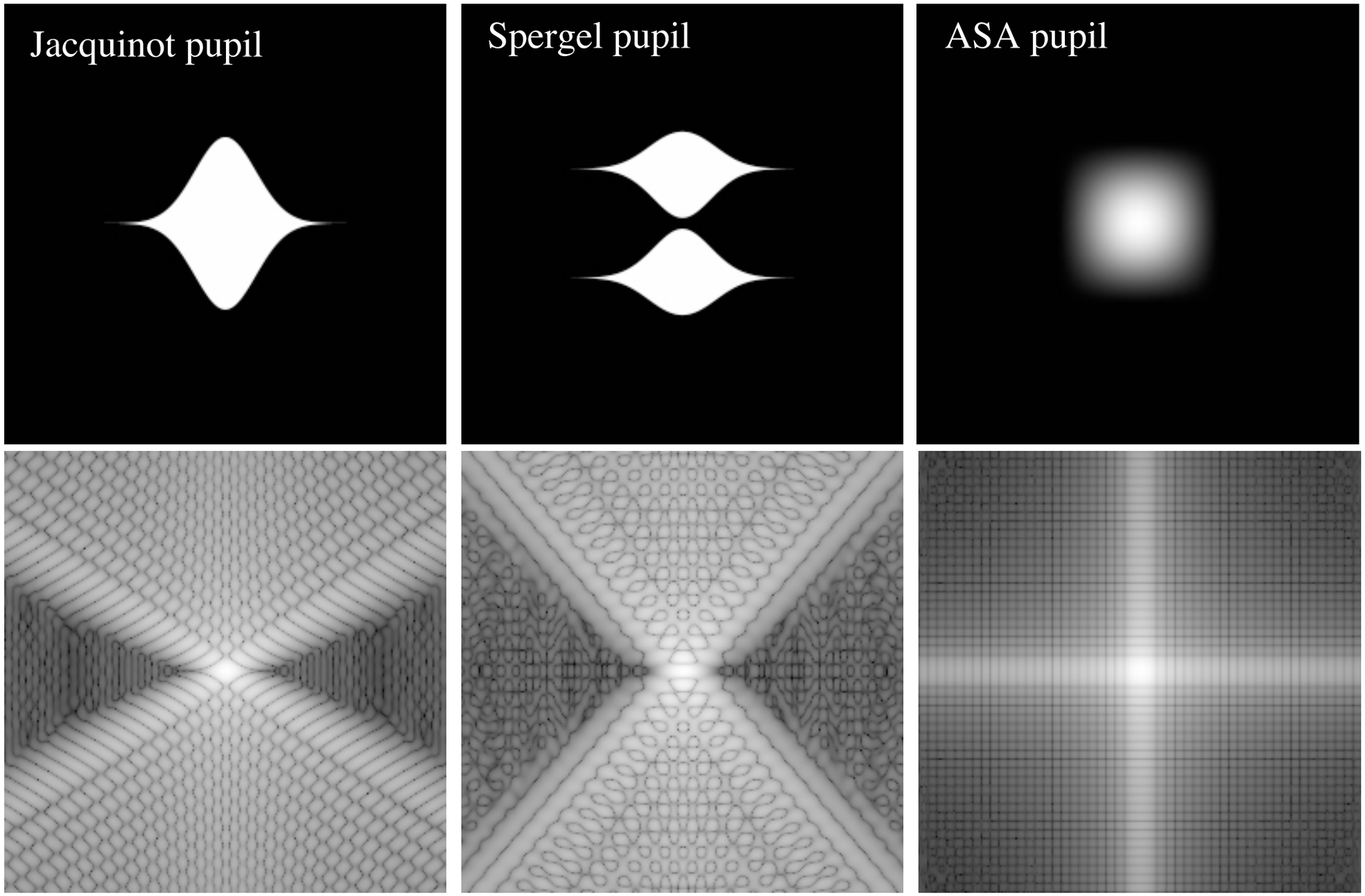
They modify the shape of the telescope PSF to have a dark region

Classical Pupil Apodization

Modify the telescope pupil through AMPLITUDE and/or PHASE to remove the effects of diffraction

Pupil

PSF



Jacquinot & Roizen-Dossier 1964

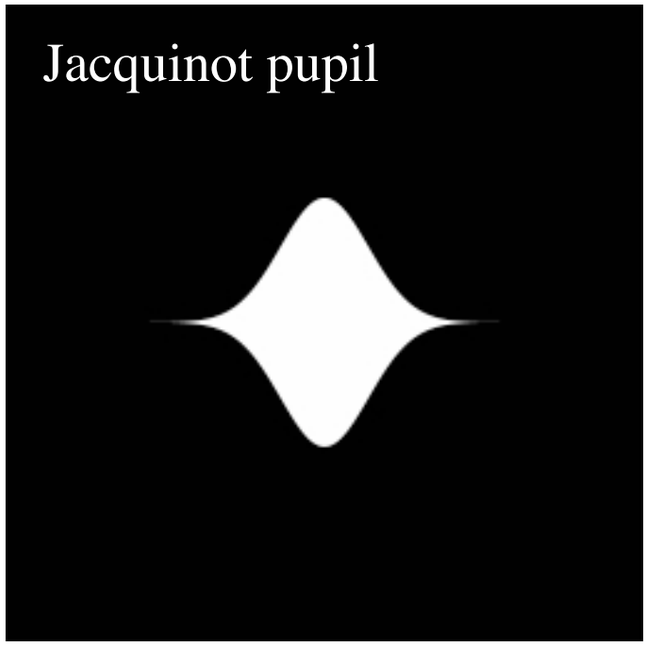
Spergel 2001

Classical Pupil Apodization

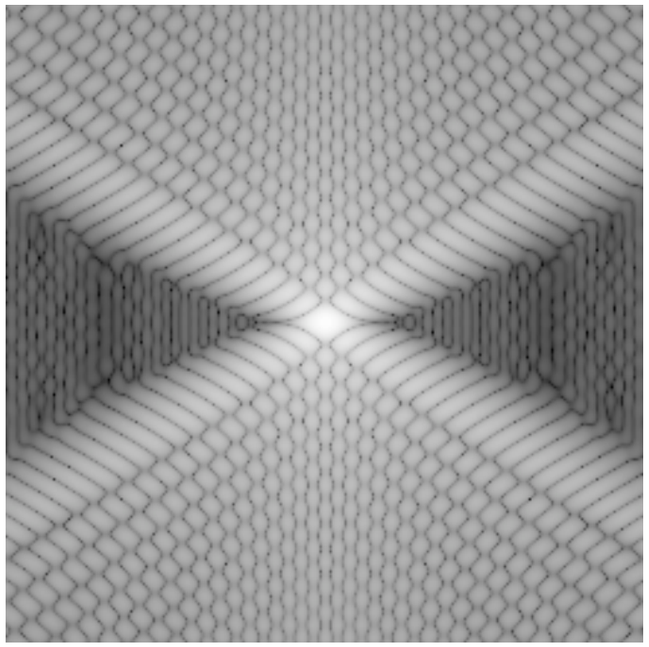
Most have very low throughput (~0.1 to 0.3) and limited field of view

Jacquinot & Roizen-Dossier 1964

Pupil



PSF



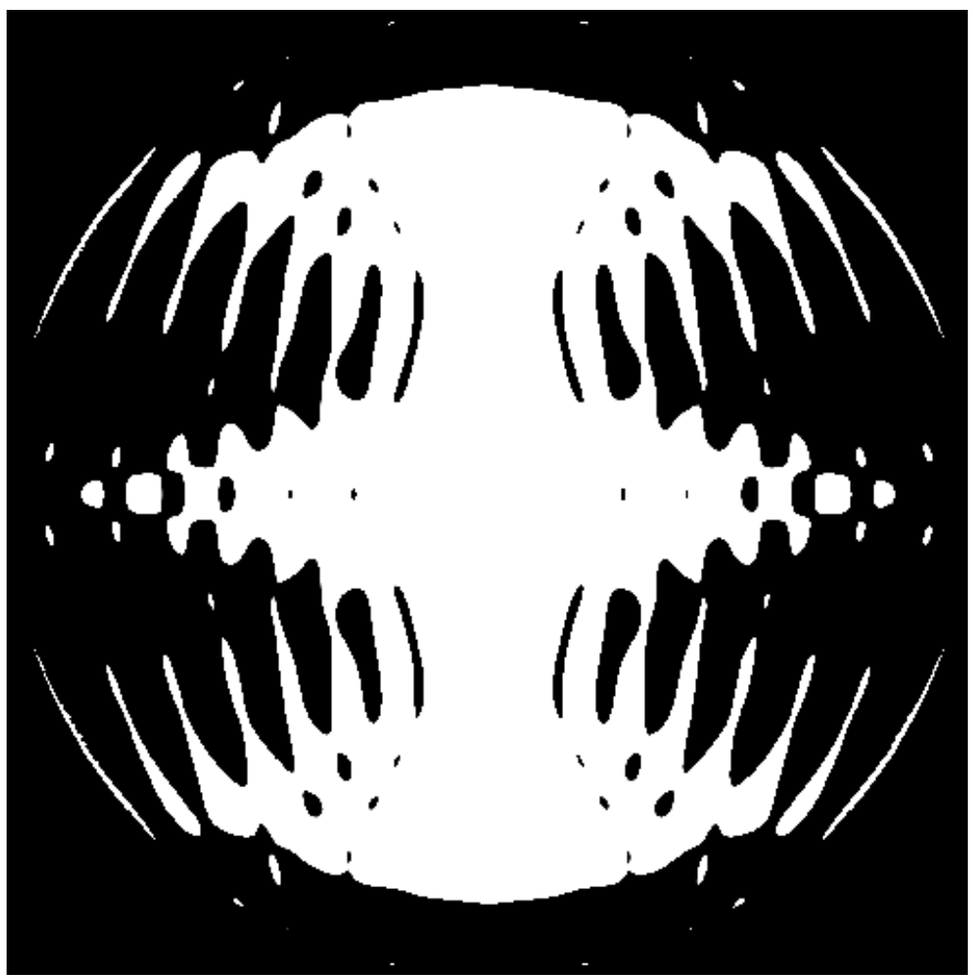
$$|y| < R \times \left(e^{-\left(\frac{\alpha x}{R}\right)^2} - e^{-\alpha^2} \right) \tag{7}$$

where R is the radius of the pupil, x and y are the D coordinates in the pupil plane, and $\alpha = 2$. The pupil transmission is equal to 0 everywhere else.

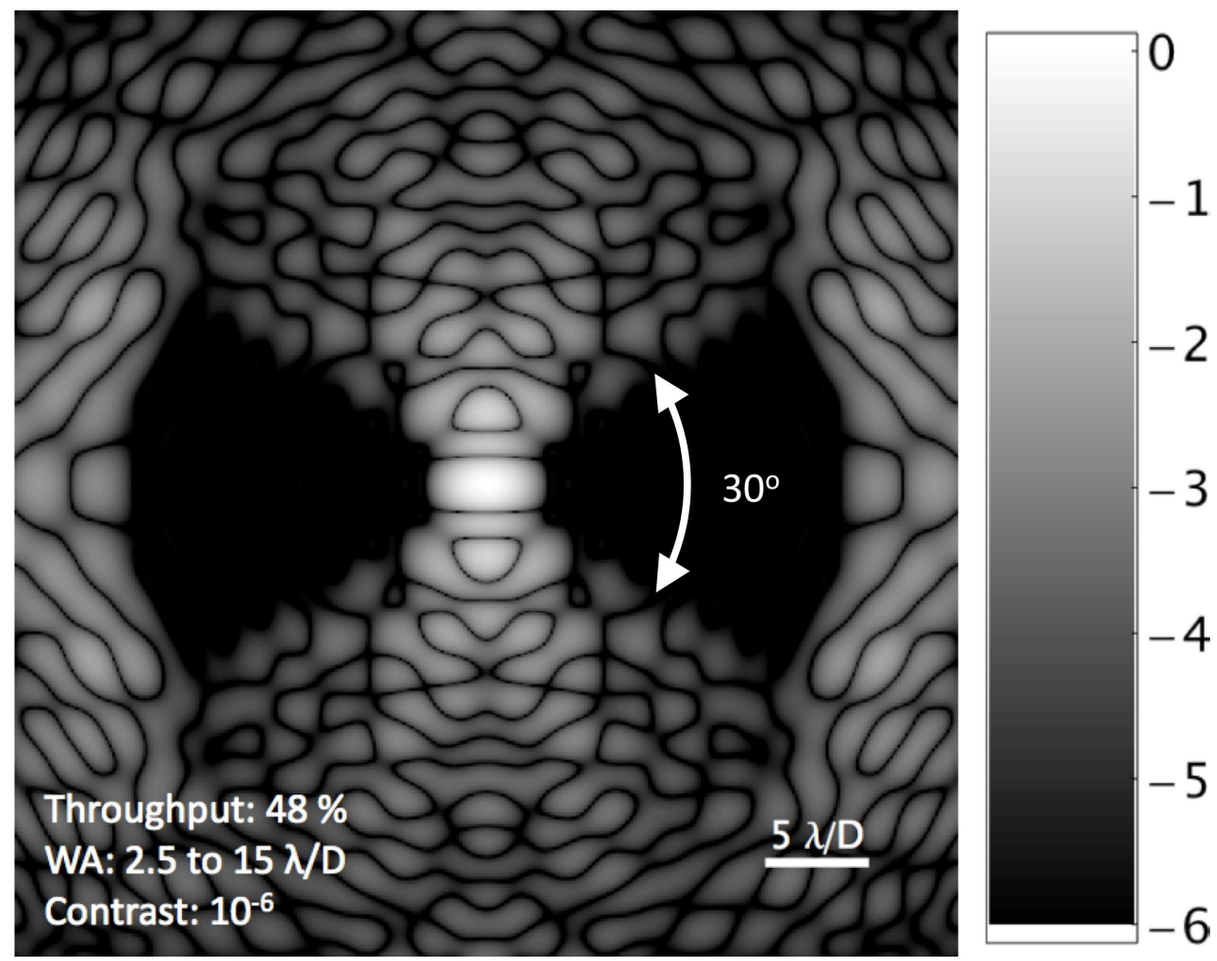
Optimized Pupil Apodizations

Developed by Carlotti, Vanderlei and Kasdin

Pupil



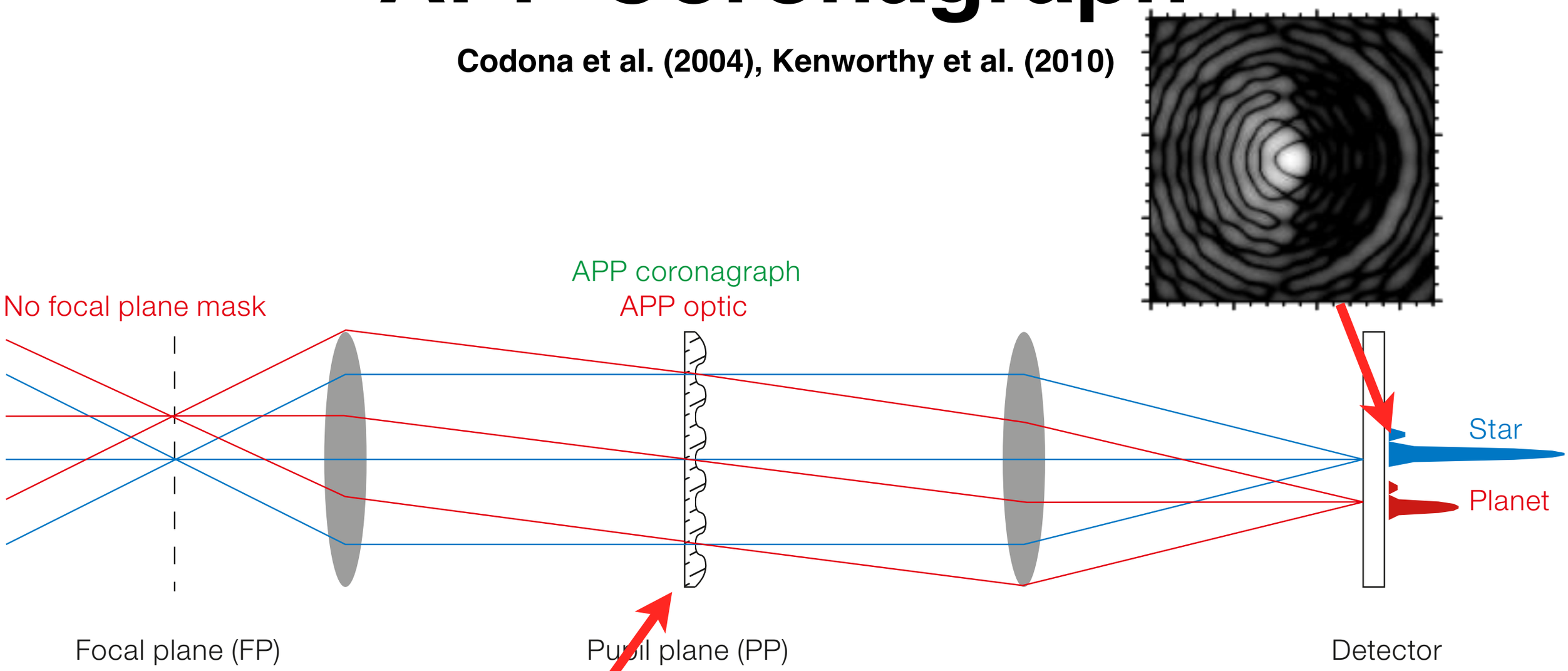
PSF

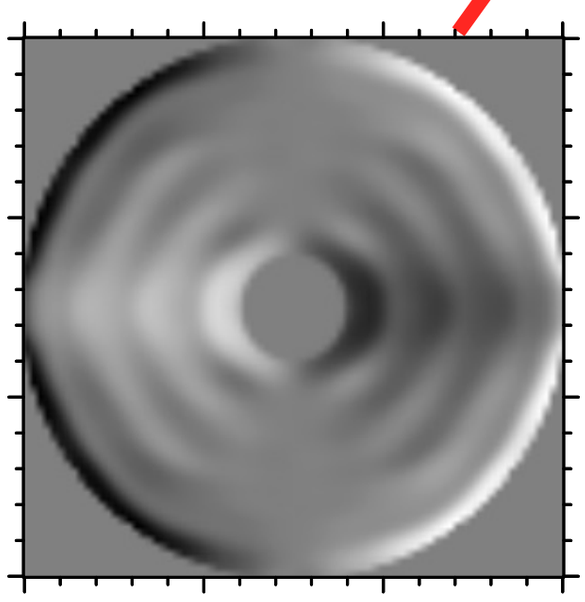


Carlotti 2011 JOSA

APP Coronagraph

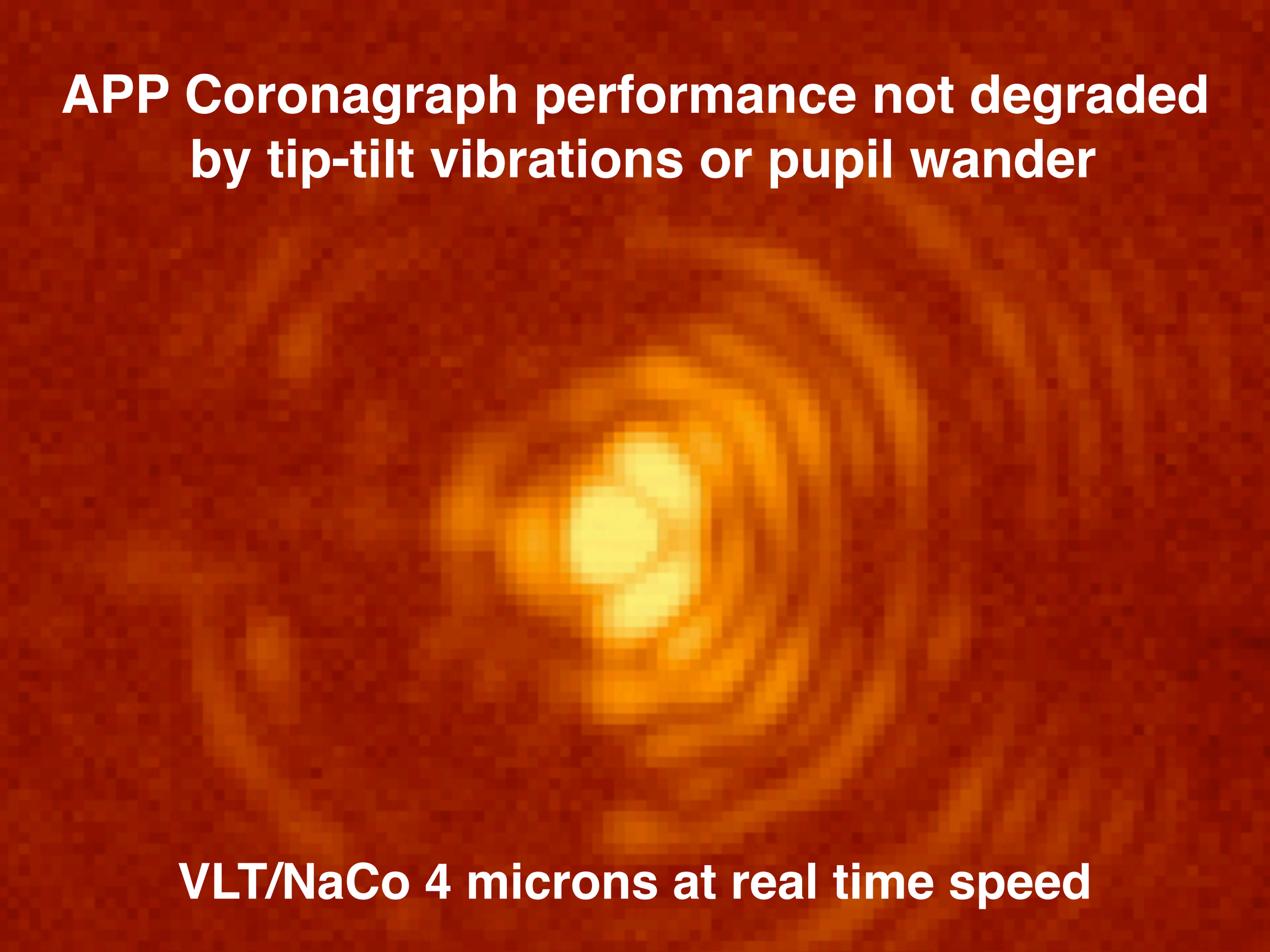
Codona et al. (2004), Kenworthy et al. (2010)



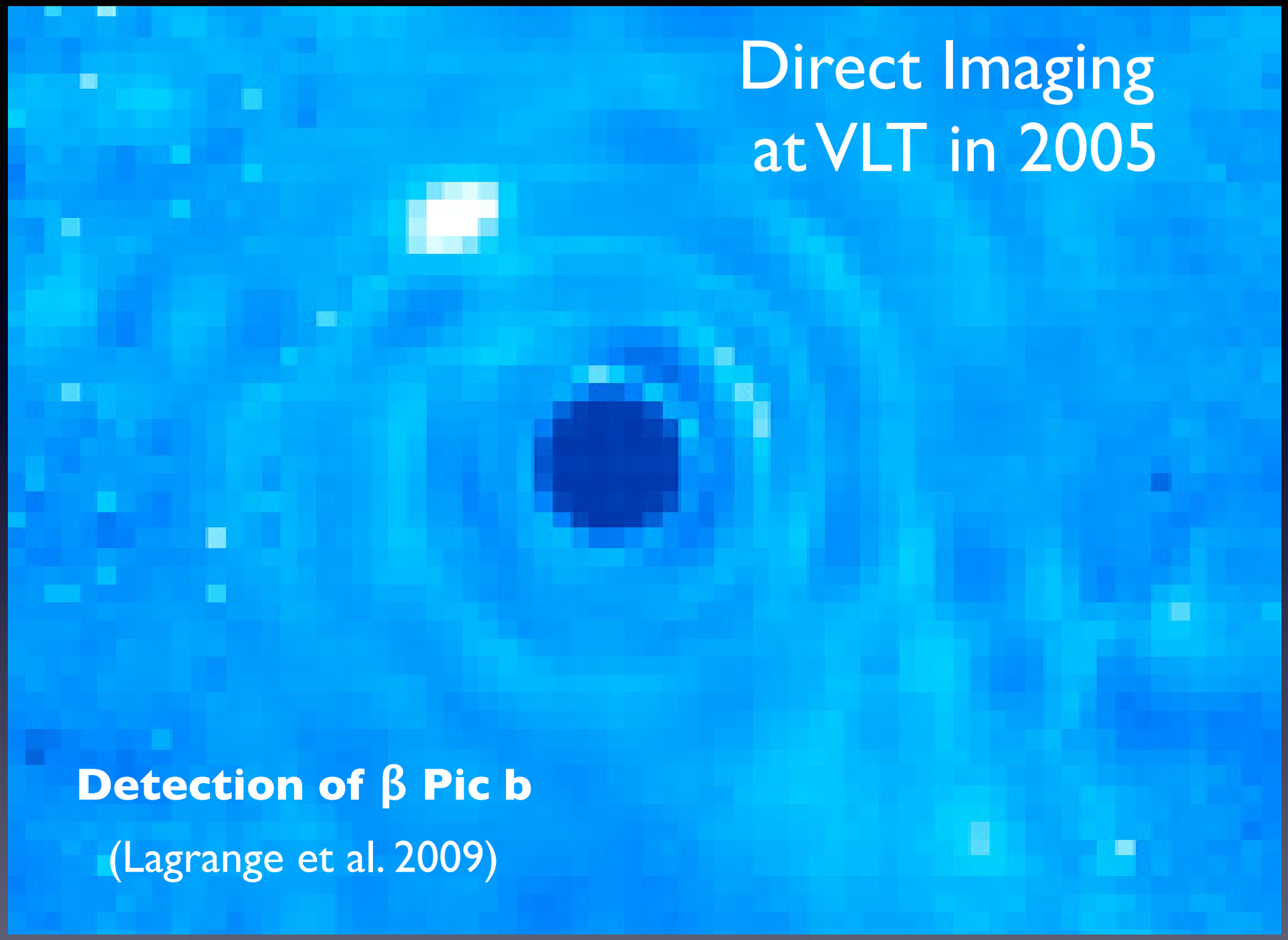


Apodize with phase instead of amplitude

APP Coronagraph performance not degraded by tip-tilt vibrations or pupil wander



VLT/NaCo 4 microns at real time speed

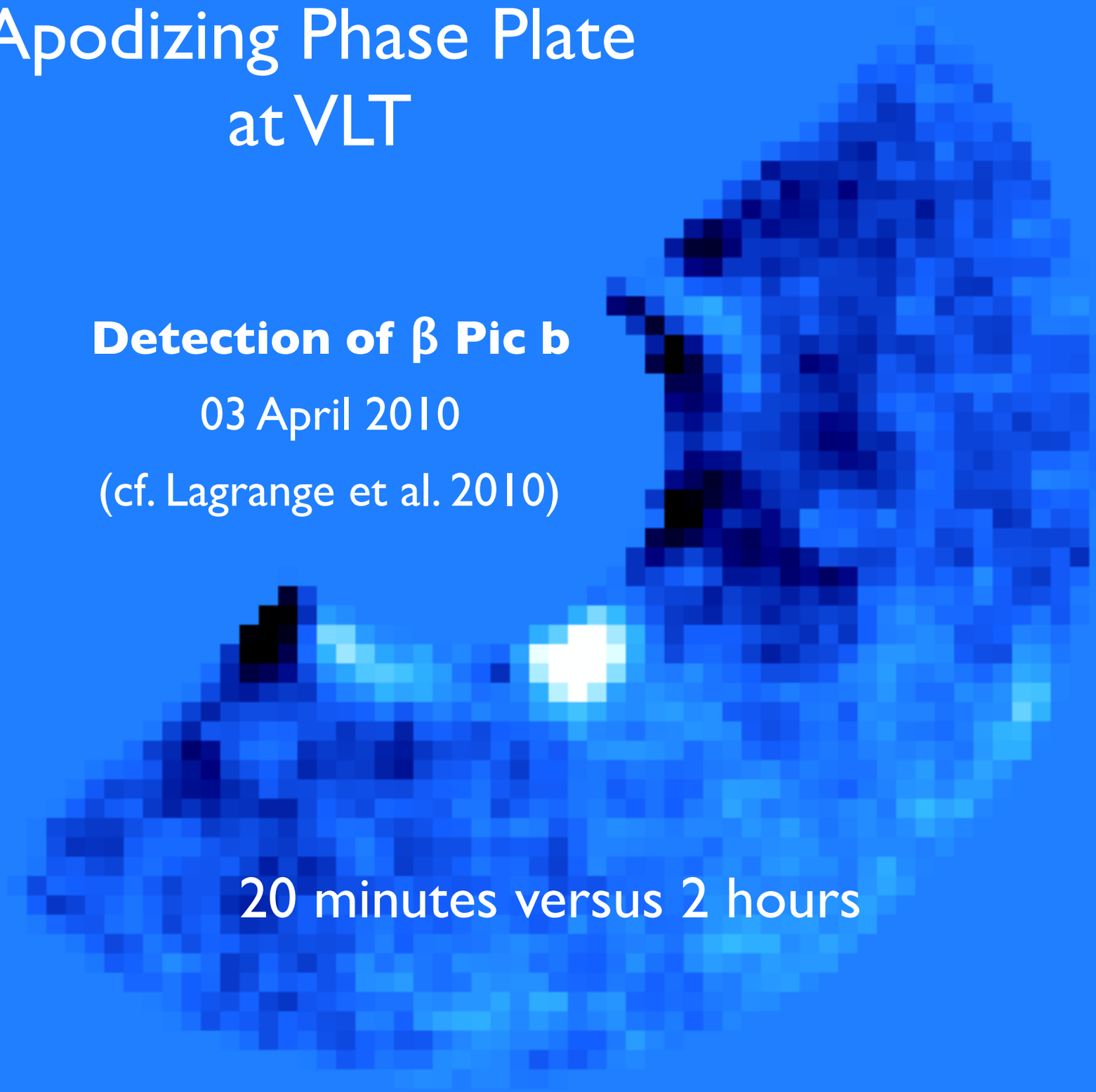

Direct Imaging
at VLT in 2005
Detection of β Pic b
(Lagrange et al. 2009)

Apodizing Phase Plate at VLT

Detection of β Pic b

03 April 2010

(cf. Lagrange et al. 2010)

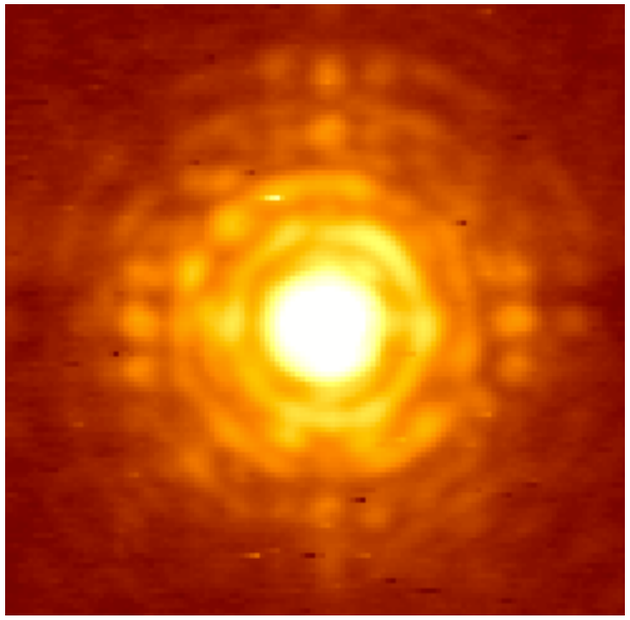


20 minutes versus 2 hours

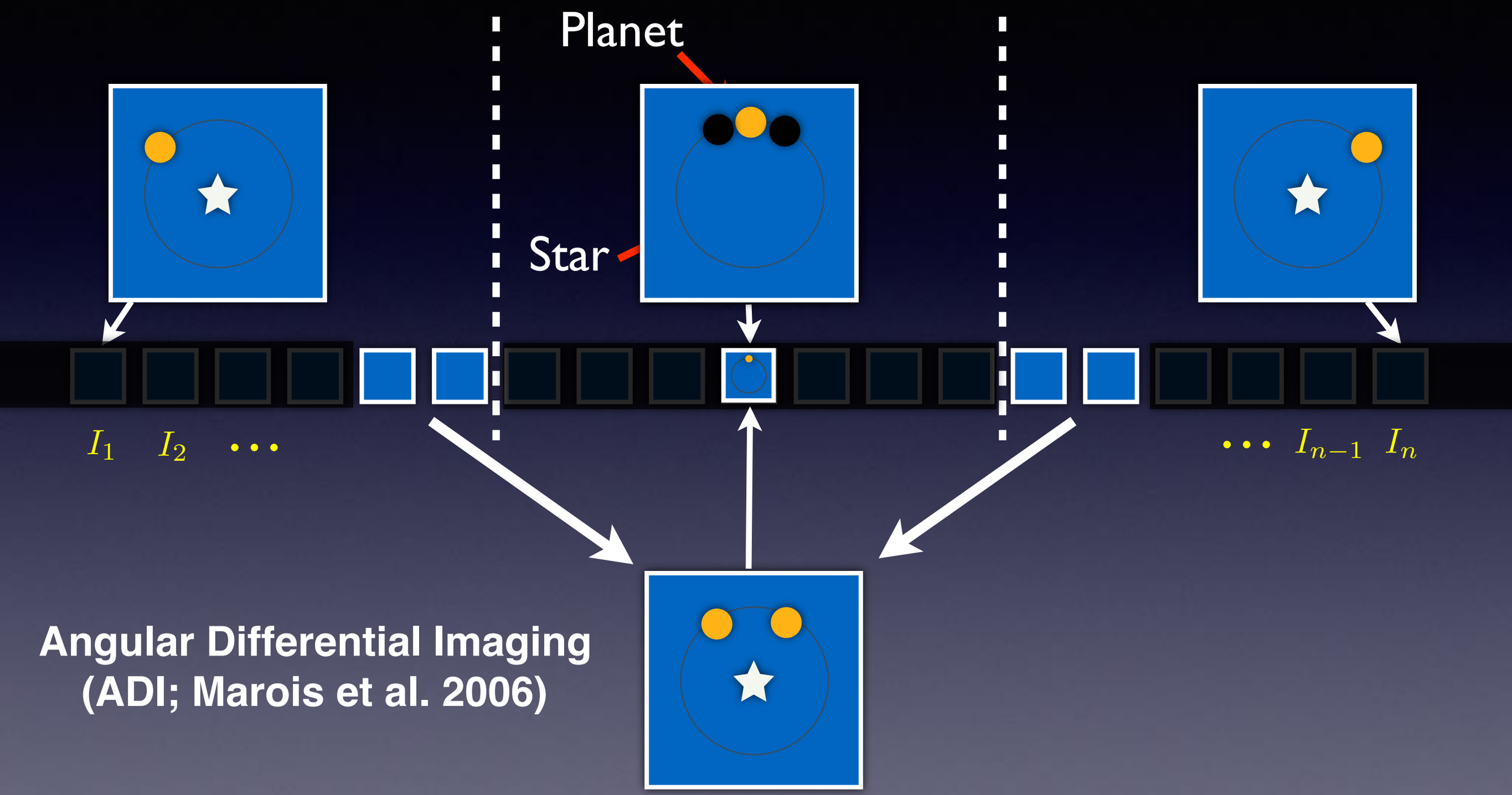
Quanz et al. (2010)

What do we want?

The instrumental PSF
for each Science Camera Image

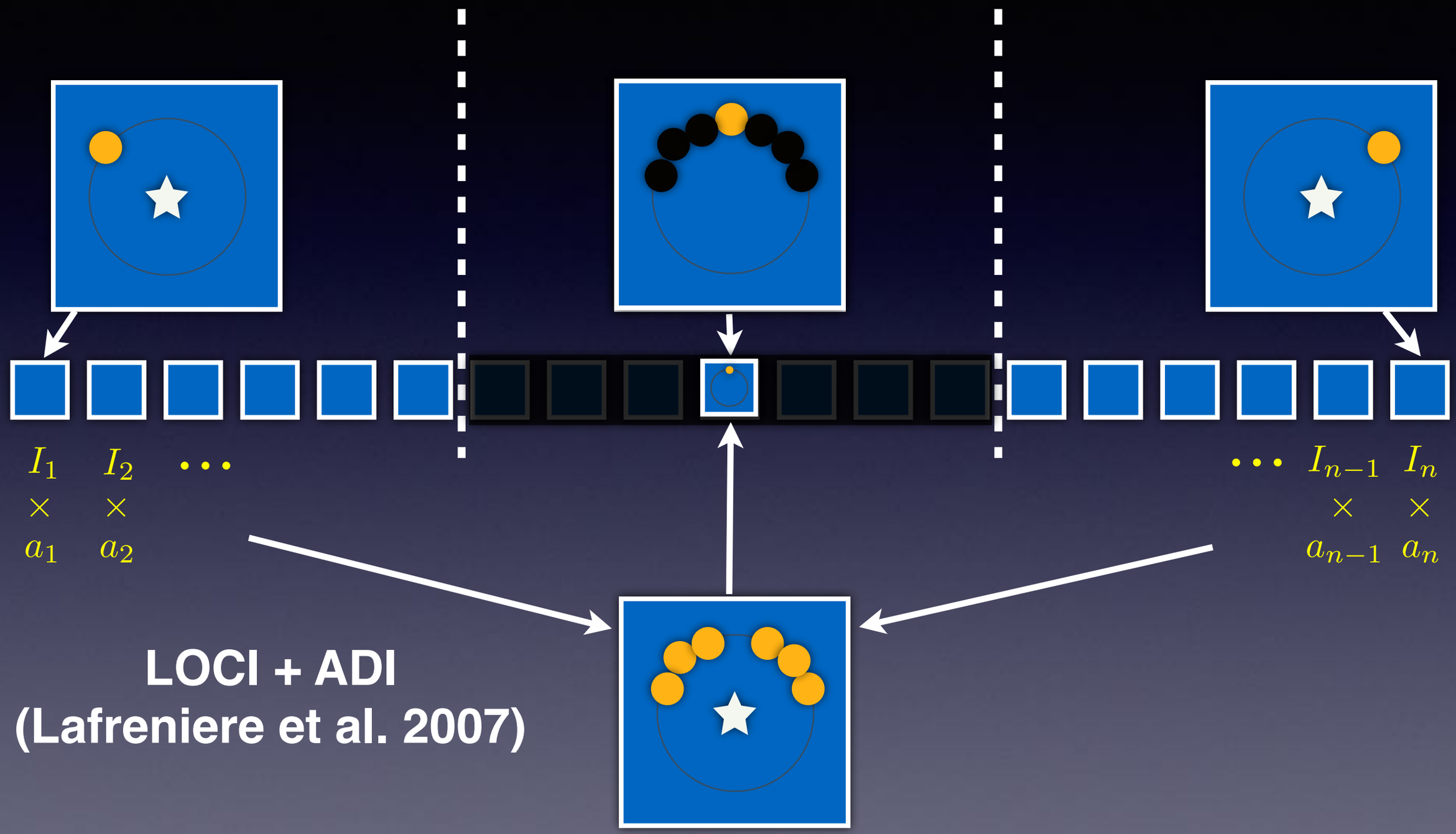


Approximating the Science PSF



Angular Differential Imaging (ADI; Marois et al. 2006)

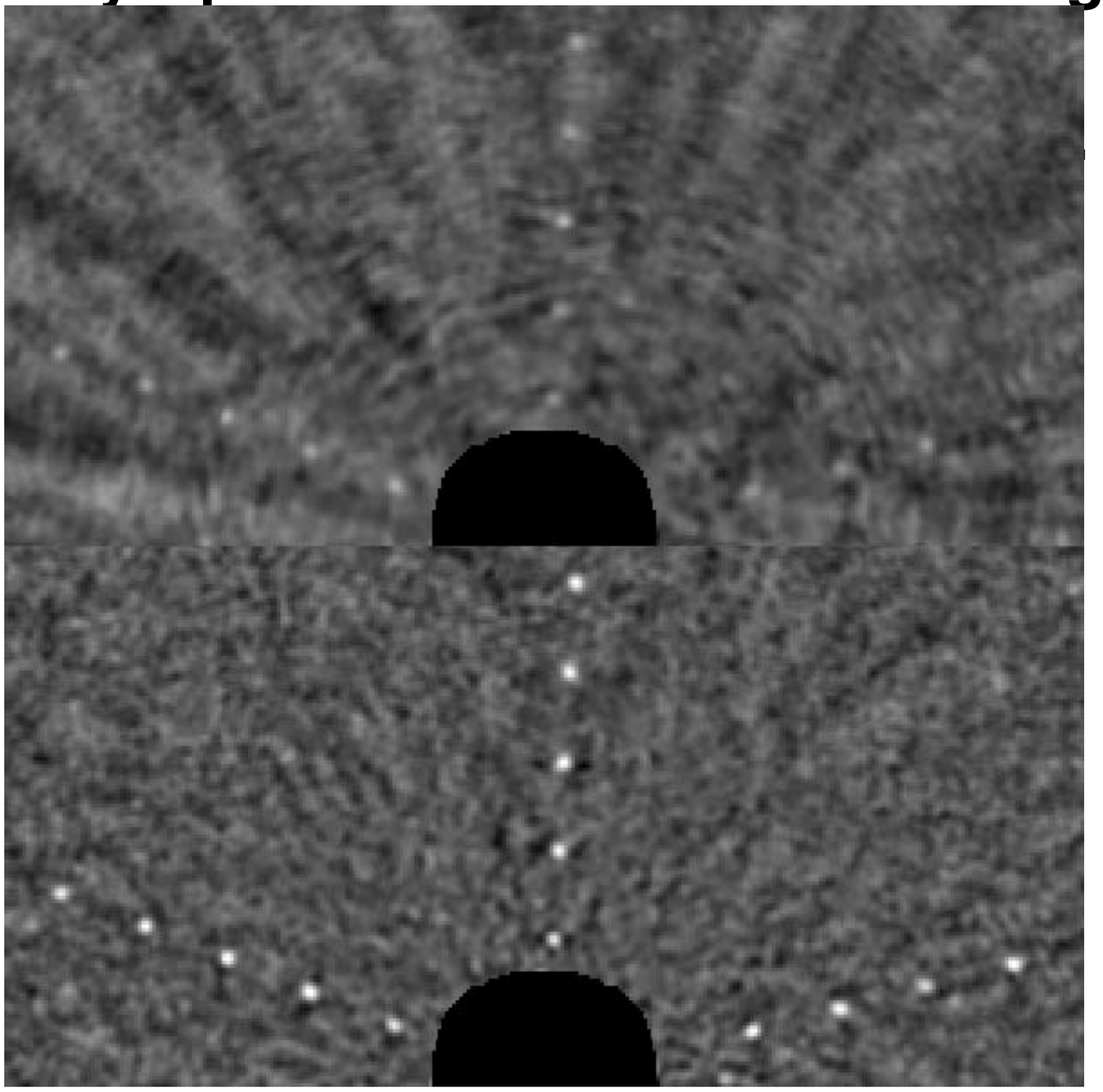
Approximating the Science PSF



LOCI + ADI
(Lafreniere et al. 2007)

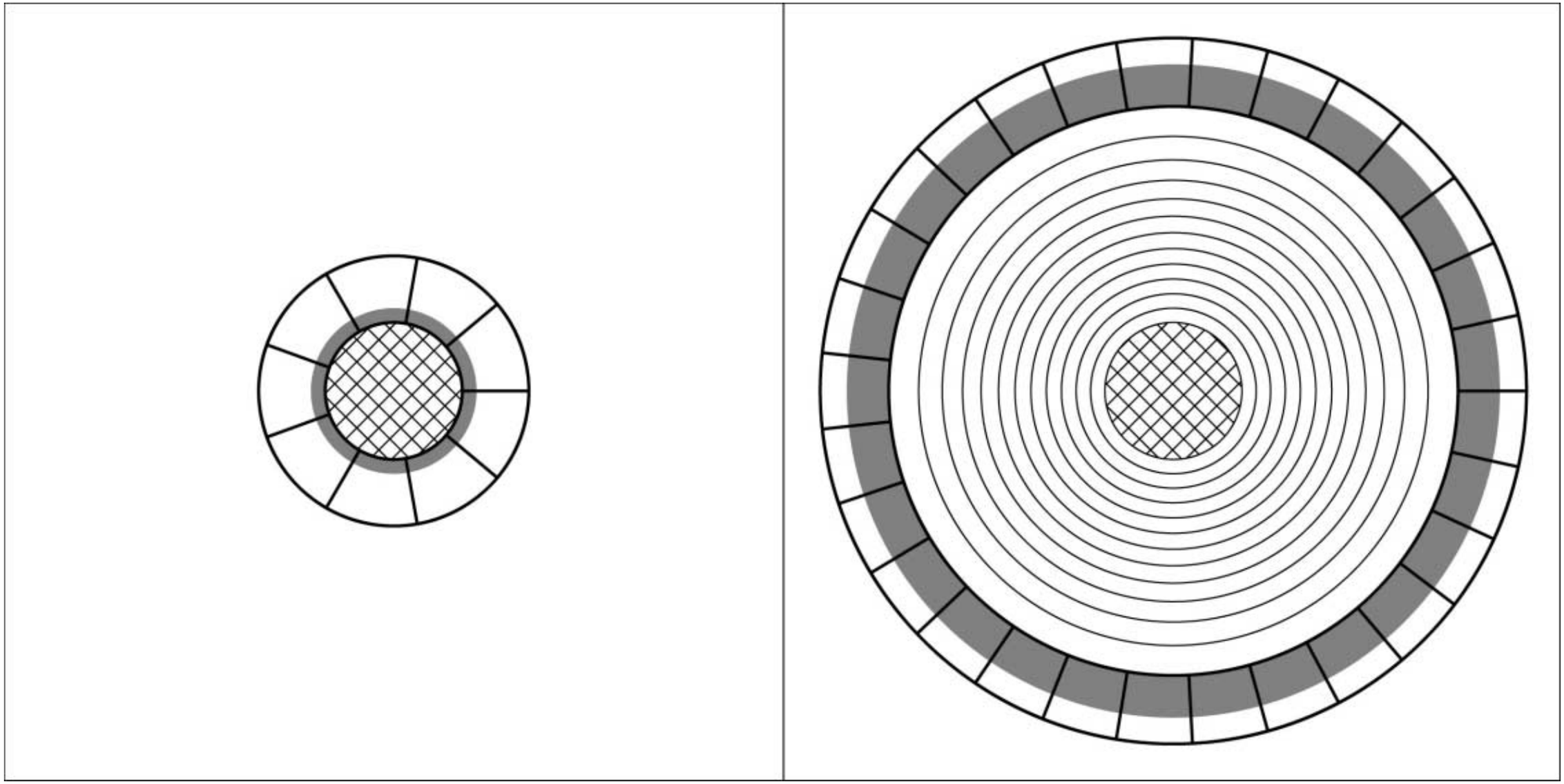
LOCI

Locally Optimised Combination of Images



LOCI

Locally Optimised Combination of Images



Optimization region geometry a challenge

Stars and Planets

Typically 1e4 to 1e9 times brighter than planet

Spatially separate from the star Photons are incoherent from the stellar photons

Diversity and Algorithms

Diversity: **The property that differentiates planets from speckles (e.g. Angular, Temporal, Spectral….)**

and

Algorithm: **The method used to combine the images to make a PSF based on the Diversity (e.g. LOCI, PCA)**

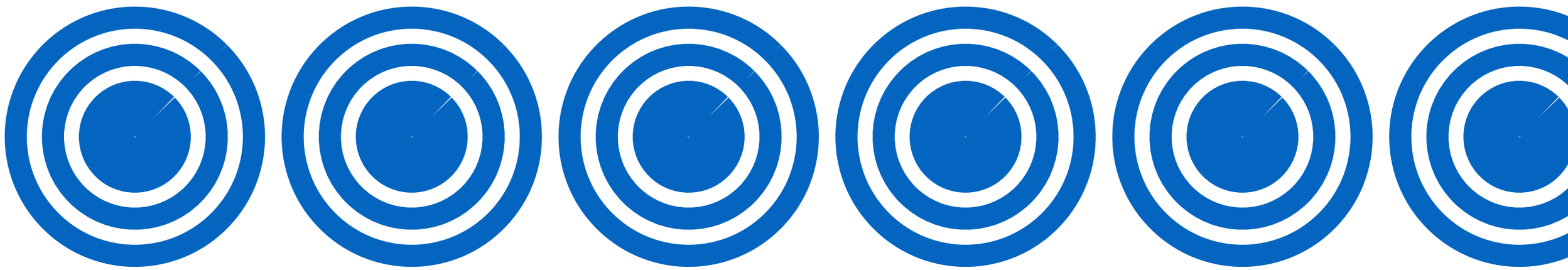
Diversity and Algorithms

So you can have:
ADI-LOCI, SDI-KLIP, and combinations
of different diversities as well!

Diversity and Algorithms

Name	Diversity/Algorithm	Paper
ADI	Angular Differential Imaging	Marois 2006
LOCI	Locally Optimised Combination of Images	Lafreniere 2007
ANDROMEDA		Mugnier 2008
SOSIE	ADI/SSDI/RSDI and LOCI	Marois 2010
PynPoint	Principal Component Analysis	Amara 2012
KLIP	Principal Component Analysis	Soummer 2012
DLOCI	Damped LOCI	Pueyo 2012
TLOCI	Template LOCI	Marois 2014
MLOCI	Matched LOCI	Wahhaj 2015
SADI	SDI+ADI	Rameau 2015

Diversity

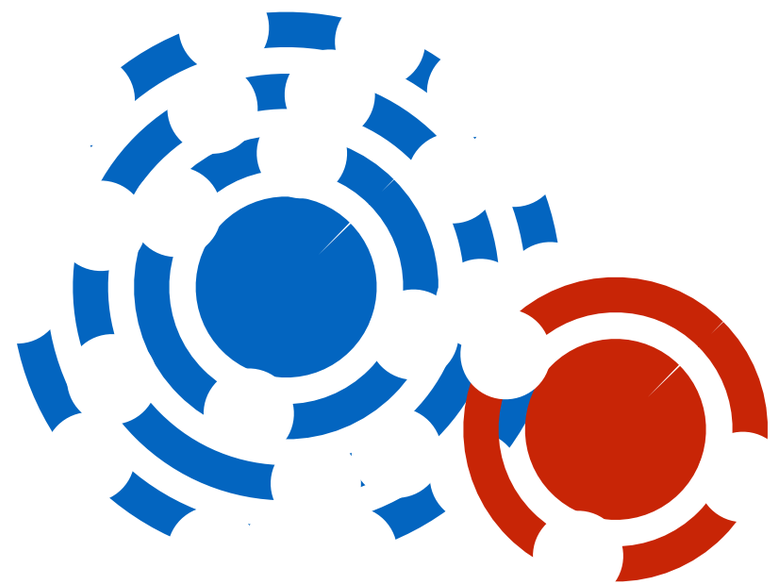


I_1 I_2 I_3 $\cdots$

$$I_n \text{ where } n = 1, 2, 3, ..., N$$

Angular Diversity

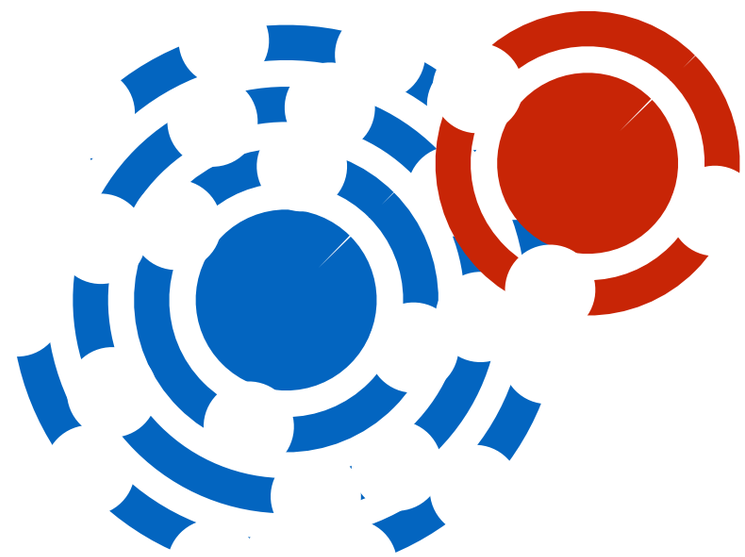
$$I_n = I(\theta_n, t_n)$$



The telescope optics are fixed with respect to the science detector and the sky rotates around

Angular Diversity

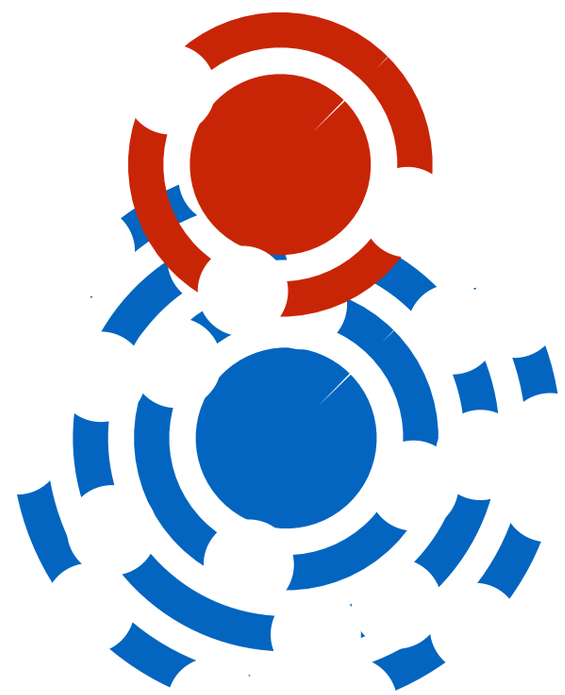
$$I_n = I(\theta_n, t_n)$$



The telescope optics are fixed with respect to the science detector and the sky rotates around

Angular Diversity

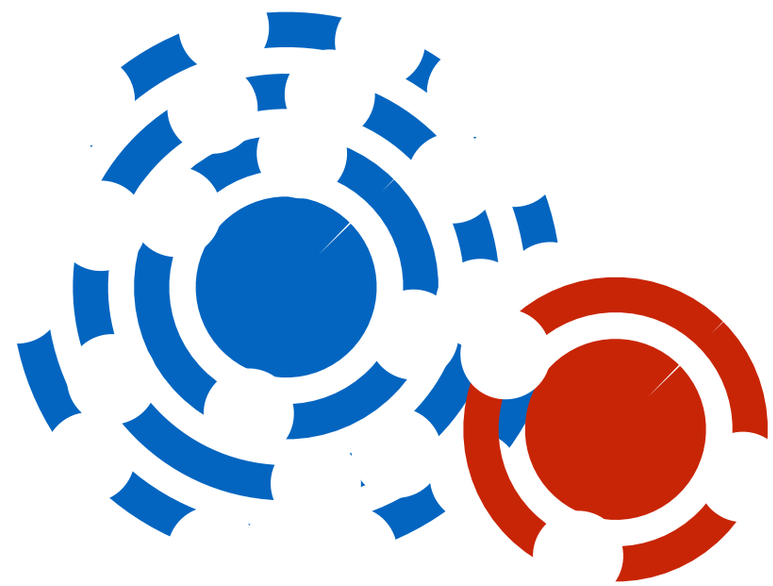
$$I_n = I(\theta_n, t_n)$$



The telescope optics are fixed with respect to the science detector and the sky rotates around

Spectral Diversity

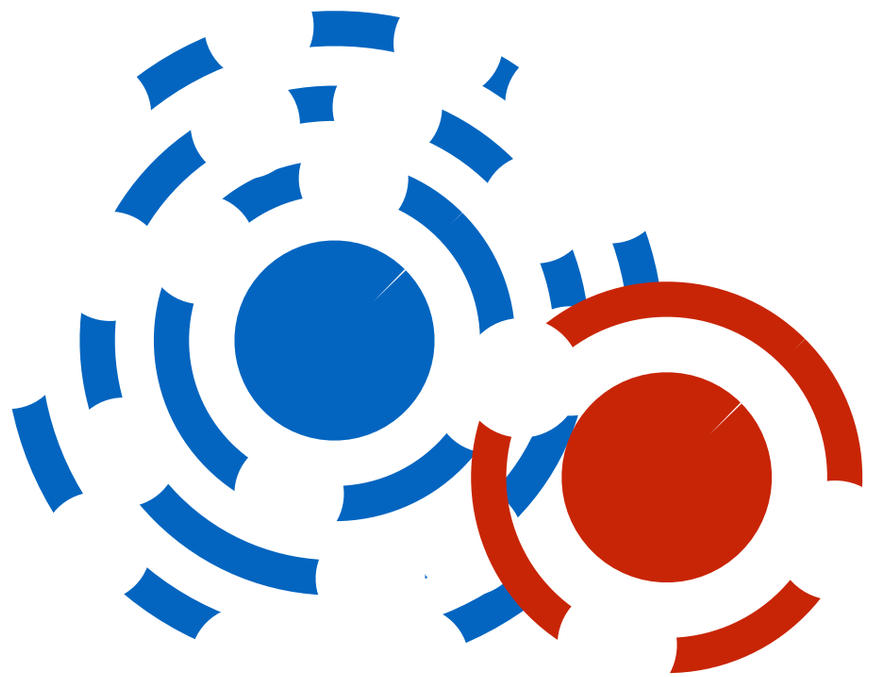
$$I_1 = I(\lambda_1)$$



PSF scales as $\frac{\lambda}{D_{tel}}$ but the planet remains in the same position

Spectral Diversity

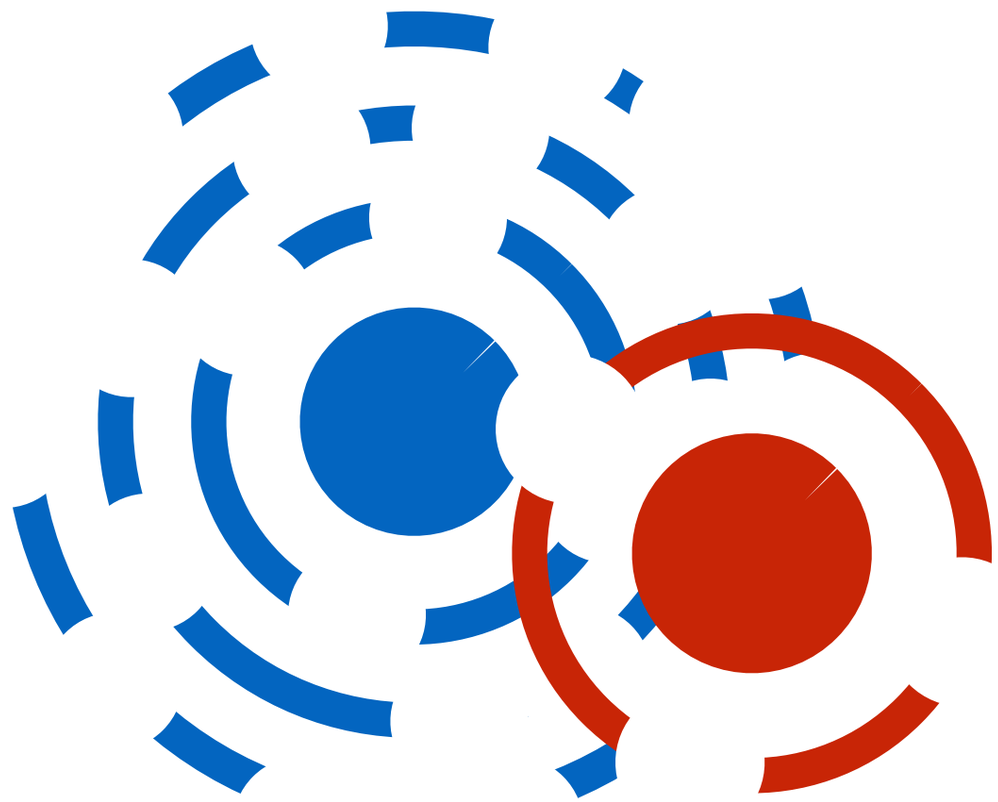
$$I_2 = I(\lambda_2)$$



PSF scales as $\frac{\lambda}{D_{tel}}$ but the planet remains in the same position

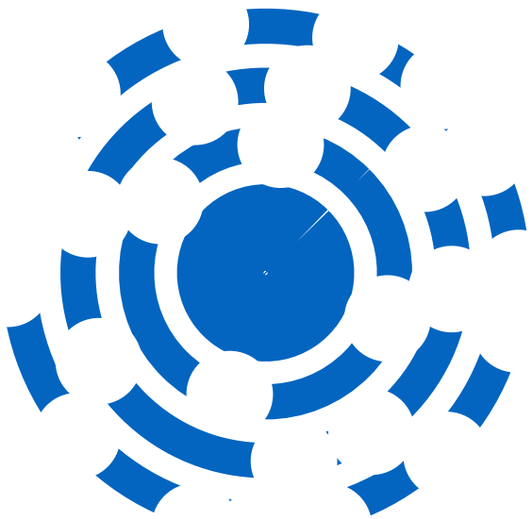
Spectral Diversity

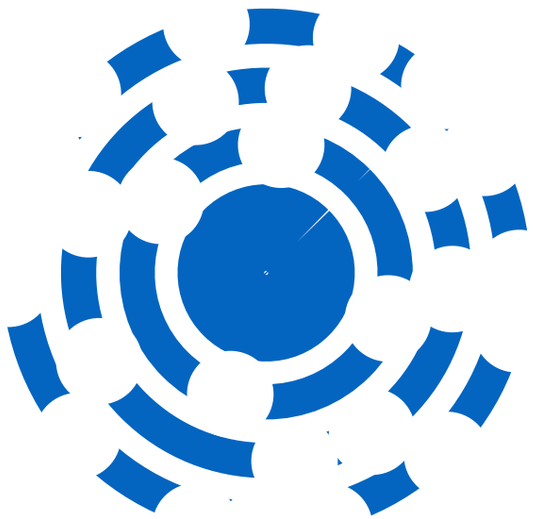
$$I_n = I(\lambda_n)$$

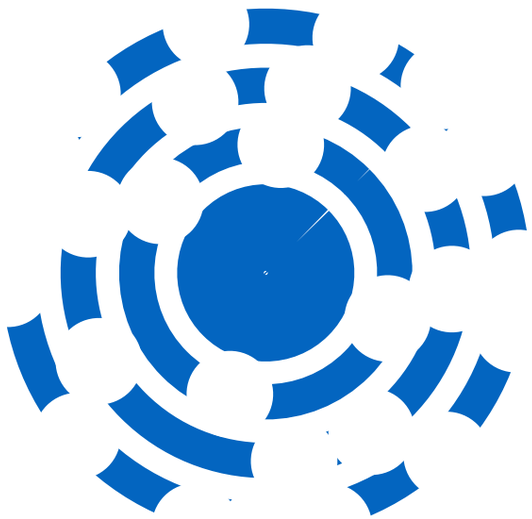


PSF scales as $\frac{\lambda}{D_{tel}}$ but the planet remains in the same position

PSF Library







$I_1 = I(\text{Star 1})$ $I_2 = I(\text{Star 2})$ $I_3 = I(\text{Star 3})$ $\cdots$

Use other stars in the same field of view
AND/OR in the same night

Algorithms

We want the science PSF for all images m

$I_{(m,\text{science PSF})}$ **for** $m = 1, 2, 3, ..., N$

…but that doesn't exist as there's a planet/ disk in all the images!

We approximate by linearly combining all the PSF images and the challenge is to find the best coefficients so that

$$I_{(m,\text{science PSF})} \approx I_{(m,\text{PSF estimate})}$$

$$I_{(m,\text{PSF estimate})} = a_{(1,m)}.I_1 + a_{(2,m)}.I_2 + a_{(3,m)}.I_3 + ...$$

A linear combination of all the PSFs

$$I_{(m,\text{science PSF})} \approx I_{(m,\text{PSF estimate})}$$

where

$$I_{(m,\text{PSF estimate})} = a_{(1,m)}.I_1 + a_{(2,m)}.I_2 + a_{(3,m)}.I_3 + ...$$

...or more compactly....

$$I_{(m,\text{PSF estimate})} = \sum_{N}^{n=1} a_{(n,m)}.I_n$$

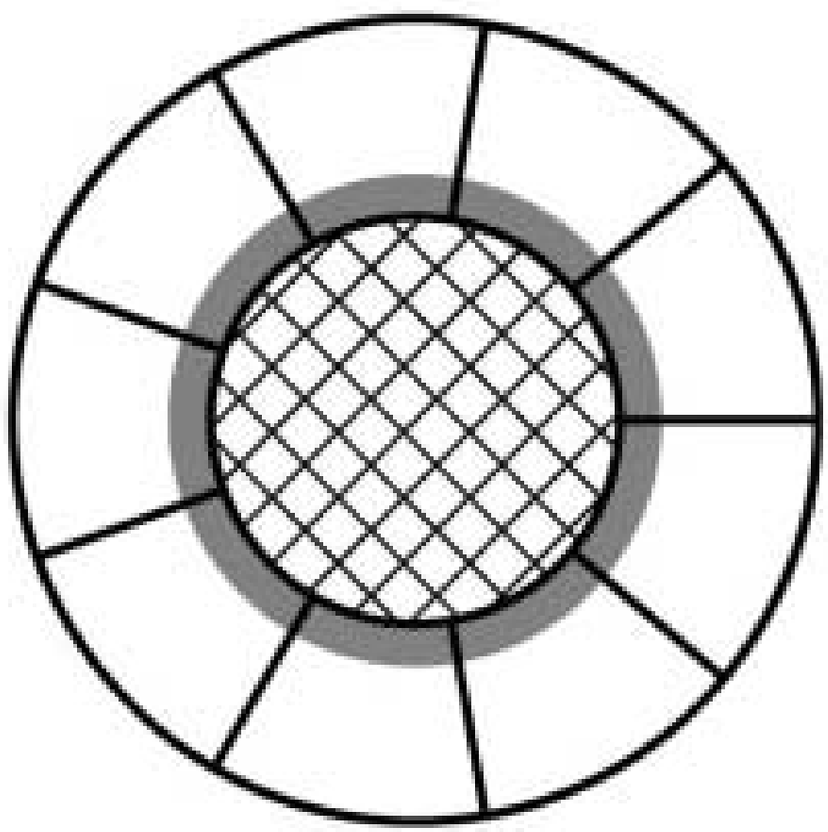
We need to determine all the values of $a_{(n,m)}$

Locally Optimised Combination of Images (LOCI)

Lafreniere et al. (2007)

PSF is cut into small radial and azimuthal wedges

A linear combination of all the science PSFs is chosen to minimise the R.M.S. within a small area

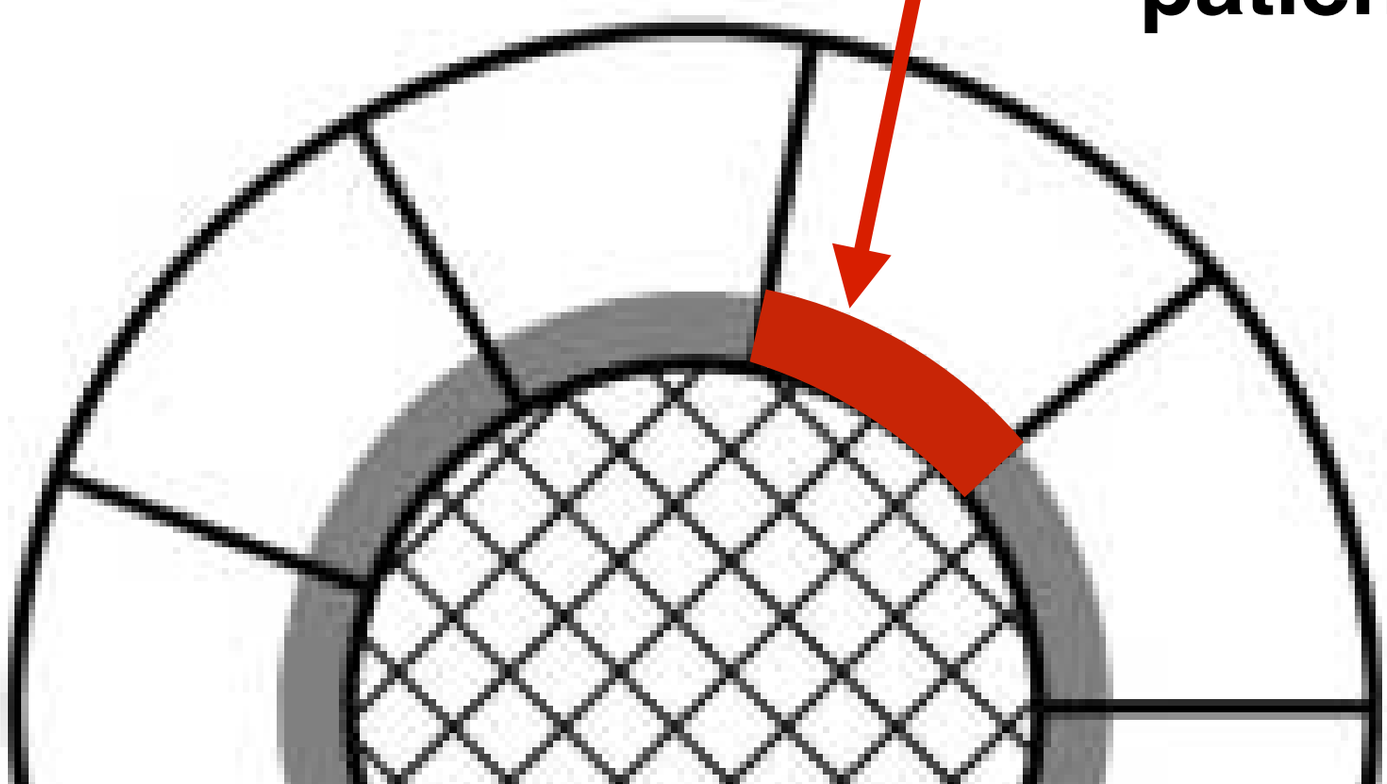


Example of 9 wedges at a given radius around a central star

LOCI

For each wedge subsection S^T

Number of wedge subsections limited by computer power and your patience in doing this!



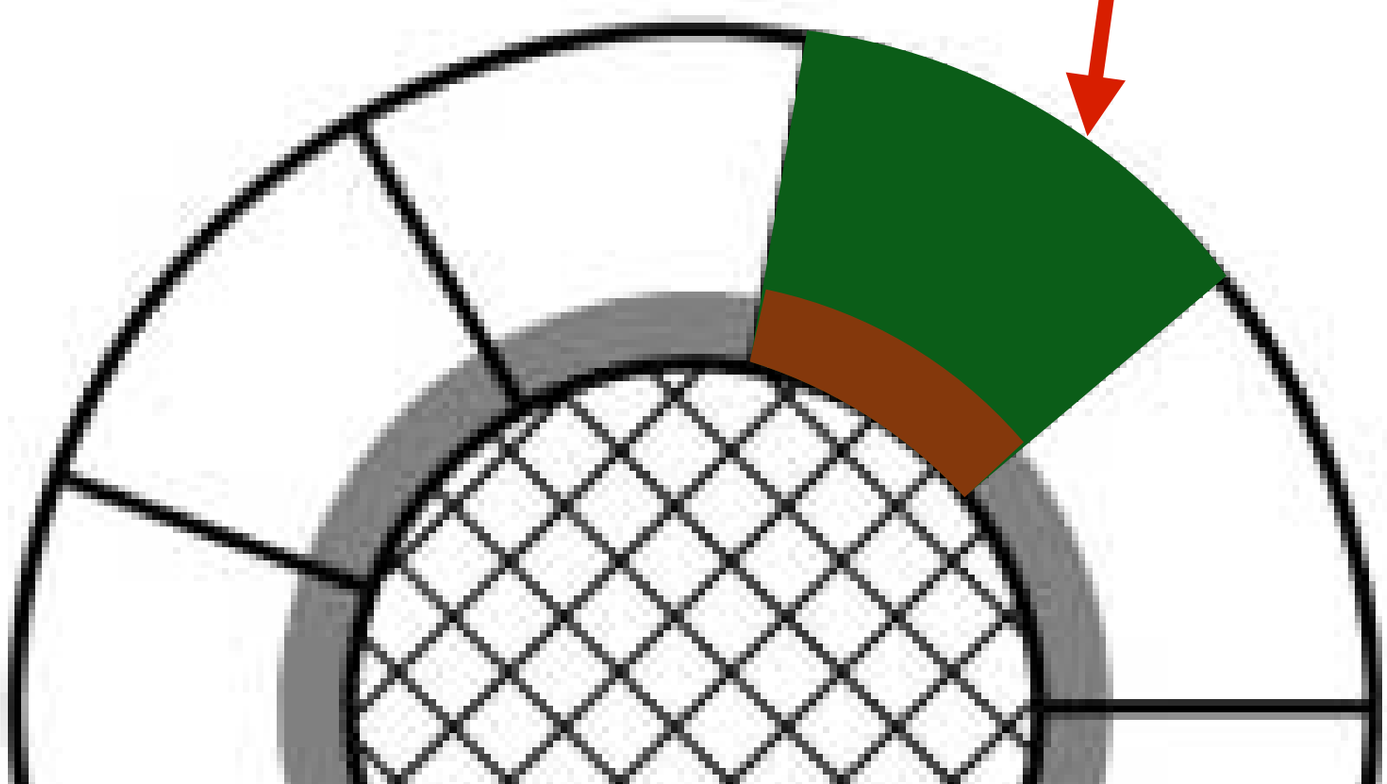
LOCI

and Optimisation subsection O^T

$$A = N_A \pi \left(\frac{W}{2}\right)^2, \tag{1}$$

where W is the full width at half-maximum (FWHM) of the PSF; N_A thus corresponds to the number of "PSF cores" that fit in the optimization subsection.

Size of O^T is determined by how many diffraction patches can fit in it - minimises the self-subtraction problem



Linear combination

You determine what a coefficients will minimise

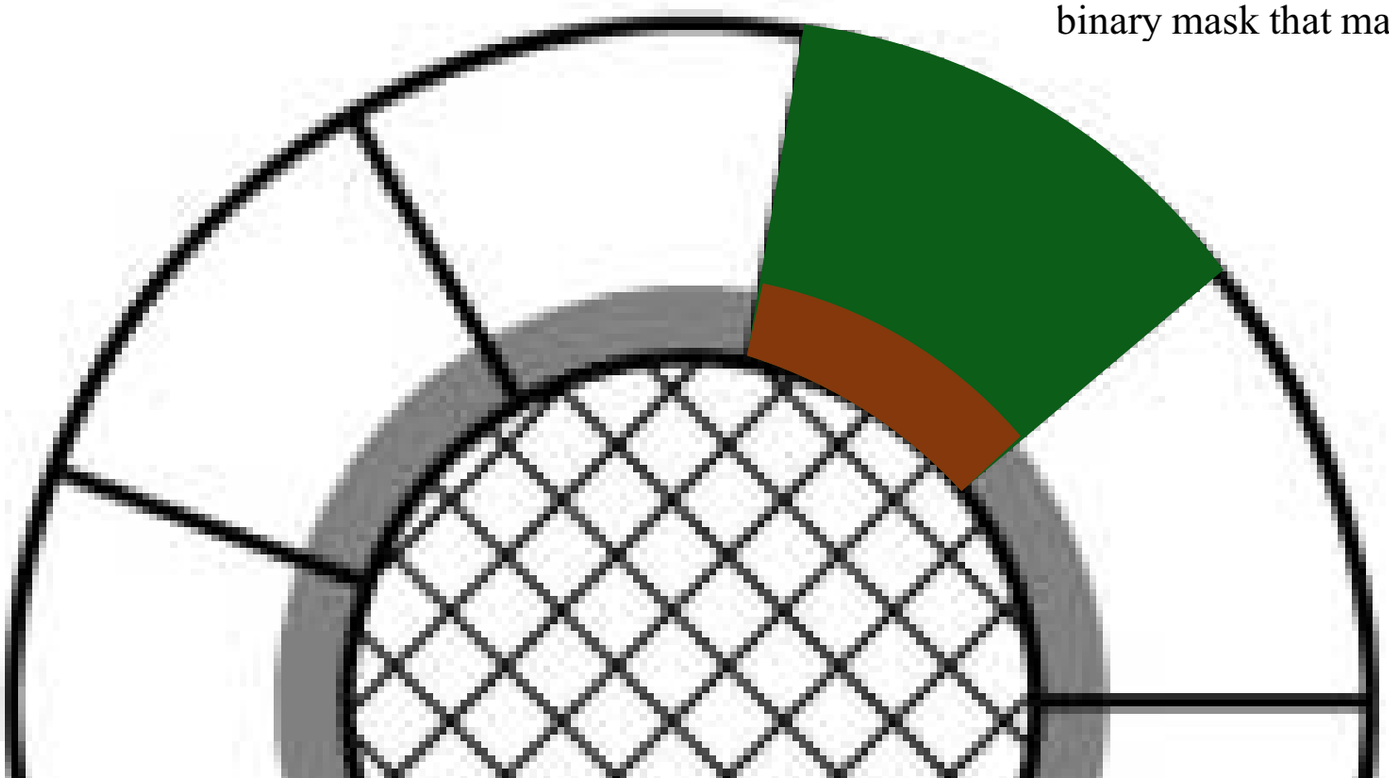
The reference PSF for the optimization subsection is then constructed according to

$$O^R = \sum_{k \in K} c^k O^k, \tag{3}$$

where the coefficients c^k are to be determined by the algorithm. They are computed by minimizing the sum of the squared residuals of the subtraction of O^R from O^T, which is given by

$$\sigma^2 = \sum_i m_i \left(O_i^T - O_i^R\right)^2 = \sum_i m_i \left(O_i^T - \sum_k c^k O_i^k\right)^2, \tag{4}$$

where i denotes a pixel in the optimization subsection and m is a binary mask that may be used to ignore some pixels. The quan-



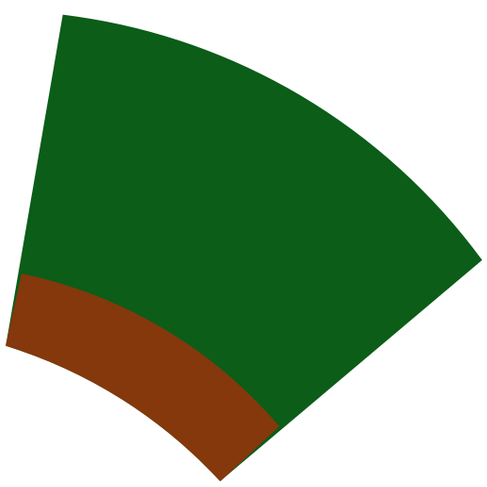
Multiple parameters to “tune up”

TABLE 1

PARAMETER VALUES USED FOR OPTIMIZATION

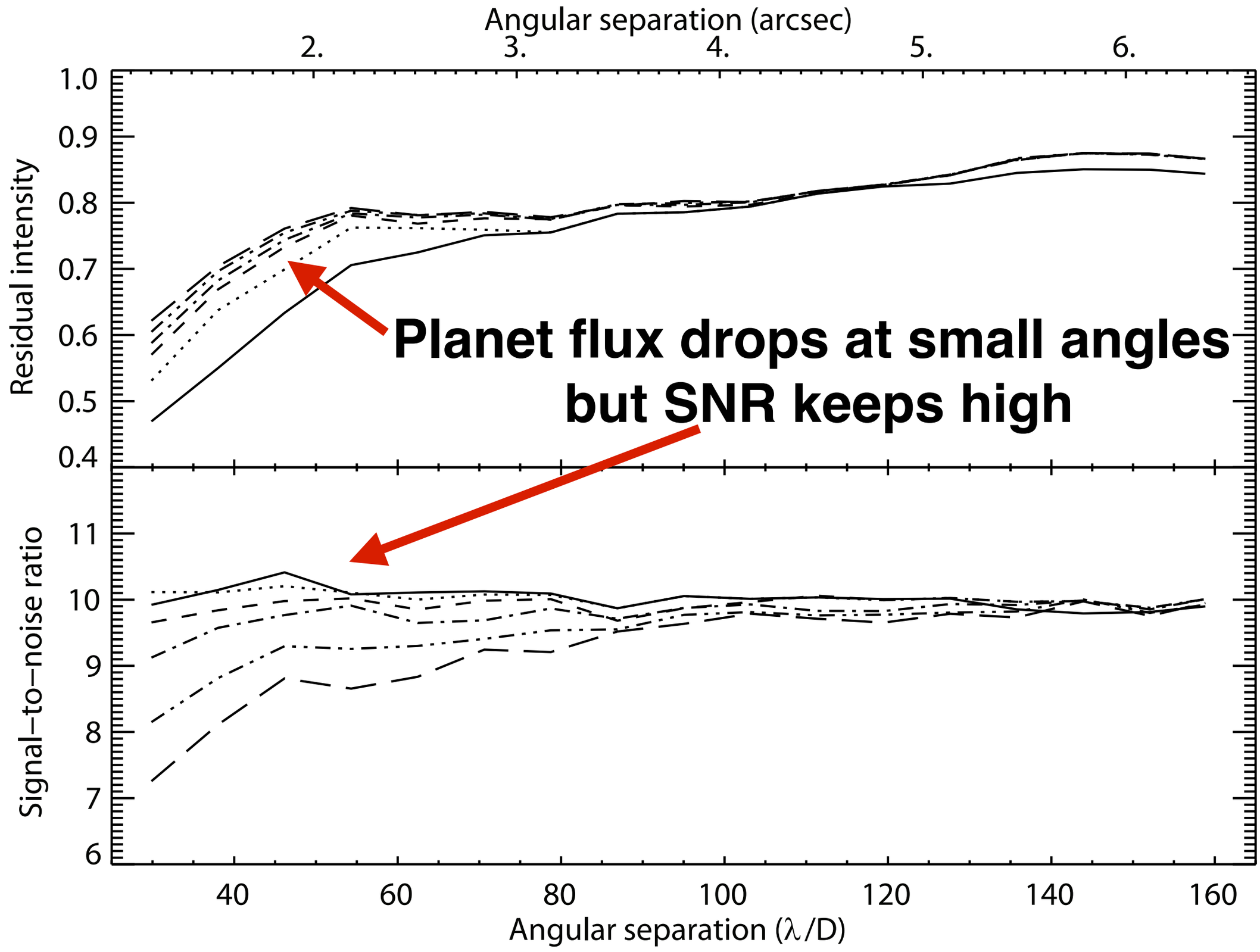
Parameter	Trial Values	Adopted Value	
N_δ	0.25, 0.5, 0.75, 1.0, 1.5, 2.0	0.5	**FWHM shift**
N_A	50, 100, 150, 300, 500	300	**# of FWHM**
g.....	0.5, 1.0, 2.0	1.0	**ratio of width to height**
dr	1.5, 3, 6, 9, 15, (1.5–15)[a]	(1.5–15)[a]	**Width of annuli**

[a] We use $dr = 1.5$ for separations less than $60\lambda/D$ and $dr = 15$ for larger separations.

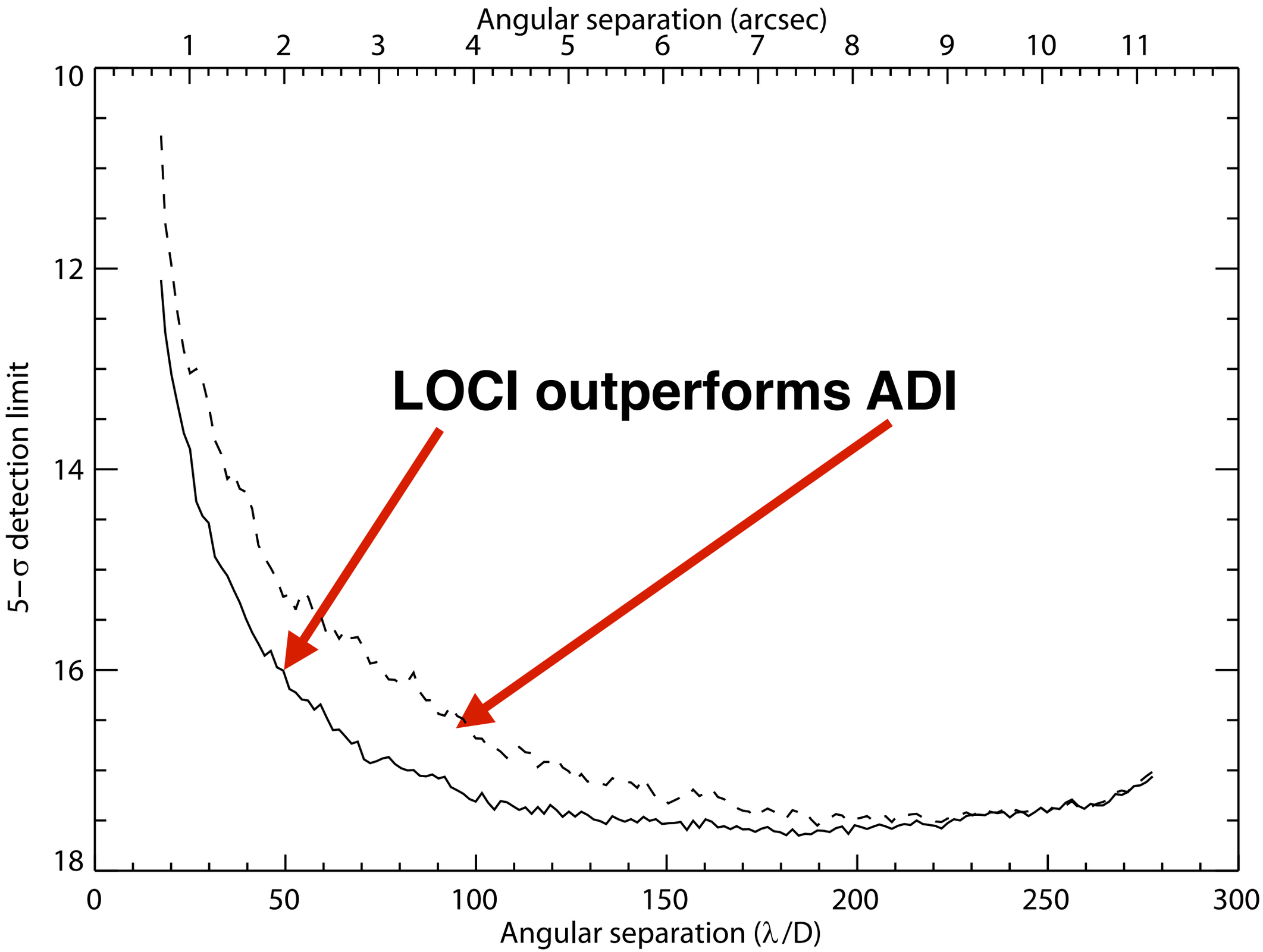


LOCI has several parameters that need to be optimised for each data set and for each planet radial distance. This is a BIG parameter space to explore…..

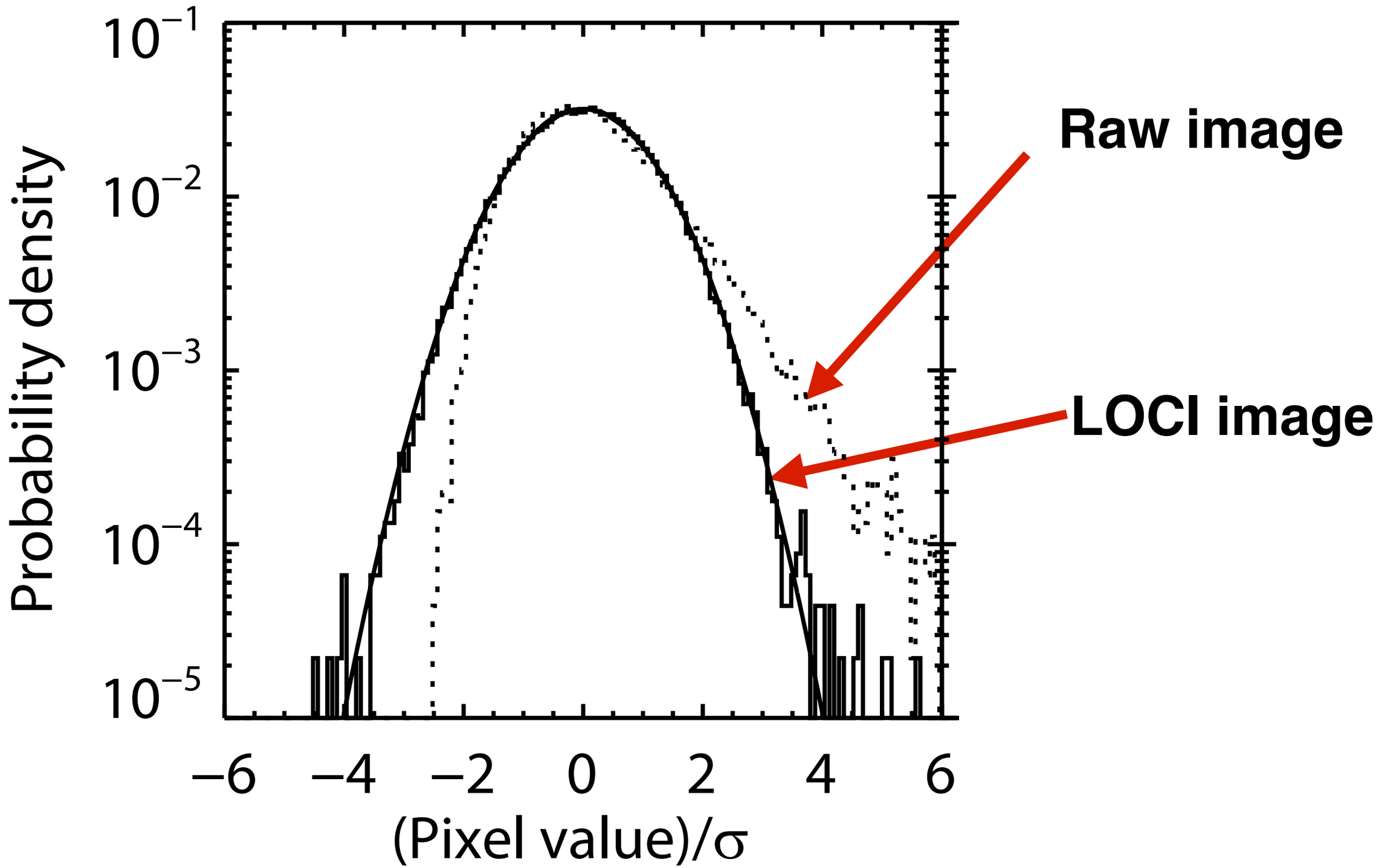
Self-subtraction



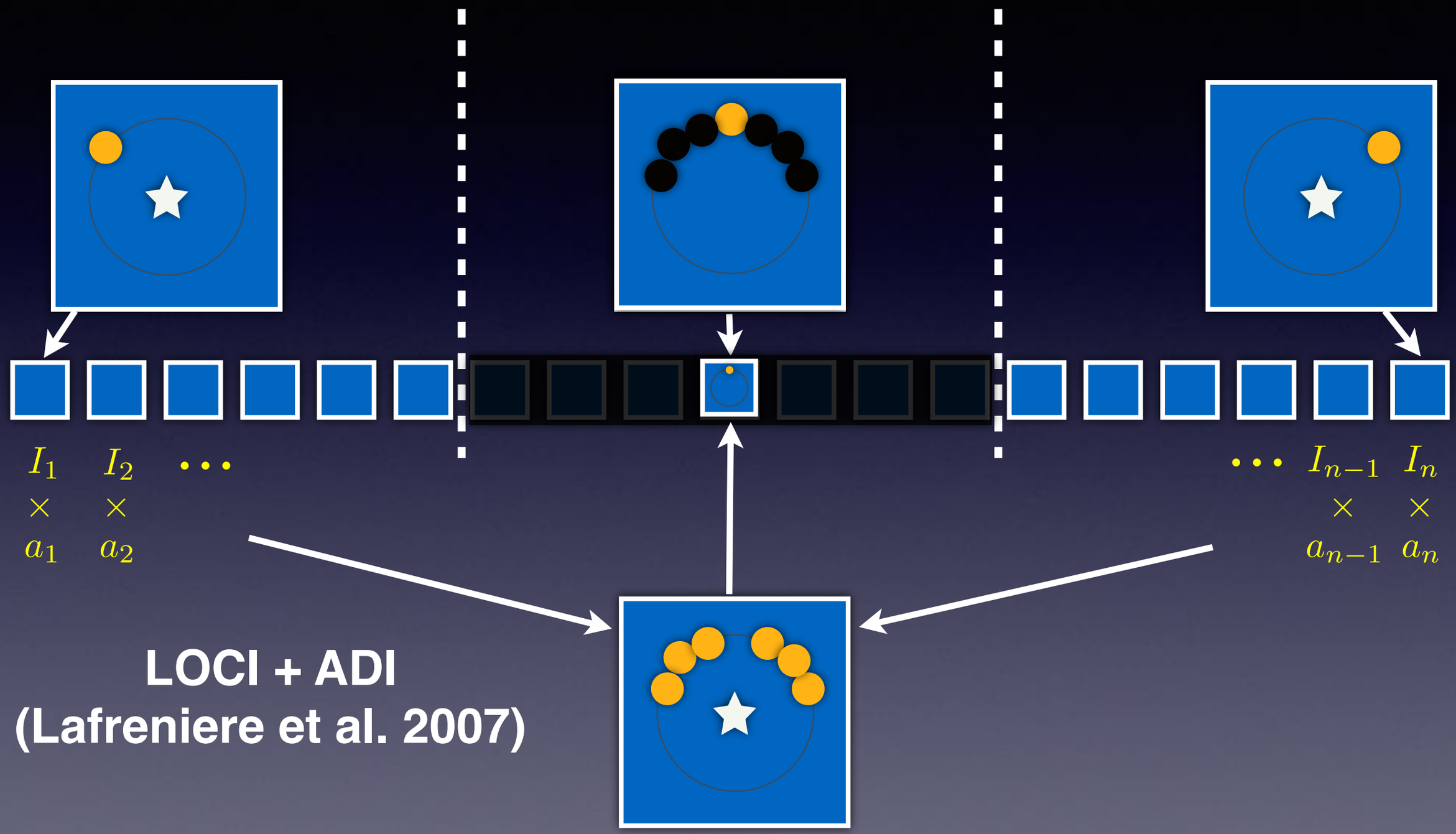
LOCI gain over ADI



Statistical distribution of LOCI pixels is closer to Gaussian



Approximating the Science PSF



LOCI + ADI
(Lafreniere et al. 2007)

PynPoint / KLIP

Amara and Quanz 2012 / Soummer et al. 2012

Any science image can be thought of as a linear combination of an orthogonal basis set formed from all the science images.

$$I(\vec{x}) = \sum a_i \phi_i(\vec{x}), \tag{1}$$

where $I(\vec{x})$ is the image of the PSF, $\phi(\vec{x})$ is a given basis and a_i is the coefficient for each basis function.

Instead of small wedges, the whole stack of images is taken and a Principal Component Analysis (PCA) is performed on it.

Singular Value Decomposition (SVD)

Take stack of input images, and subtract off the mean from all of them, then form a 2-D array S where each row i is the unravelled version of image i.

means that $\mathbf{S}$ has dimensions $\mathbf{M} \times \mathbf{N}$, where $\mathbf{N}$ is the number of pixels in an image and $\mathbf{M}$ is the number of images in a stack. We calculate the SVD such that

$$\mathbf{S} = \mathbf{U}\mathbf{W}\mathbf{V}^{\mathbf{T}}, \tag{4}$$

where $\mathbf{W}$ is a diagonal matrix with positive (or zero) elements. In this decomposition, $\mathbf{V}$ is a matrix containing the PCA elements that form an orthogonal basis set ($\mathbf{U}$ and $\mathbf{V}$ are column-orthogonal matricies).

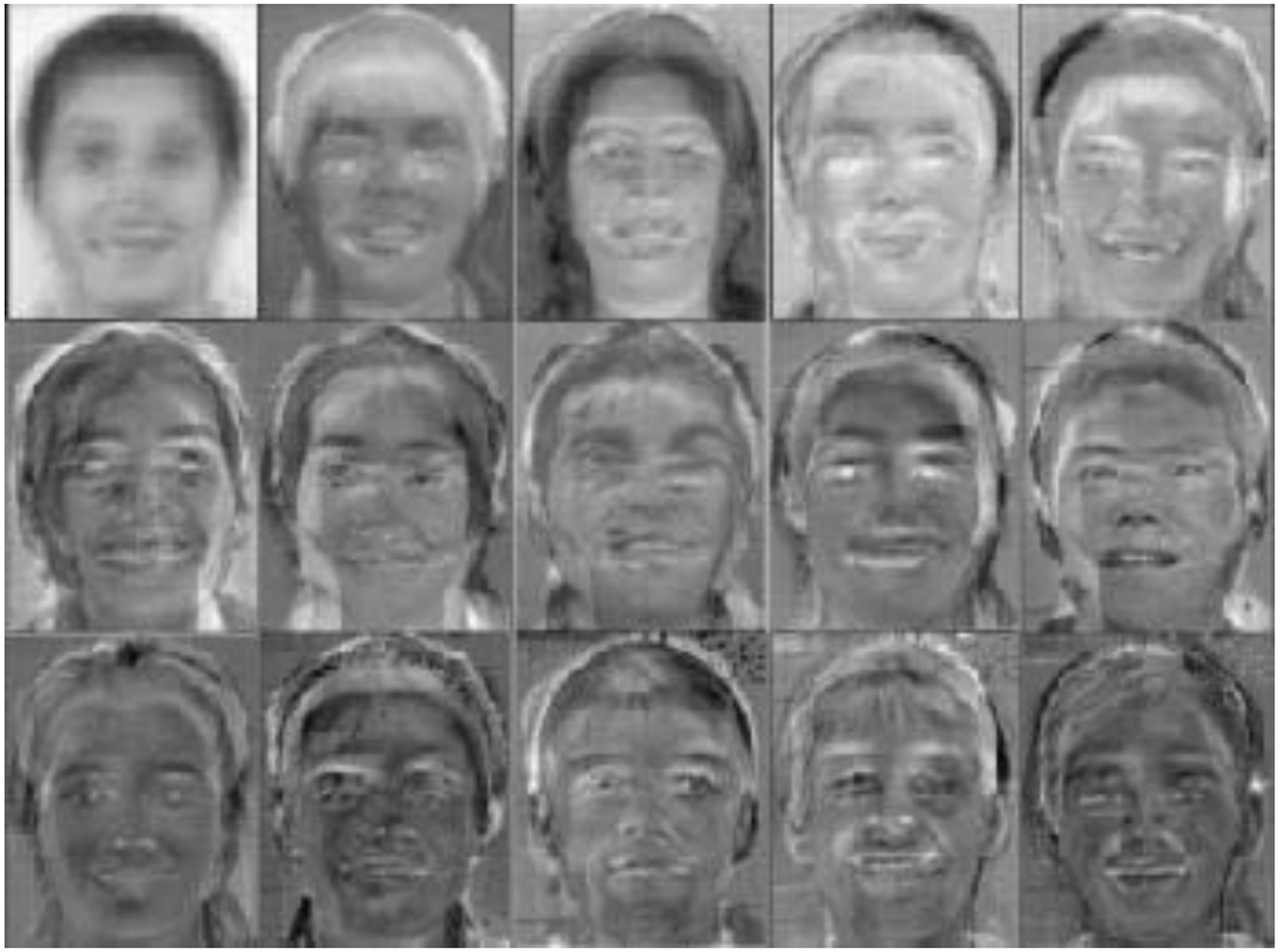
SVD example

Input is a set of images of faces:

http://www.eos.ubc.ca/research/cdsst/Tad_home/eigenfaces.html

Produce orthogonal eigenmodes

After SVD, output looks like this:



http://www.eos.ubc.ca/research/cdsst/Tad_home/eigenfaces.html

eigenfaces!

Can now use the eigenfaces and linearly fit them to any of the original data using just a few coefficients

http://www.eos.ubc.ca/research/cdsst/Tad_home/eigenfaces.html

PynPoint / KLIP

Amara and Quanz 2012 / Soummer et al. 2012

Now linearly fit each image with just a few of the lowest PCA components (typically 2 to 10)

$$I(\vec{x}) = \sum a_i \phi_i(\vec{x}), \tag{1}$$

where $I(\vec{x})$ is the image of the PSF, $\phi(\vec{x})$ is a given basis and a_i is the coefficient for each basis function.

PynPoint

Amara and Quanz 2012