Lecture 11: Spectrographs

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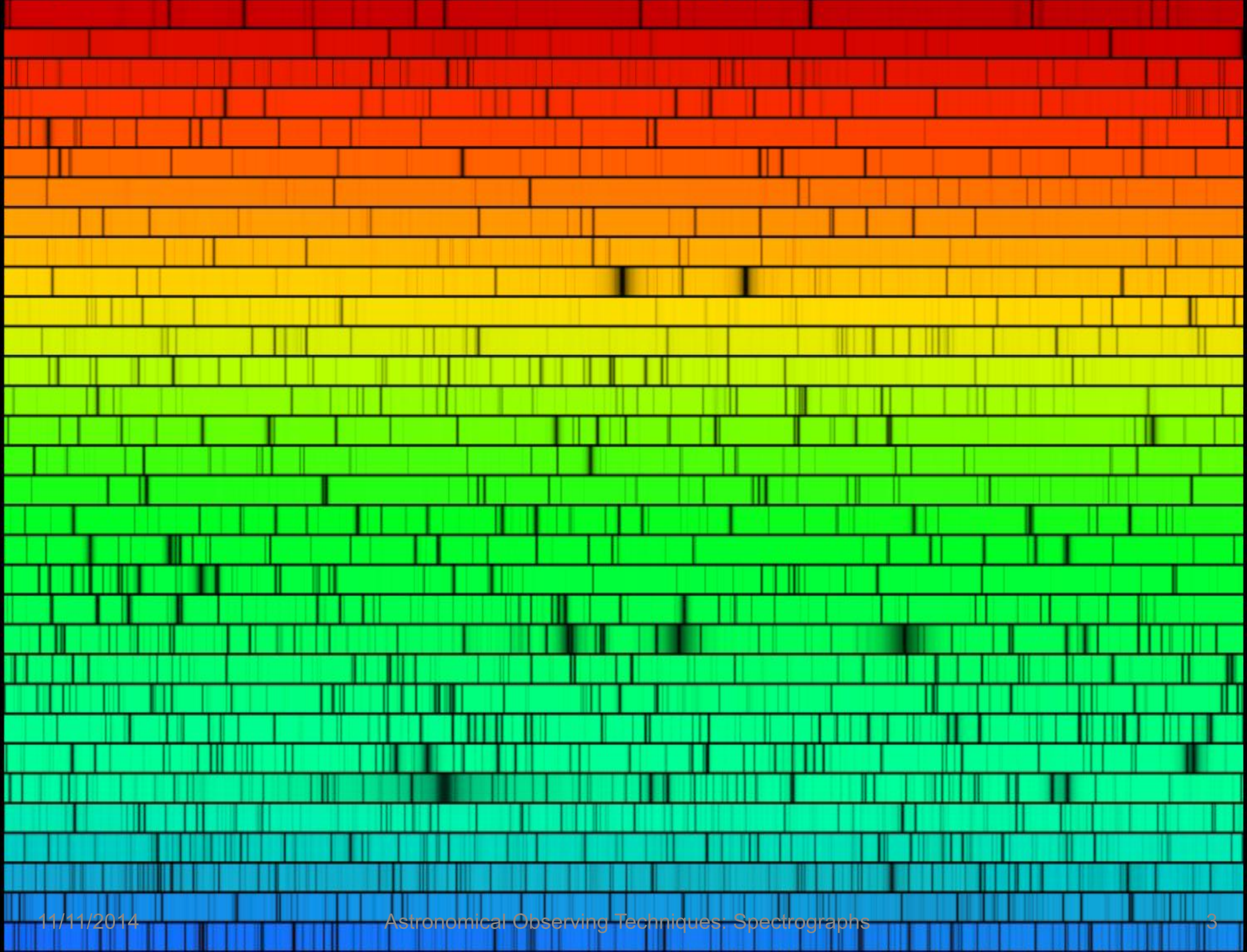
Overview

1. Spectral Lines
2. Spectrograph Concept
3. Grating Spectrograph
4. Grisms
5. Filters and Fabry-Perots
6. OH Suppression Spectrographs
7. Multi-Object Spectrographs
8. Fourier Transform Spectrometer

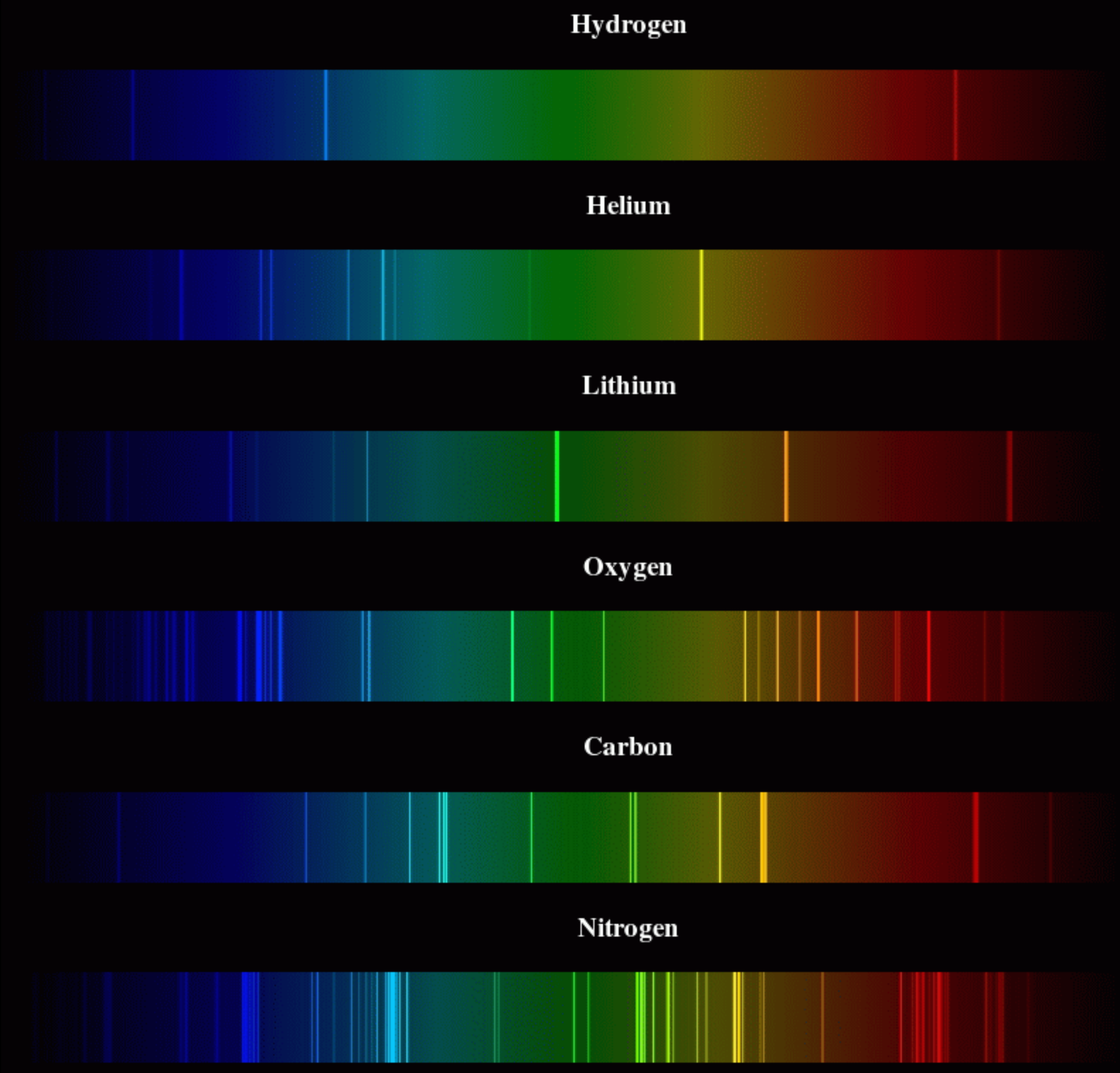


Continuous, Emission, Absorption Spectra

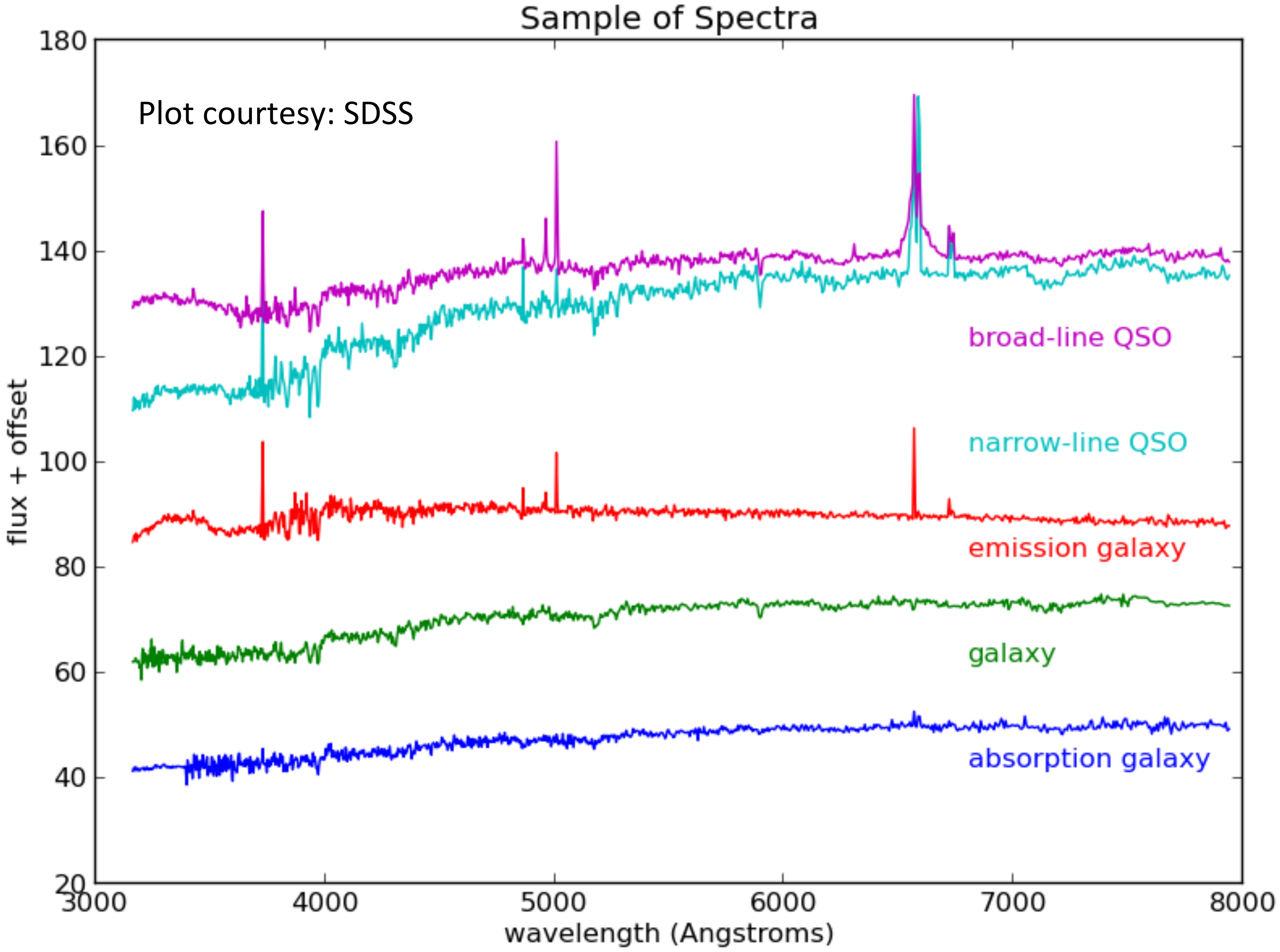
Continuous spectrum

Emission line spectrum

Absorption line spectrum

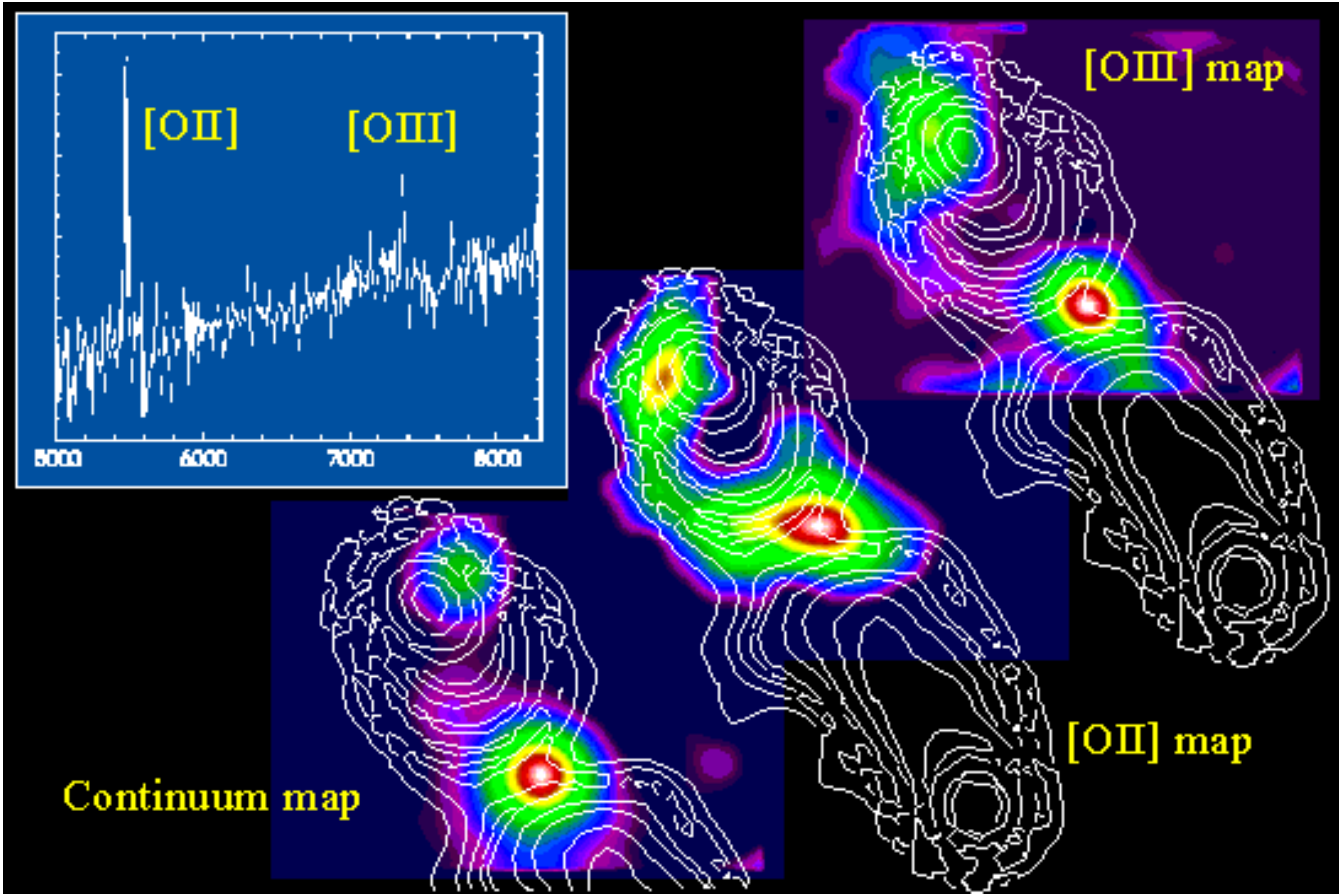


Courtesy:
http://home.achilles.net/~ypvsj/data/elements/index.html



Plot courtesy: SDSS

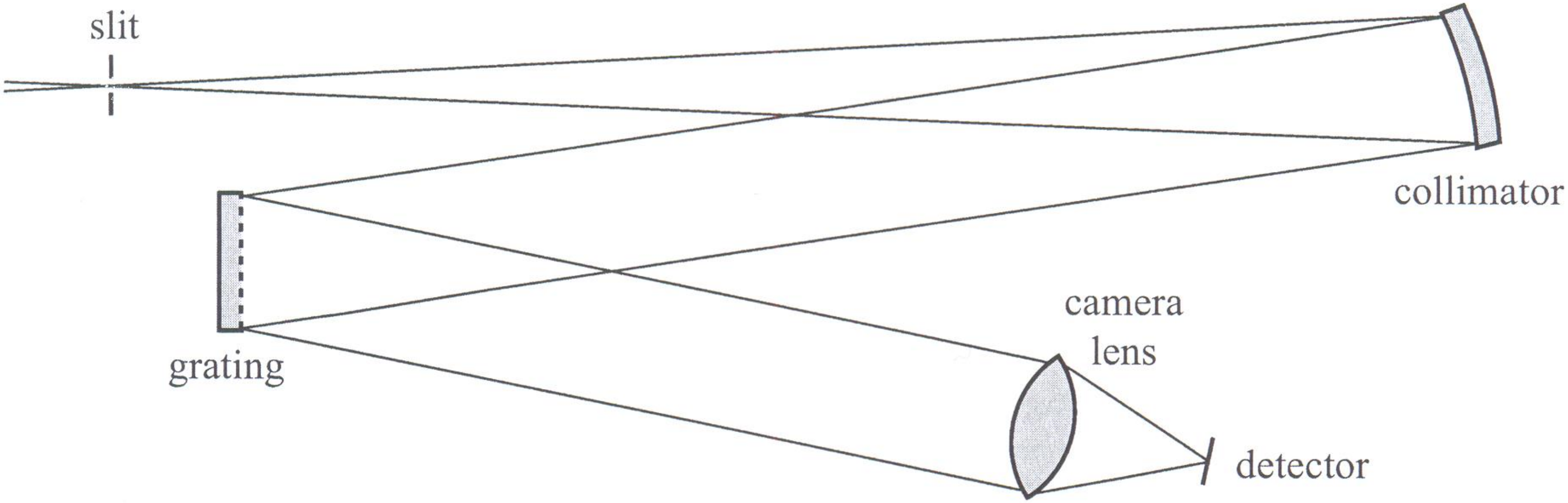
Spectral Line Maps



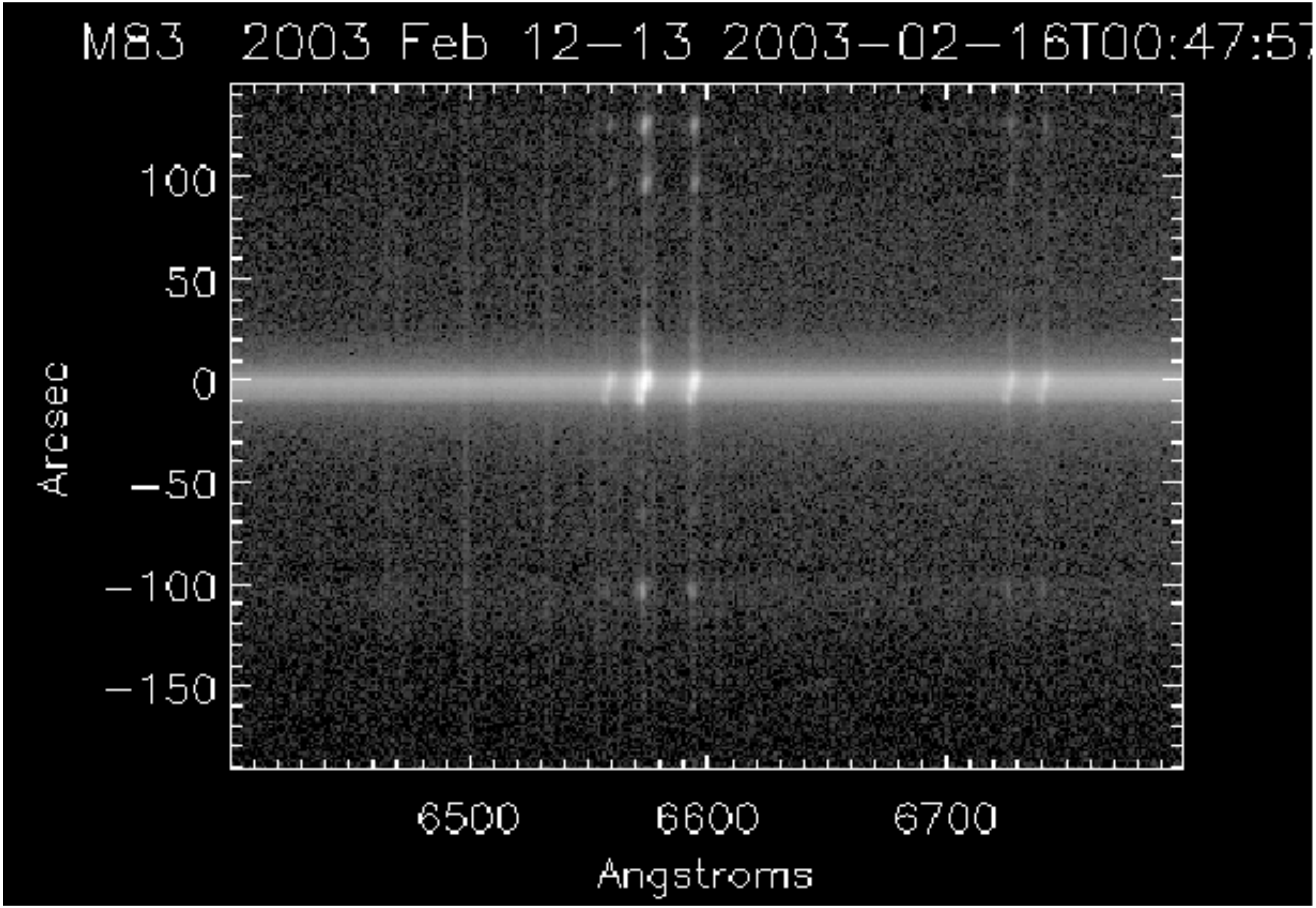
Radiogalaxy 3C435A, Plot courtesy: Universite de Lyon, Recent TIGER Scientific Results

Optical Spectrograph Components

1. Slit: reduce telescope image to one dimension
2. Collimator: collimate (make parallel) diverging light
3. Disperser: spectrally disperses the light
4. Camera: focus spectrum onto detector



Long Slit Spectrum



Main Characteristics of Spectrograph

- Spectral resolution element: Δλ
- Spectral resolution (or resolving power): R=λ/Δλ
- Instrumental profile P(λ) broadens a theoretically infinitely narrow line to the observed line width:

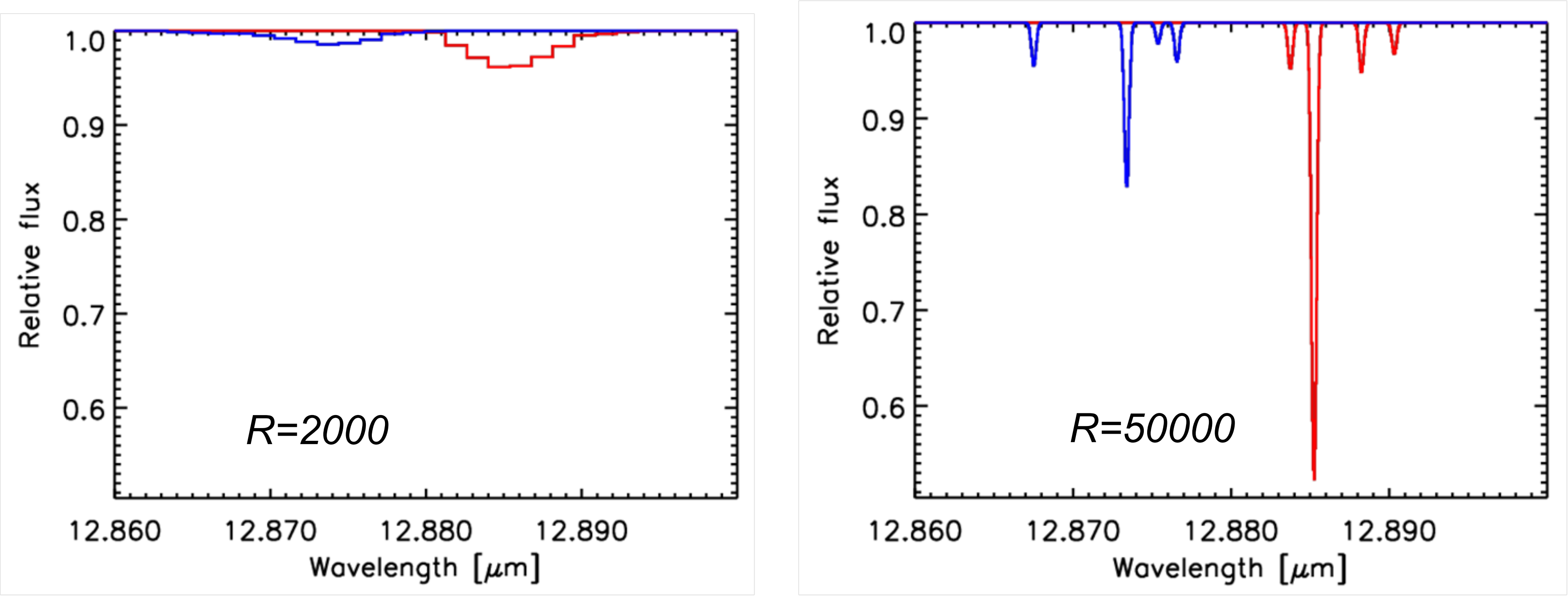
$$I_0(\lambda) = \delta(\lambda - \lambda_0) \qquad I(\lambda) = P(\lambda) * I_0(\lambda)$$

- *Usually the instrumental profile determines the spectral resolution element, which is typically Nyquist-sampled*
- Transmission determines the throughput η(λ)

$$\eta(\lambda) = \frac{I_{out}(\lambda)}{I_{in}(\lambda)}$$

Spectral Resolution and S/N

For *unresolved* spectral lines, both the S/N and the line/continuum contrast increase with increasing resolution



Model spectra of C_2H_2 at 900K and HCN at 600K (assumed Doppler broadening ~4 km/s) at different spectrograph resolutions (figure provided by F. Lahuis).

Diffraction Grating

Grating introduces an optical path difference = f(angle to surface normal)

Condition for constructive interference given by grating equation:

$$m\lambda = d \cdot (\sin\alpha \pm \sin\beta)$$

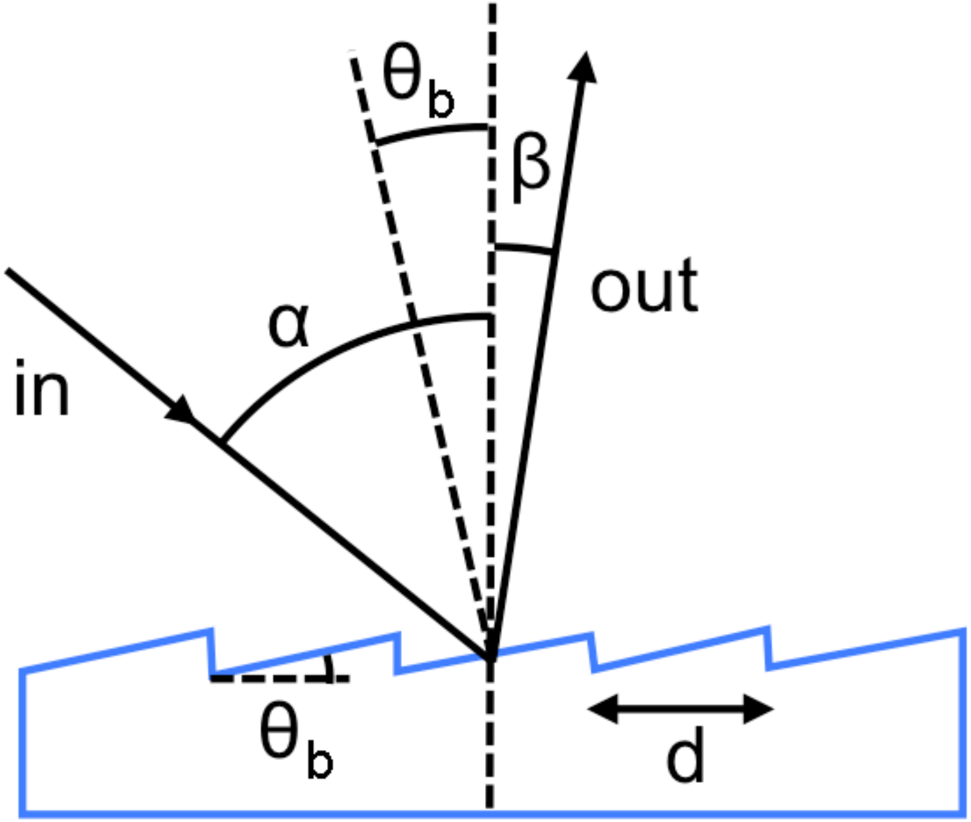
m = order of diffraction

λ = wavelength

d = distance between equally spaced grooves

α = angle of incoming beam

β = angle of reflected beam



Grating Spectral Resolution

- Grating equation $m\lambda = d \cdot (\sin\alpha \pm \sin\beta)$

- Gratings usually in collimated beam close to pupil image

- Maximum spectral resolution R given by R=mN
  N = number of (illuminated) grooves
  m = diffraction order

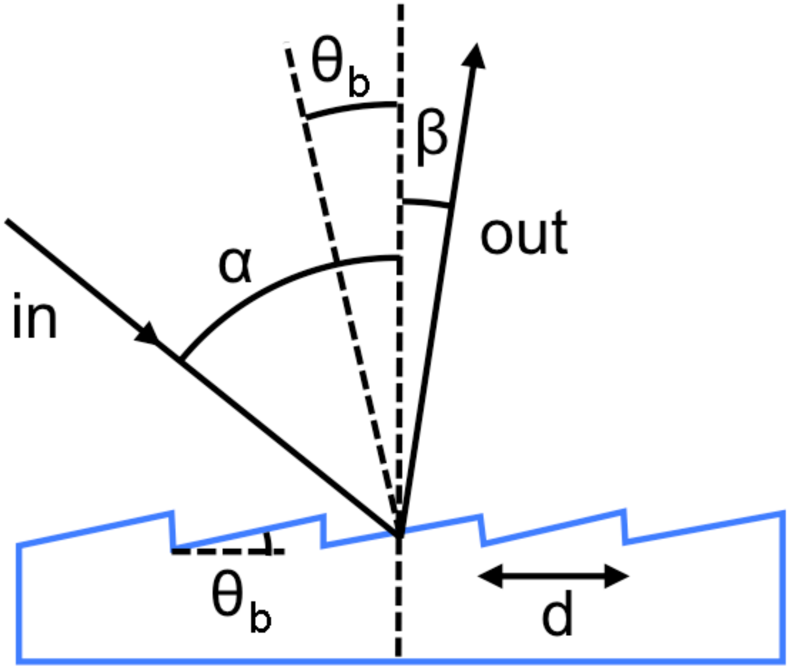
a

- Angular dispersion $d\beta / d\lambda = \dfrac{m}{d\cos\beta}$

Blaze Angle

- Periodic structure distributes energy over many orders *m*.
- Observing only one arbitrary order is inefficient
- For blazed gratings the *directions of constructive interference and specular reflection coincide*:

$$\alpha+\beta=2(\alpha+\theta_B) \Rightarrow \theta_B=\frac{\beta-\alpha}{2}$$



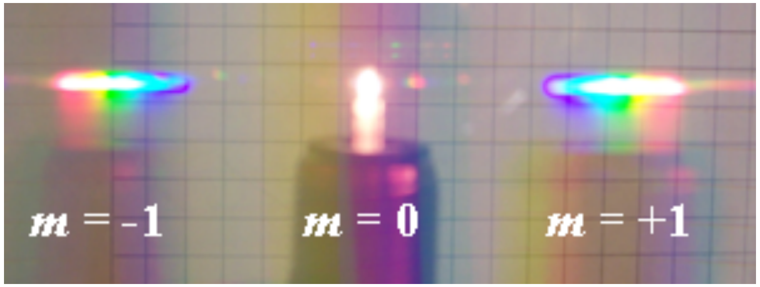
Advantage:

- High efficiency

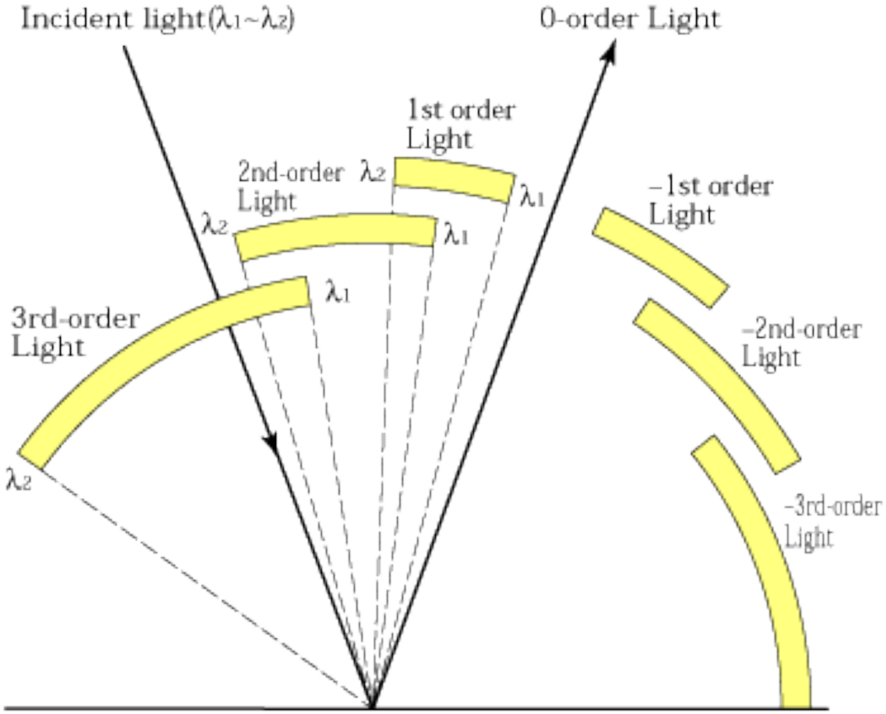
Disadvantage:

- Blaze angle θ_B (and hence blaze wavelength λ_B) are fixed by construction.

Free Spectral Range …



A light bulb seen through a transmissive grating, showing three diffracted orders. m = 0 corresponds to direct transmission; colors with increasing wavelengths (from blue to red) are diffracted at increasing angles. Source: Wikipedia



Different diffraction orders overlap with each other:

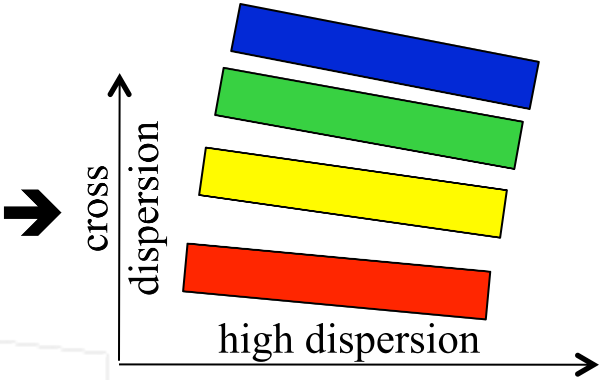
$$m\lambda = d(\sin\alpha + \sin\beta) = (m+1)\lambda'$$

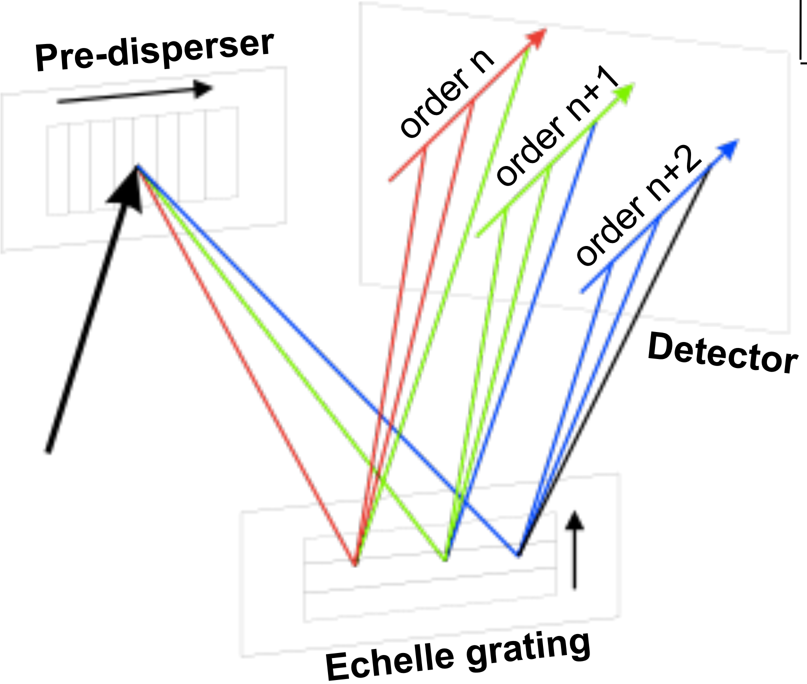
The free spectral range is the largest wavelength range for a given order that does not overlap the same range in an adjacent order.

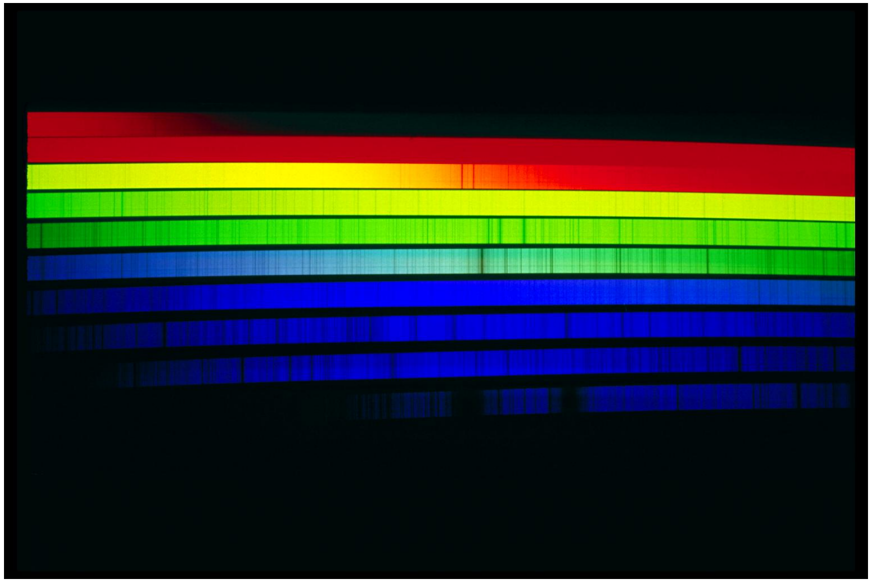
$$\Delta\lambda_{free} = \lambda - \lambda' = \frac{\lambda'}{m}$$

…and Cross-Dispersion

To spatially separate the orders and avoid overlap, an additional optical element will be needed: A low-dispersion prism/grating with a dispersion direction perpendicular to that of the high-dispersion grating







Echelle Gratings

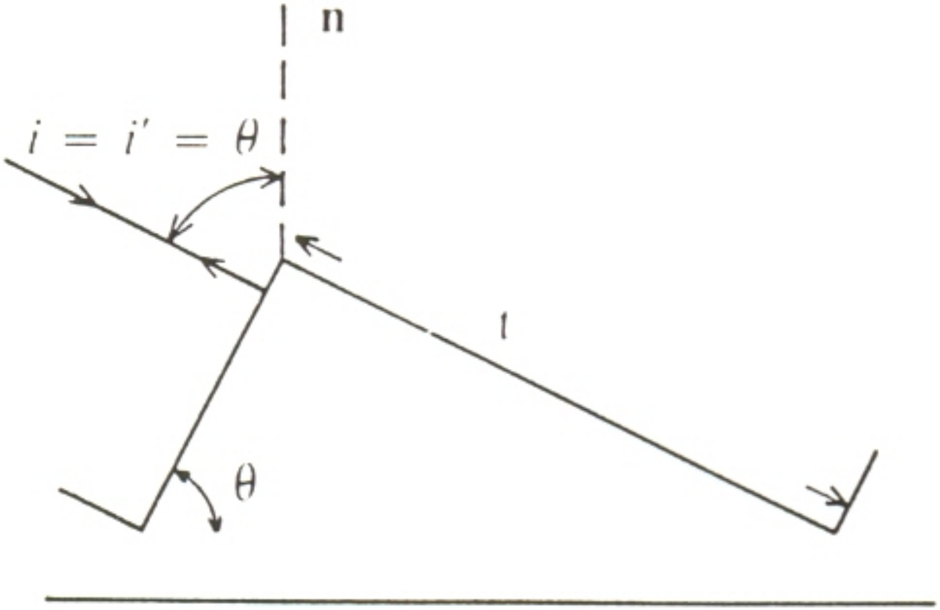
Want high dispersion

$$\frac{d\beta}{d\lambda} = \frac{m}{d\cos\beta} = \frac{\sin\alpha + \sin\beta}{\lambda\cos\beta}$$

and high spectral resolution

$$R = Nm$$

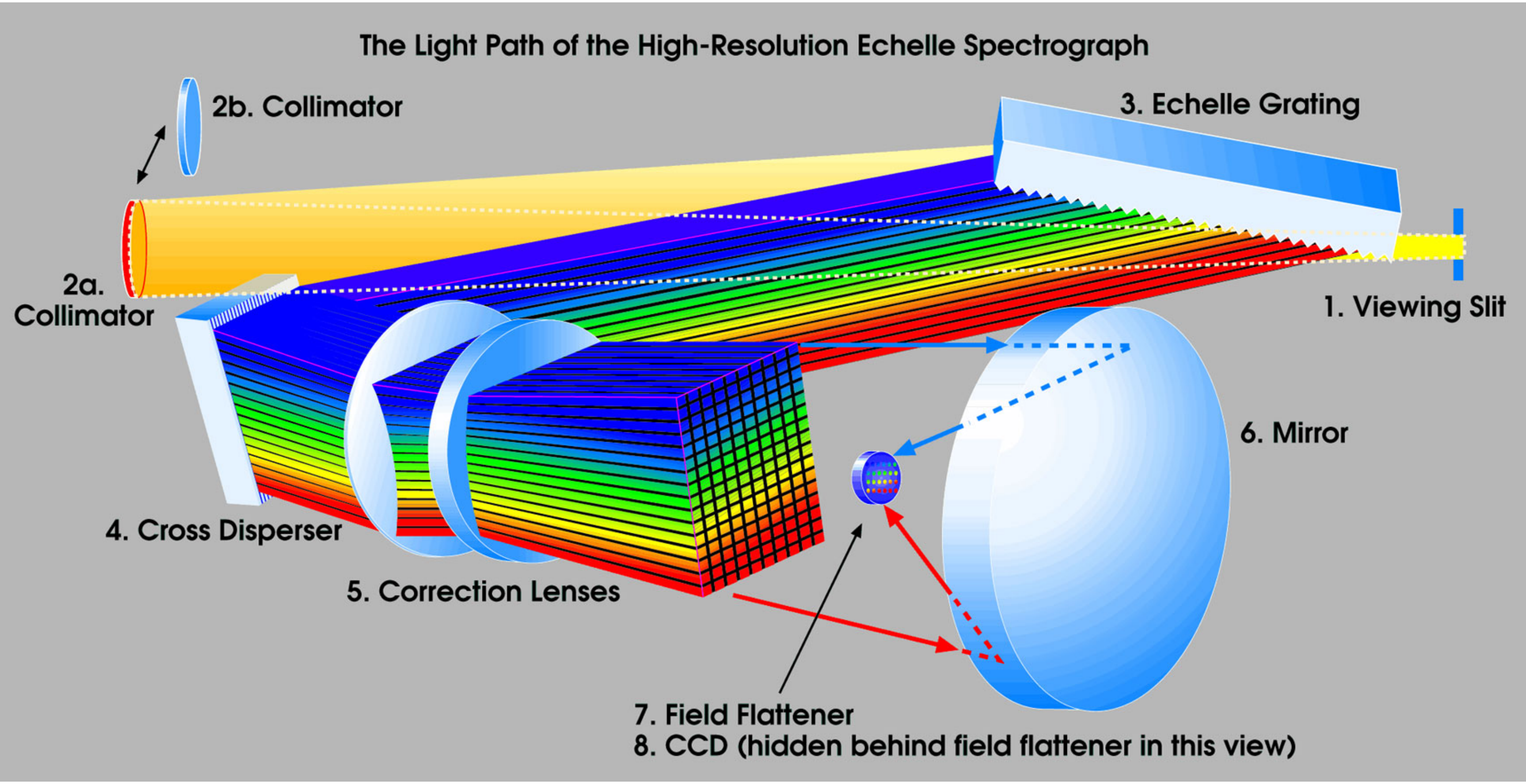
α and β large, high order m (≈ 50), and therefore large a



Grating equation in Littrow configuration (α=β): $m\lambda_B = 2d \sin\beta$

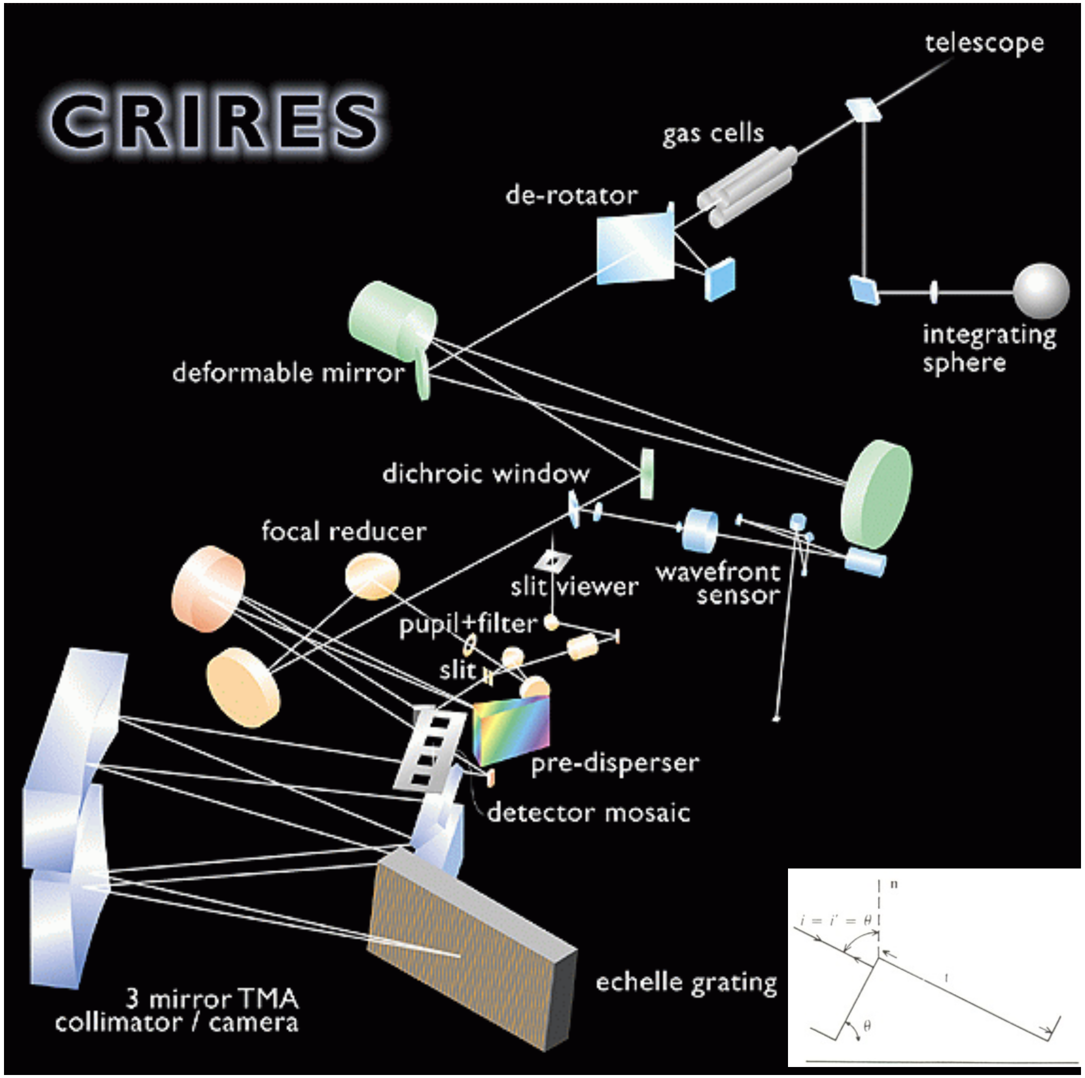
Echelle Spectrograph

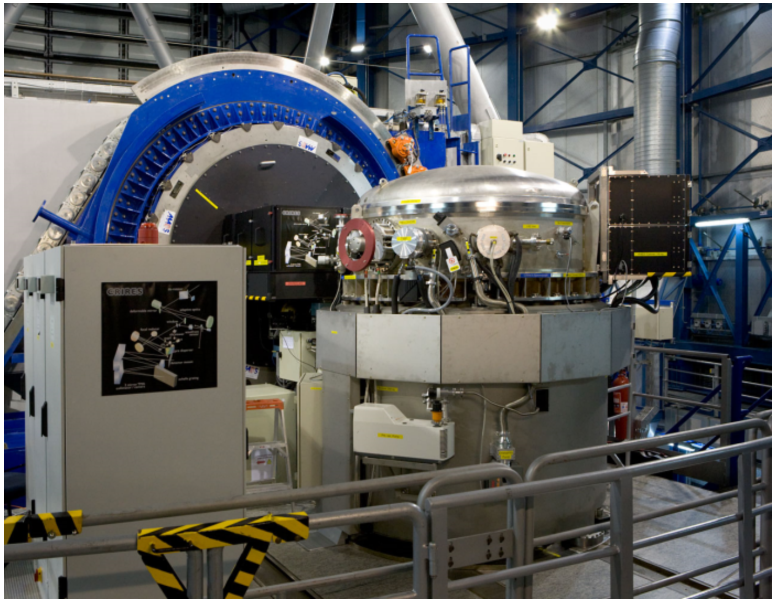
Operation in high order → pre-disperser essential



Echelle Spectrographs

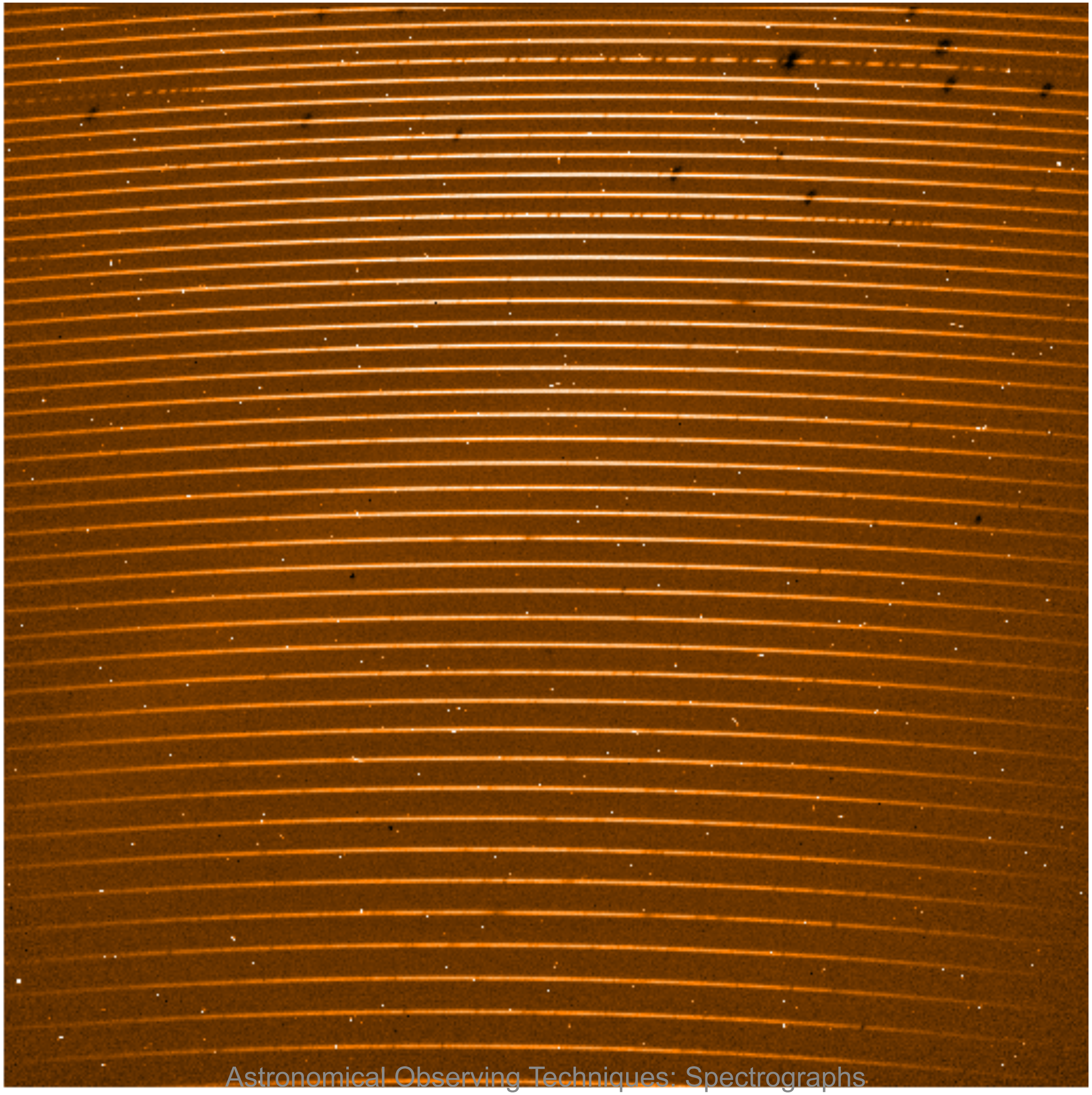
Example: ESO's VLT instrument CRIRES:





The ruled echelle grating of the SOFIA Facility Spectrometer AIRES. Two images of the engineer are seen reflected from the facets of the grooves that are at angles of 90 degrees from each other.

Echelle Spectra

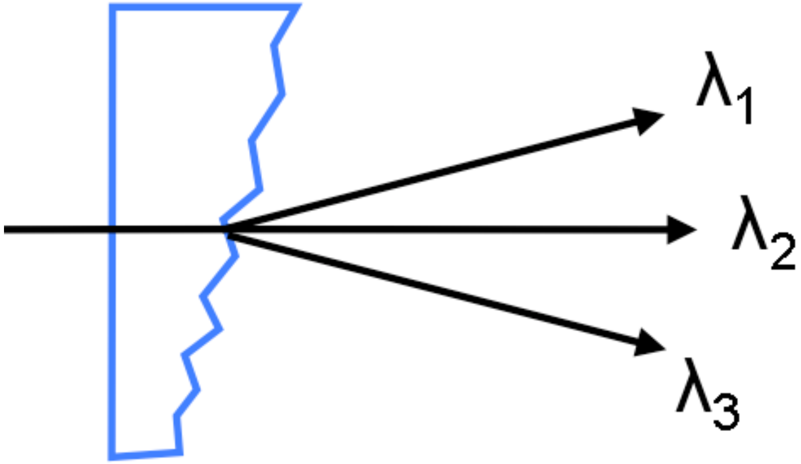


echelle spectrum of V454 Aur

Grisms

Grism = transmission GRating + prISM

For one wavelength and diffraction order, refraction of grating and prism may compensate and optical axis remains (almost) unchanged.



Advantages:

- ideal to bring in and out of a collimated beam ("filter wheel")
- reduces coma (if in non-collimated beam)

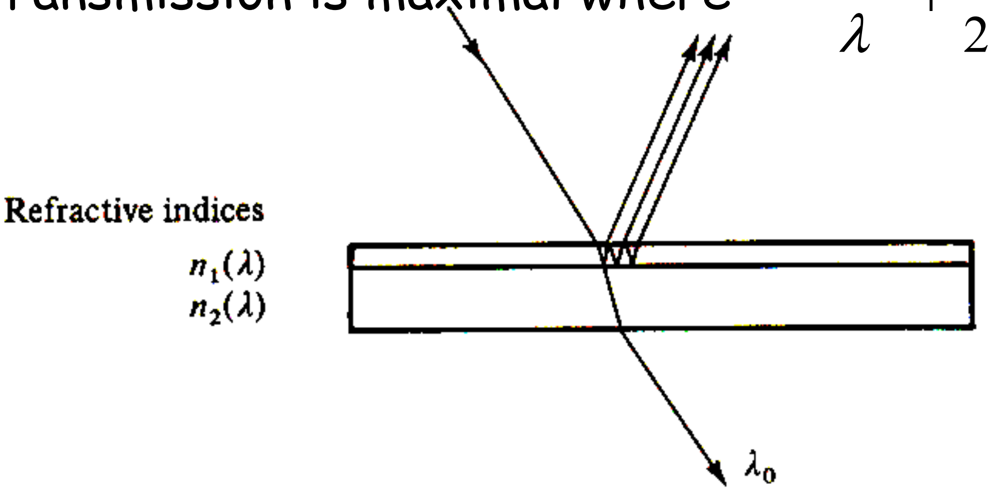
Disadvantages:

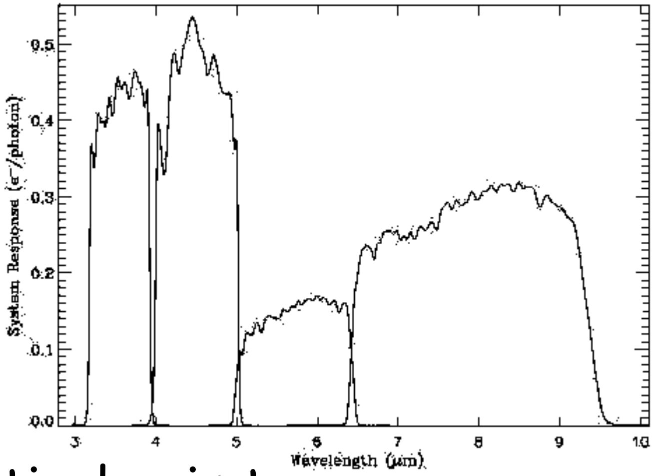
- difficult to manufacture (replication and gluing or by direct ruling.
- can be quite "bulky" (← filter wheel)

Interference (Transmission) Filters

Principle: layers with thickness of ~λ with different indices of refraction deposited on a substrate.

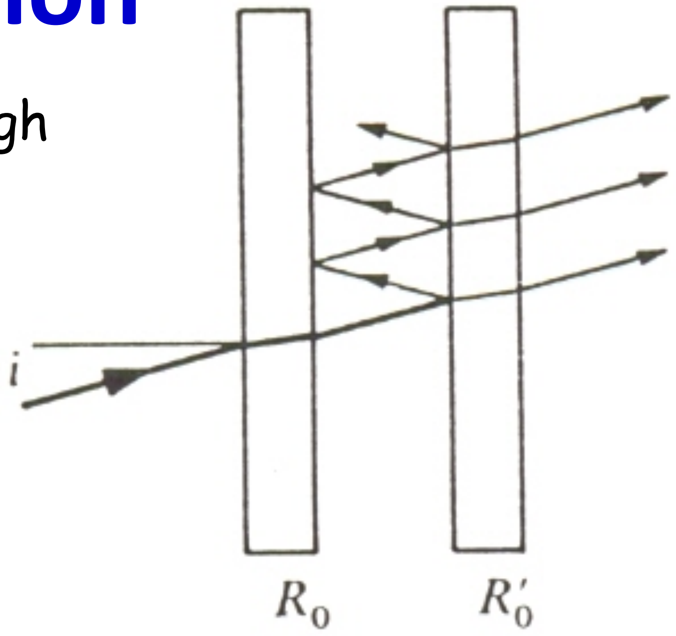
The transmission is maximal where $\frac{2n_1 d}{\lambda} + \frac{\pi}{2} = 2k\pi$





- spectral resolution typically R ~ 3 - 1000
- typically many interference layers
- filters are often tilted with respect to the optical axis to avoid reflections → shift of λ_0
- wavelengths farther from λ_0 (for which the above equation is also satisfied) need a blocking or absorbing filter.

Fabry-Perot Etalon



Two parallel plates (Fabry-Perot etalon) of high reflectivity *r* and transmission *t* = 1-*r*.

The transmission is:

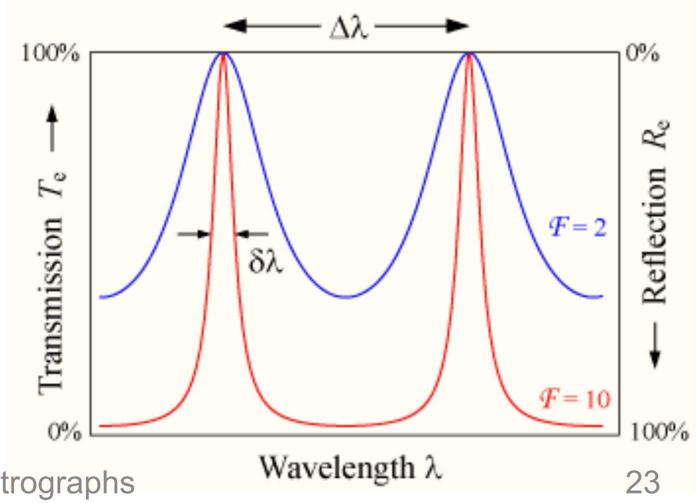
$$I = I_0\left(\frac{r}{1-r}\right)^2\left[1+\frac{4r}{(1-r)^2}\sin^2\left(2\pi dk\cos i\right)\right]^{-1}$$

and has transmission peaks where $k = \frac{m}{2d}$

Here, *m* is the order of the interferometer, *d* is the separation of the plates, and Δ*k* = 1/2*d* the free spectral range.

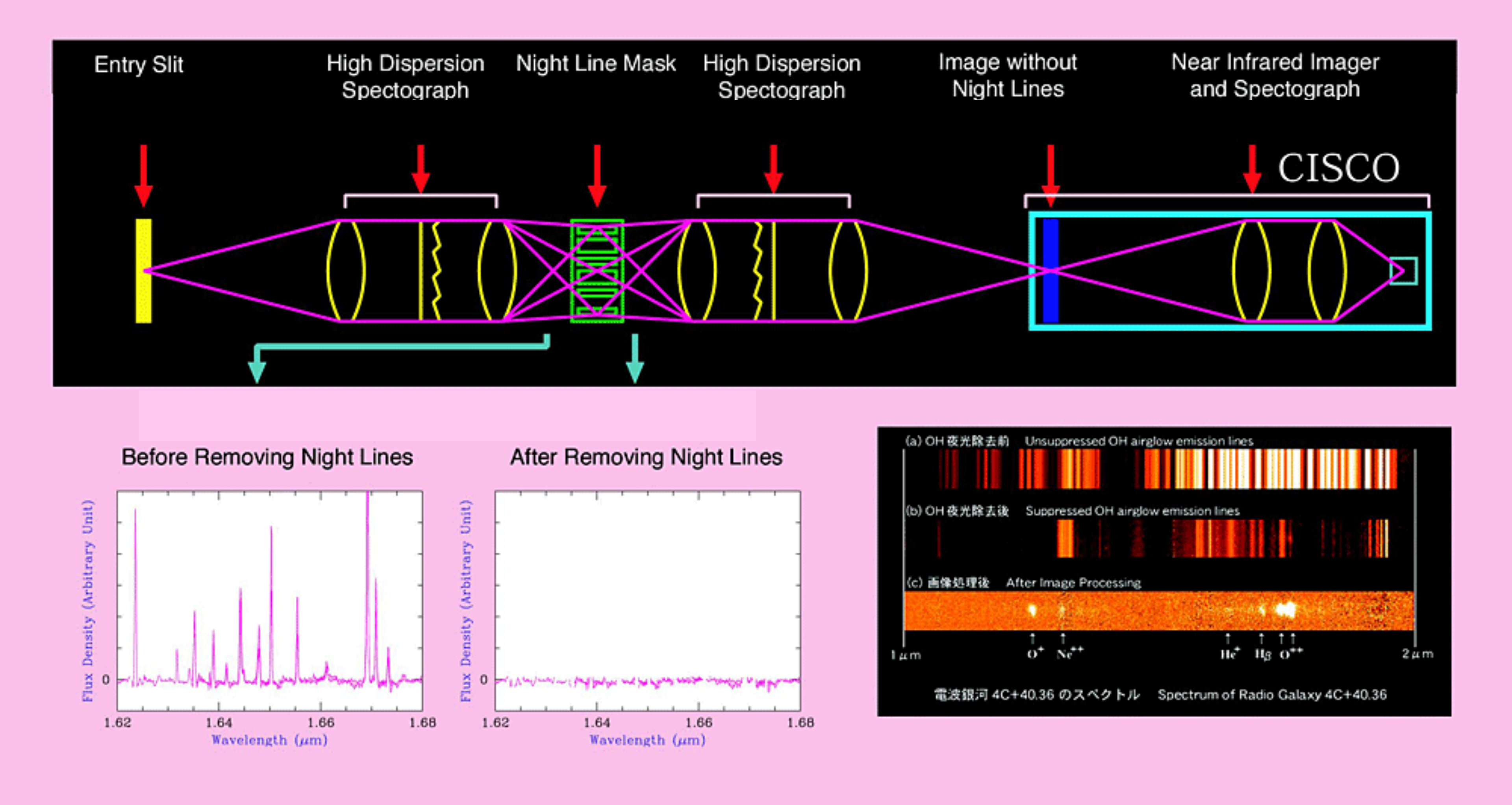
The spectral resolution is given by

1. The finesse $F = \frac{\pi\sqrt{r}}{1-r}$,
2. The resolution $R = \frac{k}{\Delta k} = mF$



OH Suppression Spectrographs

OHS filter out the wavelengths of atmospheric OH lines, which contribute the major part of the near-IR background.

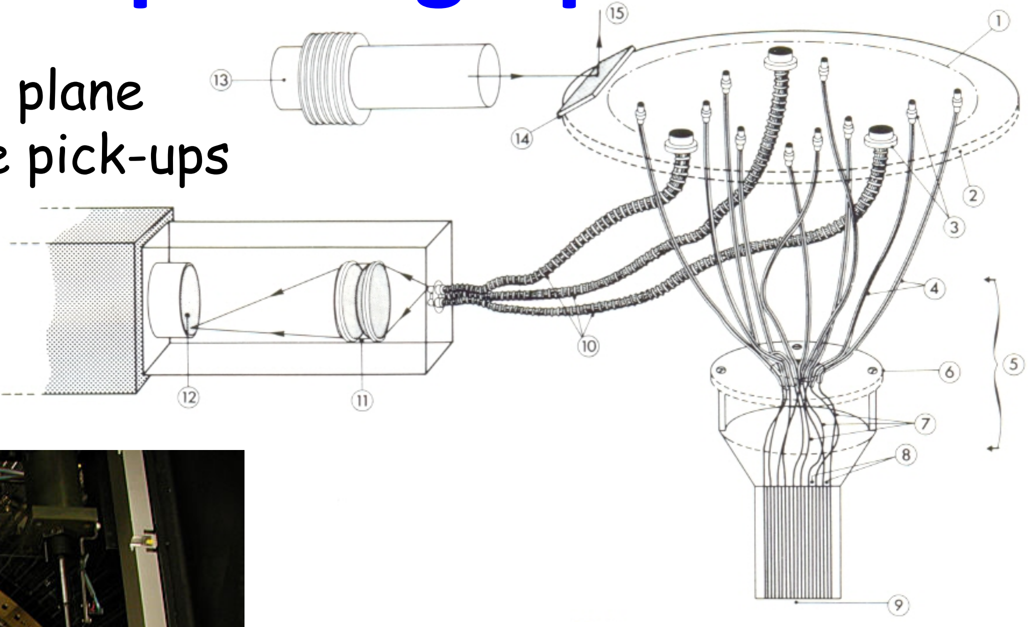


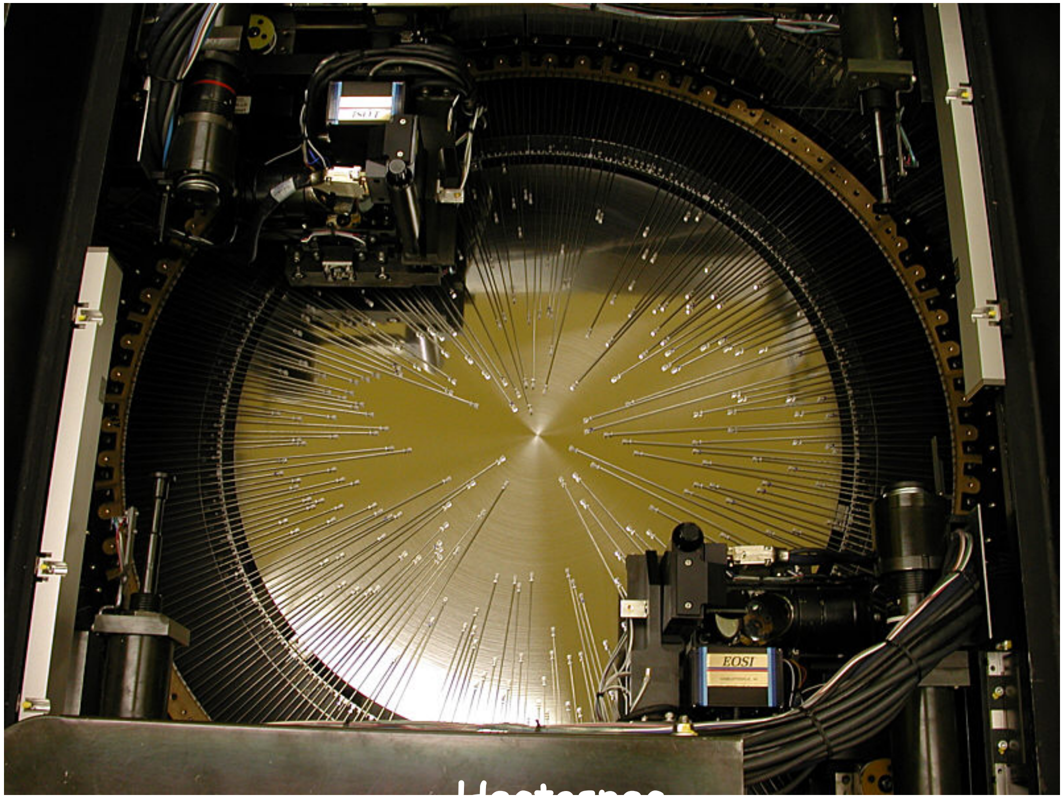
http://subarutelescope.org/Introduction/instrument/img/OHS_concept.gif

Multi-Object Spectrographs

Use numerous "slits" in the focal plane simultaneously → multiple source pick-ups using fibers or mirrors.

Needs different slit masks for different fields.





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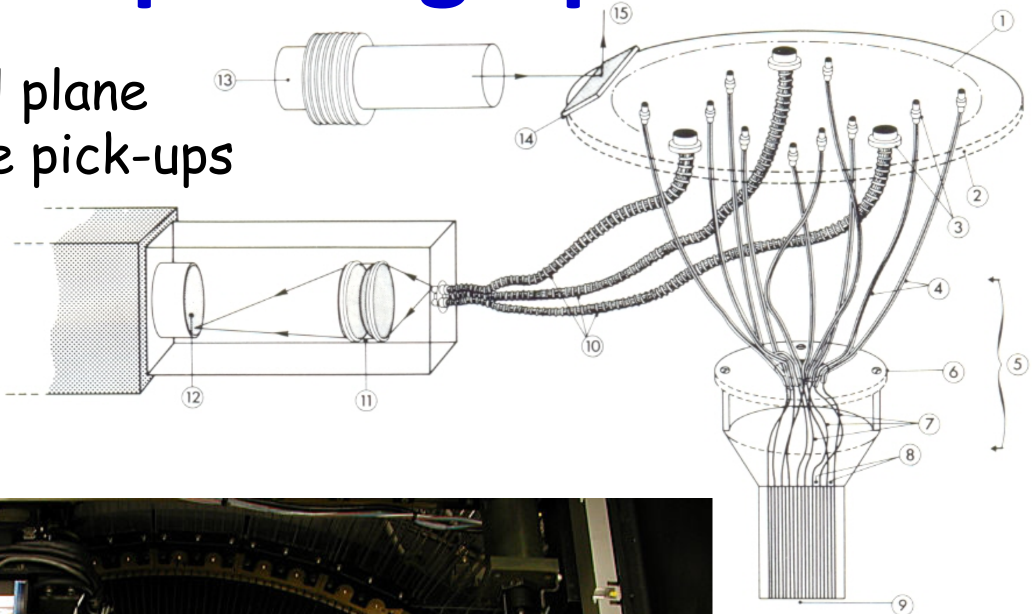
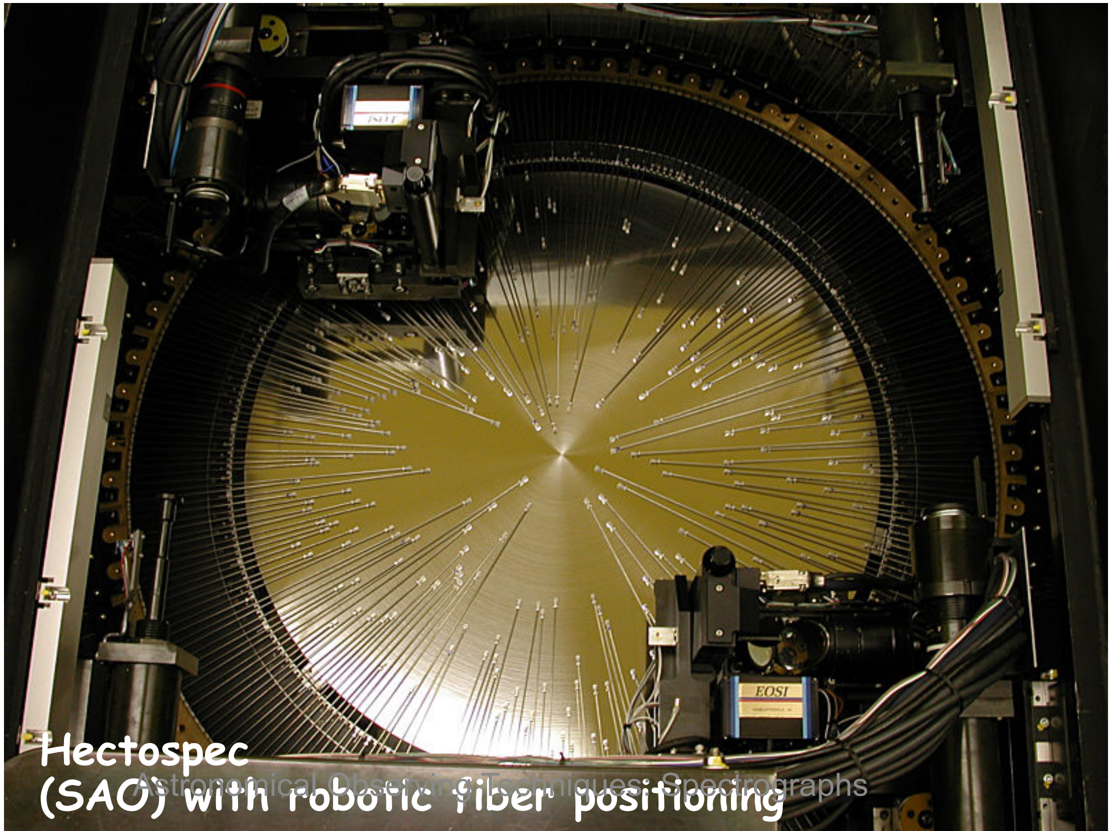
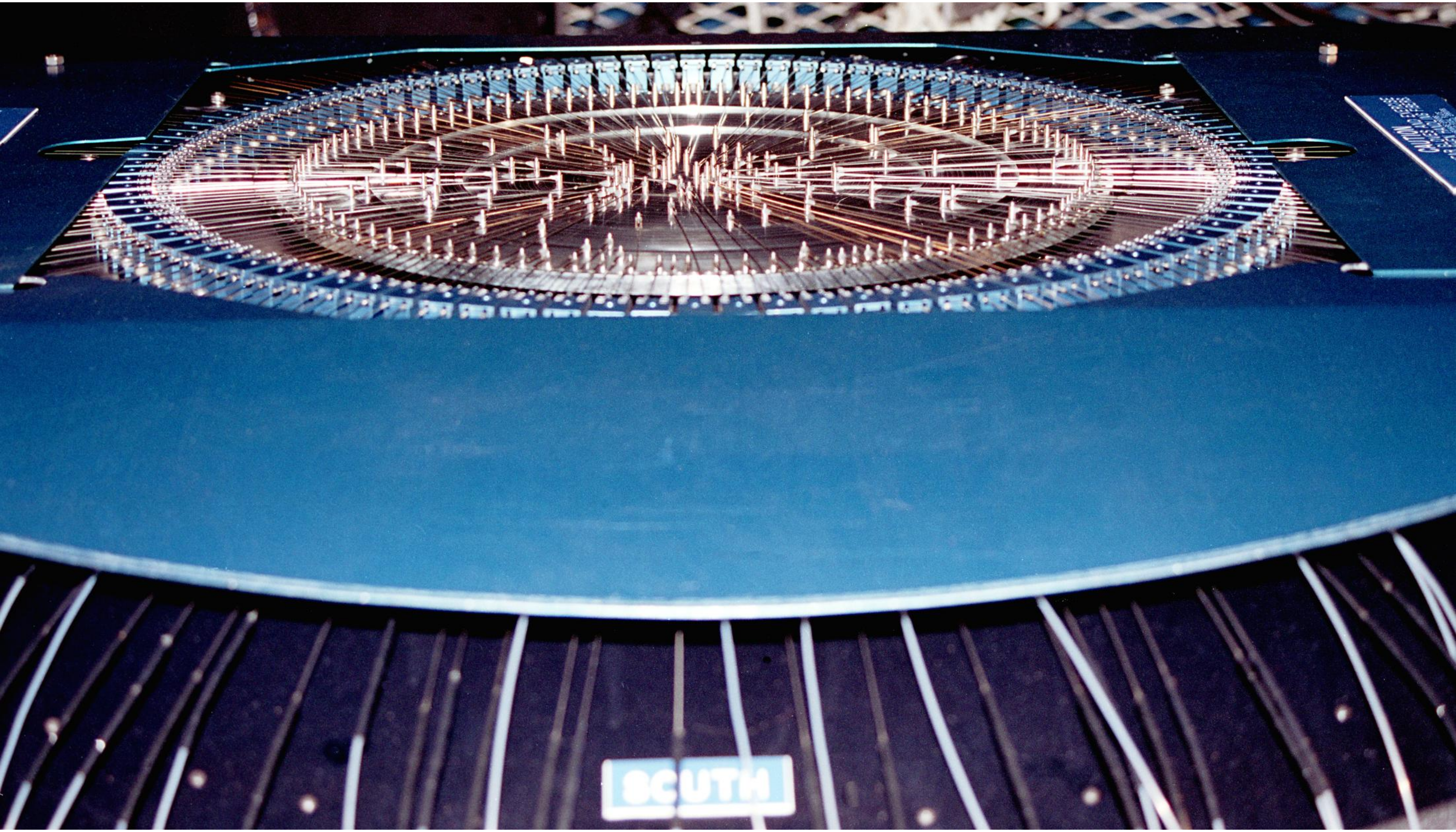


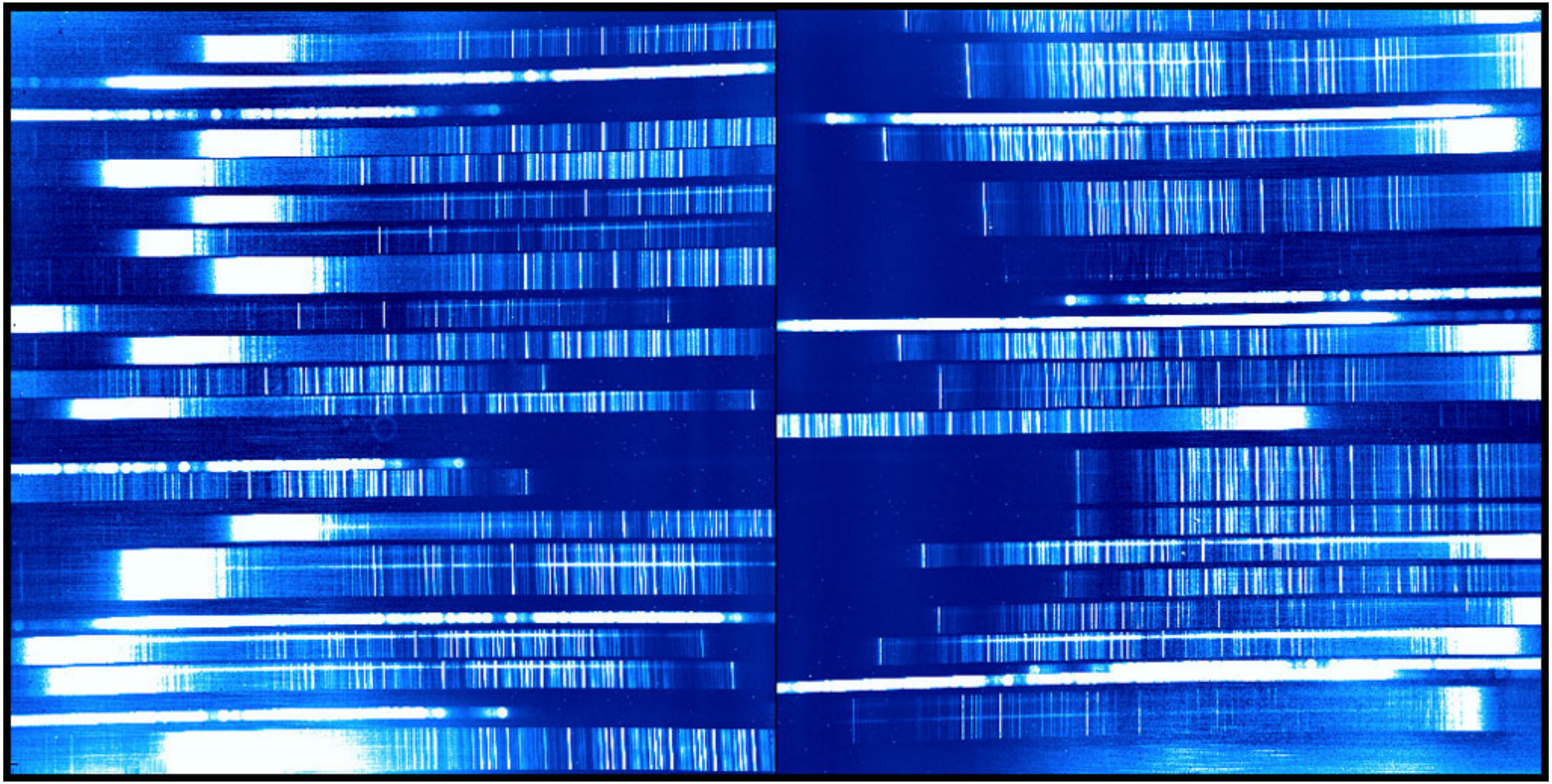


Hectospec
(SAO) with robotic fiber positioning

Hydra Arbitrary Fiber Positioning

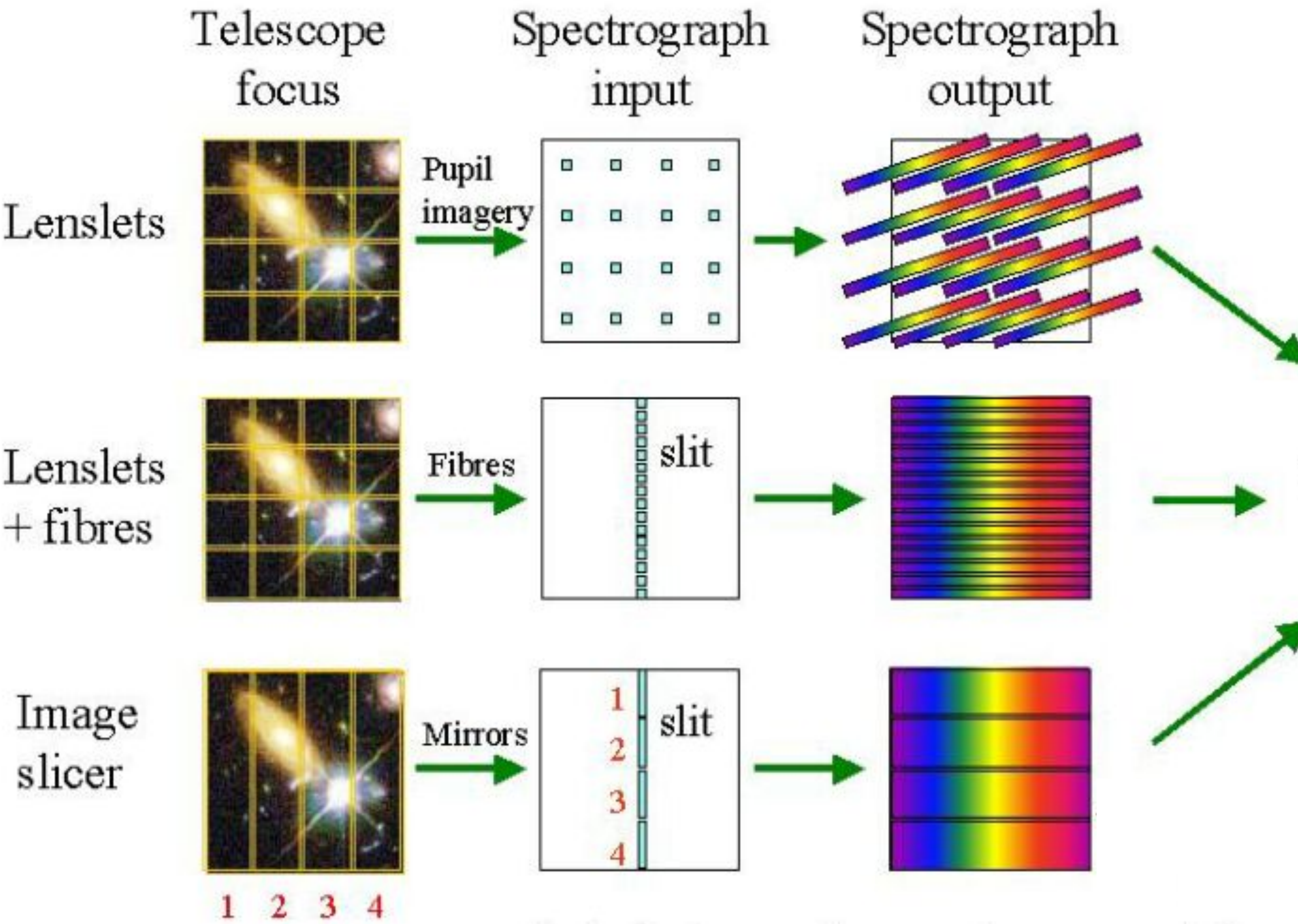


Multi-Object Spectrograph Spectra



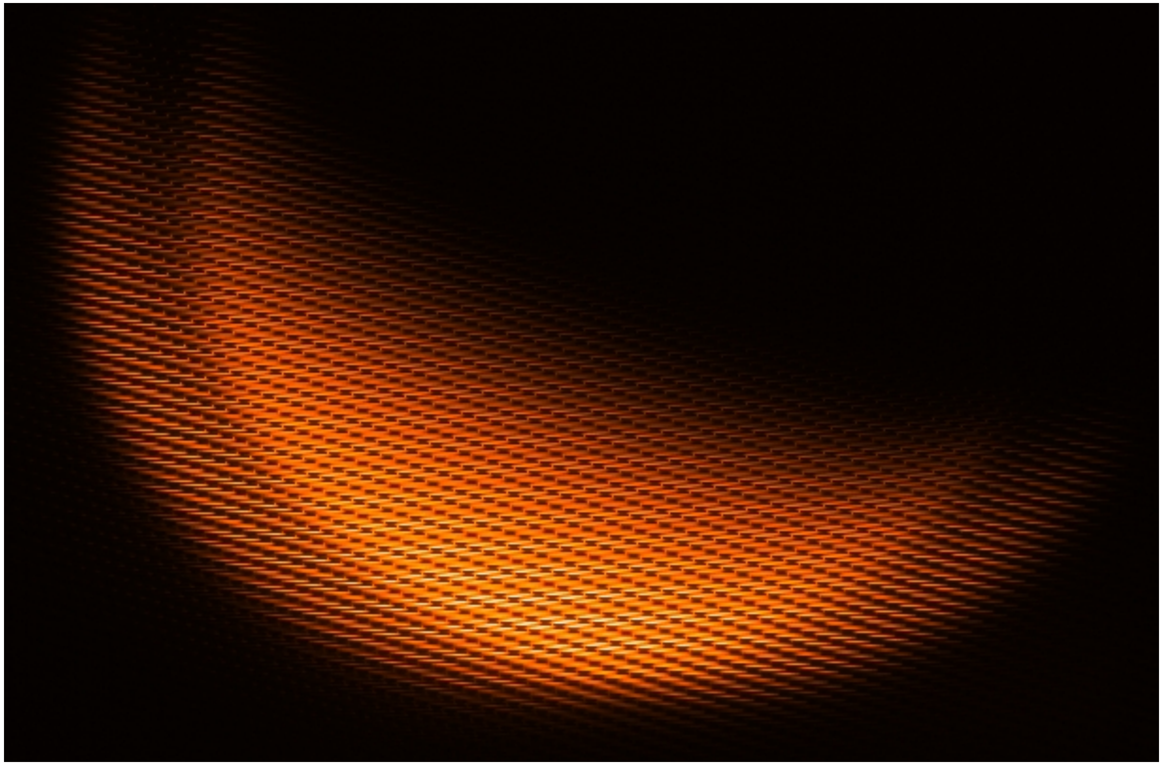
Integral Field Spectrographs

Cut area on sky into adjacent slices or sub-portions, realign them optically into one long slice and treat it as a long slit spectrograph.



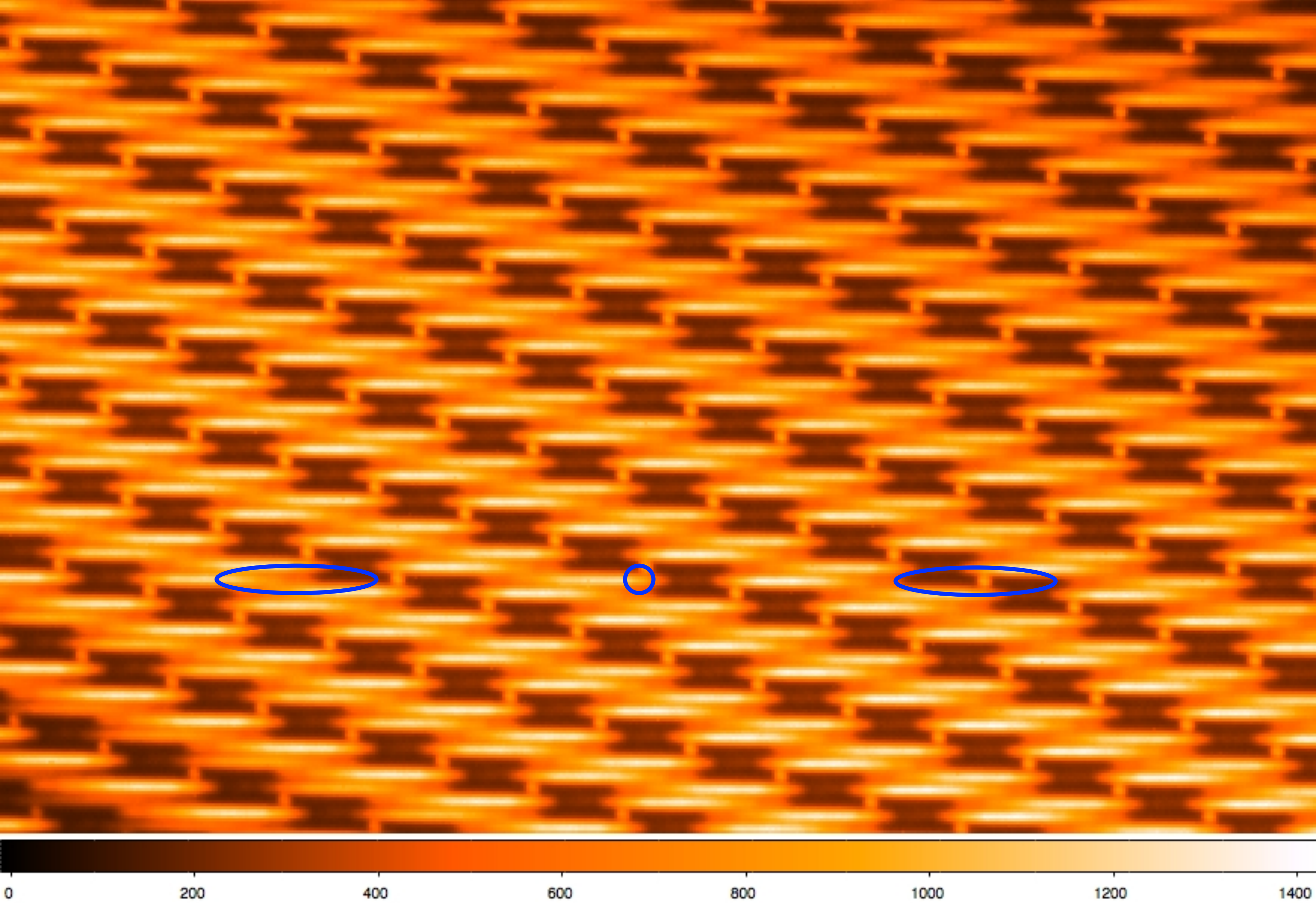
JWST-MIRI image slicer:

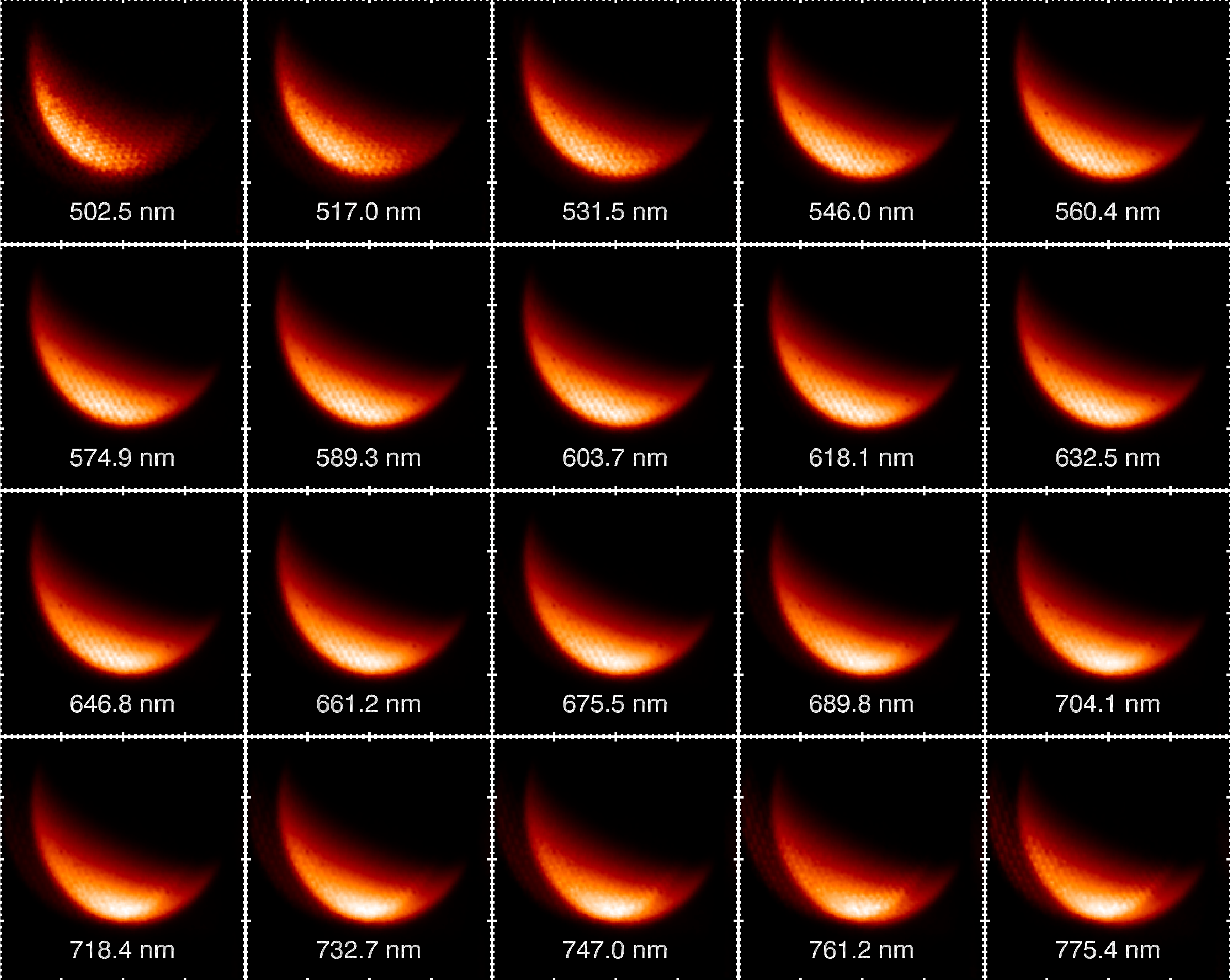
Leiden Observatory pIFU



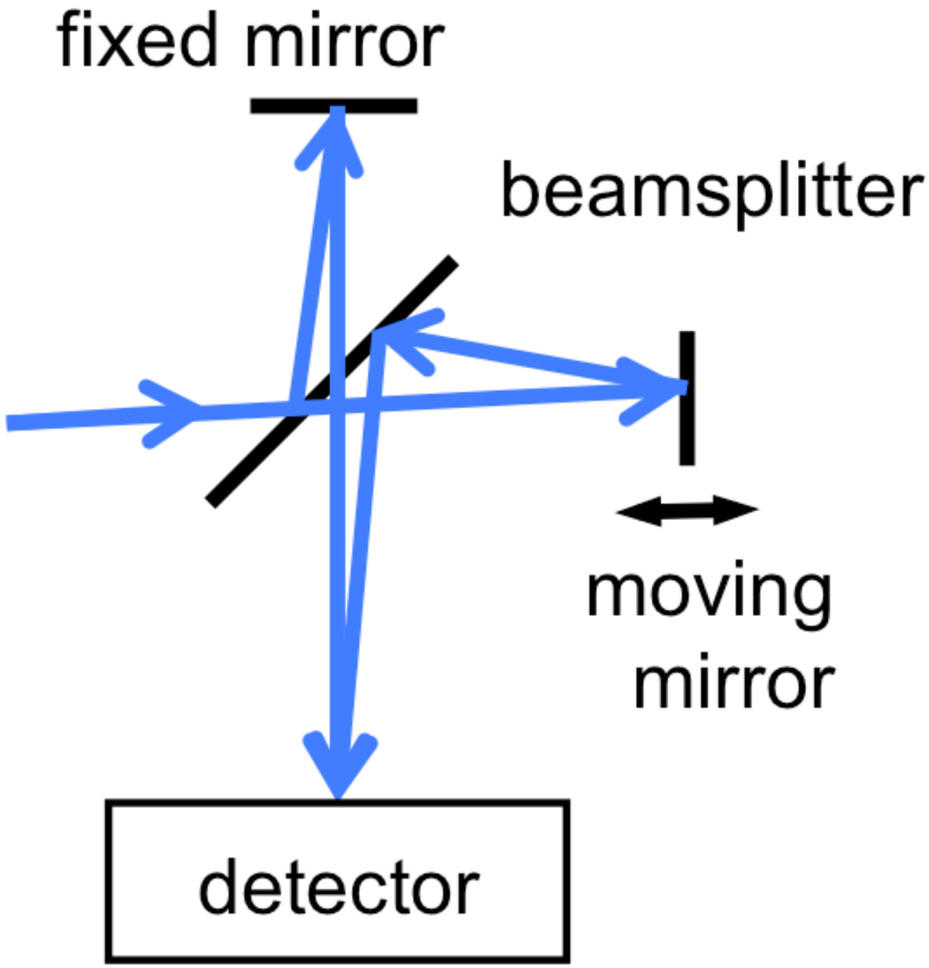
Venus
(Rodenhuis
2013)

- 450-900 nm, R~25
- polarization grating: polarizing beamsplitter and transmission grating
- polychromatic modulation at up to 50Hz
- solves all wavelength-dependent effects


0
200
400
600
800
1000
1200
1400

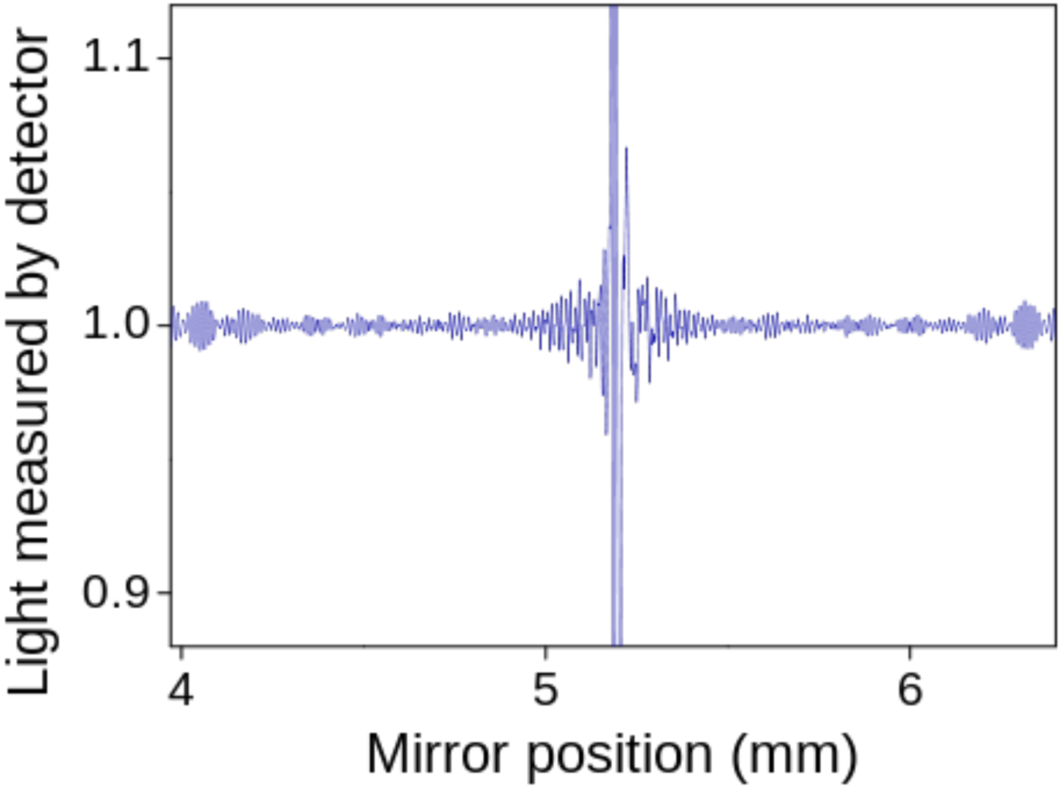

502.5 nm
517.0 nm
531.5 nm
546.0 nm
560.4 nm
574.9 nm
589.3 nm
603.7 nm
618.1 nm
632.5 nm
646.8 nm
661.2 nm
675.5 nm
689.8 nm
704.1 nm
718.4 nm
732.7 nm
747.0 nm
761.2 nm
775.4 nm

Fourier Transform Spectrometer



- *Assume* a single pixel detector
- FTS or Michelson interferometer is a <u>two-wave</u> interferometer (grating has *N* waves from *N* grooves)

FTS – Output Signal



- For each moving mirror position, broadband (integrated over wavelength) intensity is measured
- Measured signal is an interferogram
- Interferogram is Fourier transform of object spectrum

FTS – Measured Intensity

- Exit intensity *I(x)* for a monochromatic input intensity I_0 (with wave number $k=2\pi/\lambda$ and path length difference *x)* is:

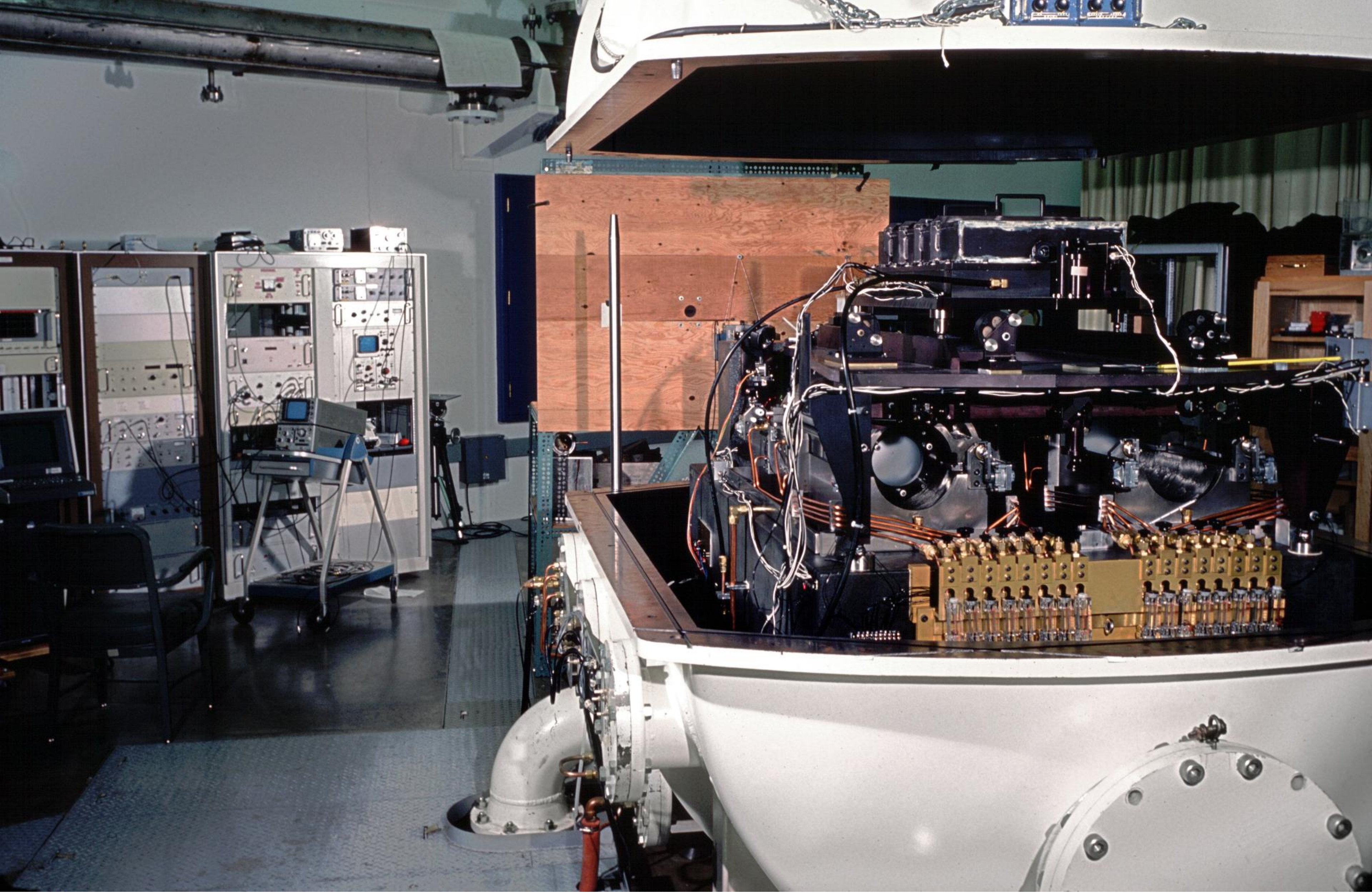
$$I(x)=\frac{I_0}{2}(1+\cos kx)$$

- Source with spectrum $I_0(k)$ in range $[k_1,k_2]$ produces signal

$$I(x)=\frac{1}{2}\int_{k_1}^{k_2} I_0(k)(1+\cos kx)\,dk$$

- For each value of *x*, all spectral elements of incident spectrum contribute to signal, but only one Fourier component is measured at any given point

- Spectral resolution with maximum path length difference x_{max} is $R=2x_{max}/\lambda$



Pros and Cons of the Different Types

Spectrometer	Advantages	Disadvantages
Long-slit	• relatively simple → high throughput • easy to calibrate	• only one object at a time • inefficient use of detector space
Echelle	• high spectral resolution • efficient use of detector	• challenging grating/optics • limited instantaneous λ range
Integral field	• instantaneous 2D info • ideal for resolved objects	• complex optics • single objects only
Multi-object	• up to thousands of spectra • ideal for spectral surveys	• complex mechanisms to select fields • fibre transmission limits λ
Fabry-Perot	• ideal for large objects • high spectral resolution • more compact than FTS	• not practical for large λ range • line and continuum observed at different times → calibration • needs pre-disperser
Fourier-transform (FTS)	• very high resolution • absolute wavelengths • imaging FTS possible	• less gain with high background • high resolution ⇔ wide interval • difficult in cryo instruments