

# *Astronomische Waarnemetechnieken (Astronomical Observing Techniques)*

**11<sup>th</sup> Lecture: 30 November 2011**



## **Content:**

1. Basic Principle
2. Main Components
3. 1D Imaging and Fringes
4. 2D Imaging
5. Fundamental Limitations
6. Radio Interferometers
7. Sub-mm Interferometers

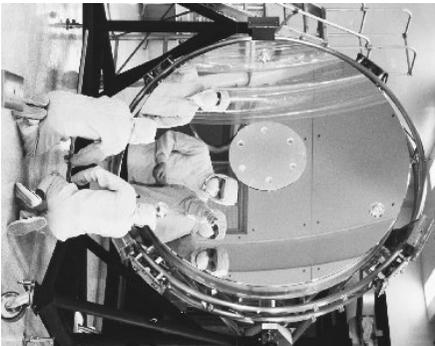
Based on: information provided by ESO on their public website, incl. tutorial by A. Glindemann; Rep. Prog. Phys. 66 (2003) 789-857 by J.D. Monnier, astro-ph/9609092v1 by T. Bedding; and ARA&A 30, 457-98 (1992) by M. Shao & M.M. Colavita.

# Basic Principle

# The Basic Idea

Angular resolution  $\theta = 1.22 \frac{\lambda}{D}$

$$D = D_{\text{tel}}$$



$$D = d_{\text{baseline}} + D_{\text{tel}}$$

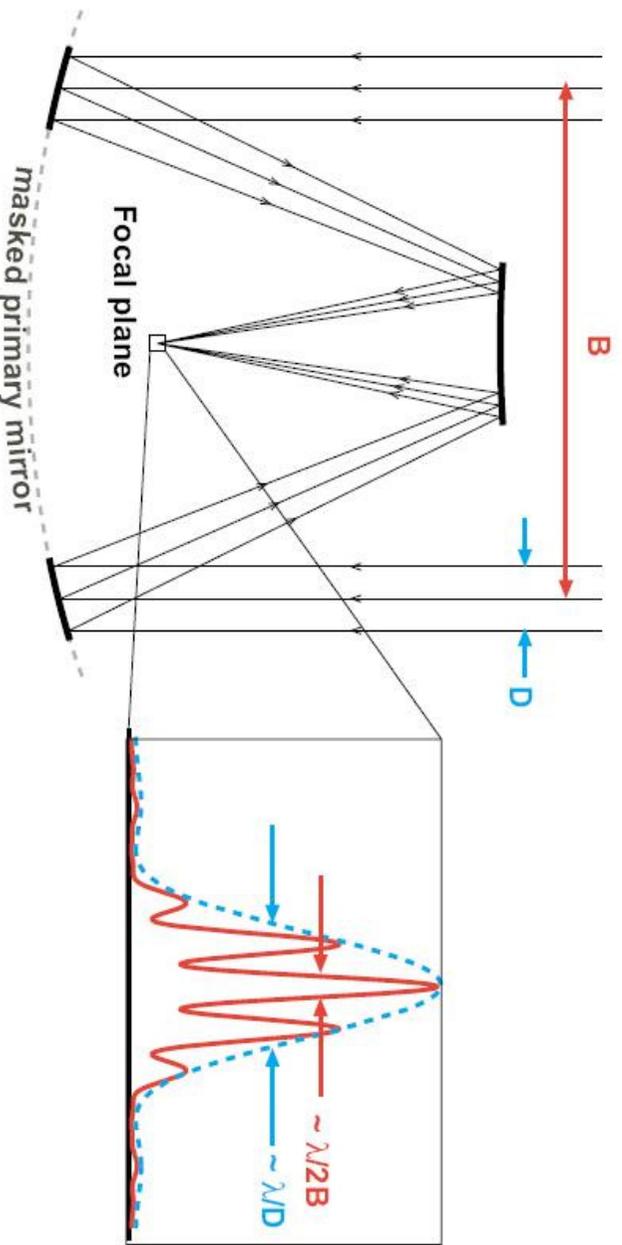


Angular resolution is determined by interference; interference does not need a continuous aperture (see Young's double slit experiment)!

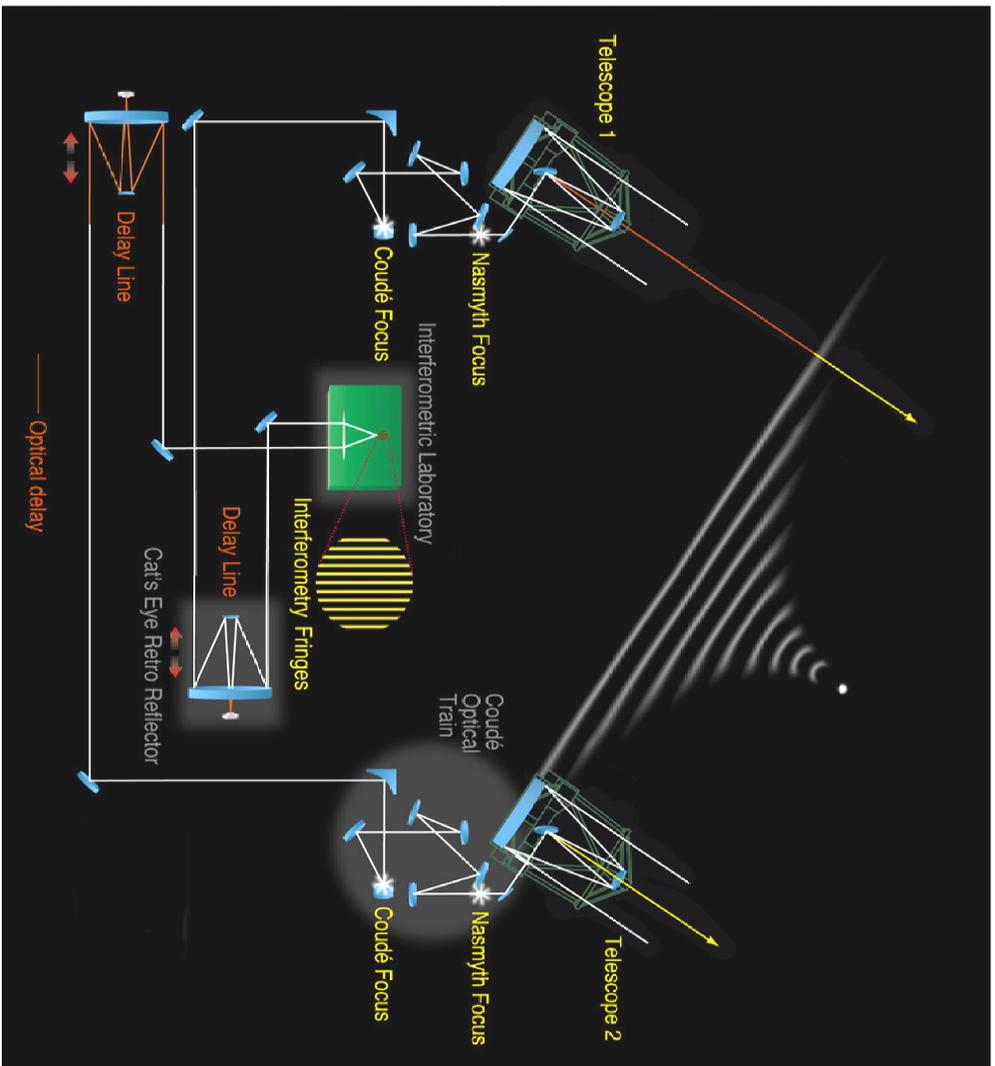
→ Hippolyte Fizeau (1868): basic concept of stellar interferometry

# The Consequence

Interferometry is like masking a giant telescope:



# The Basic Principle - Optical



# Main Components

# Main Components: 1) Telescopes

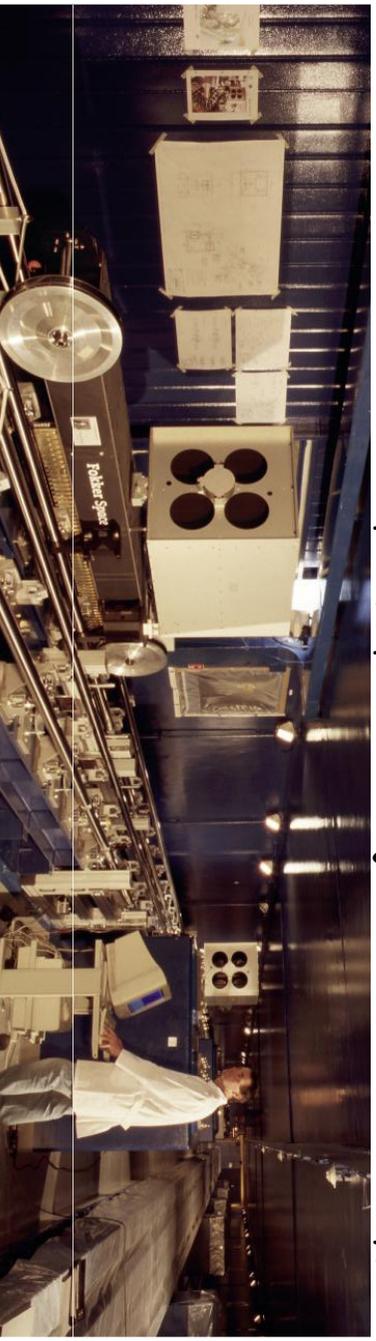
An optical interferometer typically consists of  $n$  telescopes of similar type and characteristics



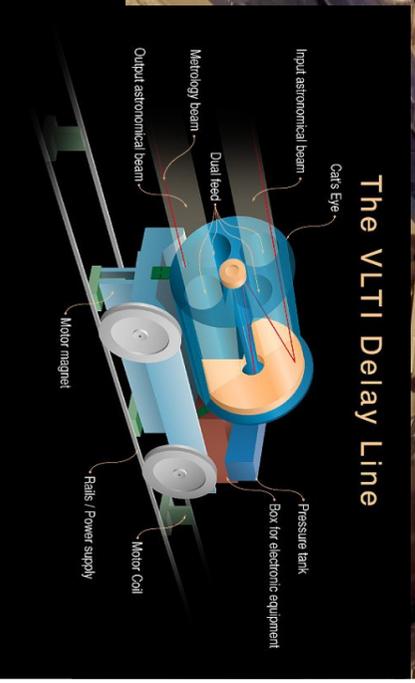
Keck interferometer (Hawaii) ↑  
← VLTI (Paranal)

# Main Components: 2) Delay Lines

Delay lines are needed to compensate the optical path difference between the various telescopes (depends on object location on the sky)



Challenge: travel over tens of meters, positioning to fractions of micrometers  
→ dynamic range of  $> 10^9$ !



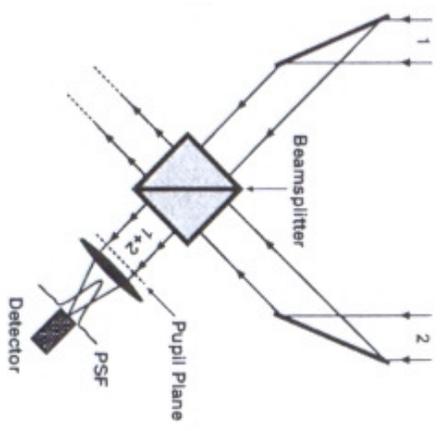
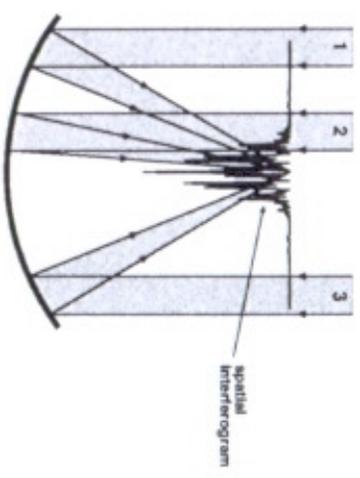
# Main Components: 3) Beam Combiner

Two main types:

- **multi-axial (image plane):** beams are placed adjacent to each other and form a fringe pattern in space.



The AMBER Instrument at the VLT Interferometer



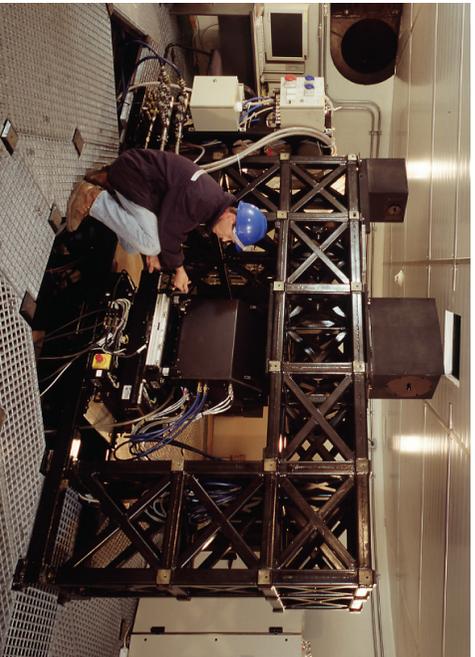
- **co-axial (pupil plane):** beams are added on top of each other e.g. via a beam splitter.
- but also single-mode fibers and integrated optics.

# Main Components: 4) Adaptive Optics

Adaptive optics (or for telescopes with  $D < r_0$  tip-tilt correction) is essential to **correct wavefront aberrations** for good interference.

The **amplitude of the fluctuations** is:  $\sigma = \sqrt{6.88} \left( \frac{B}{r_0} \right)^{5/6}$  rads RMS

Hence, for a baseline  $B = 100\text{m}$  and a seeing of  $1''$  this amounts to  $70\mu\text{m}$ !



*The MACAO (Multi Application Curvature Adaptive Optics) system on a 8m VL T. Can be used with natural guide stars with  $1 < V < 17$ , seeing  $< 1.5''$ ,  $T_0 > 1.5\text{ms}$  and airmass  $< 2$ .*

# 1D Imaging and Fringes

## Fringe Visibility - Definition

The visibility is defined as 
$$V = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}}$$

It is the Fourier transform of the object's brightness distribution.

If the dark regions in the fringe pattern go to zero  $V = 1 \rightarrow$  object is *unresolved*.

If  $V = 0$  then there are no fringes  $\rightarrow$  object is completely *resolved*.

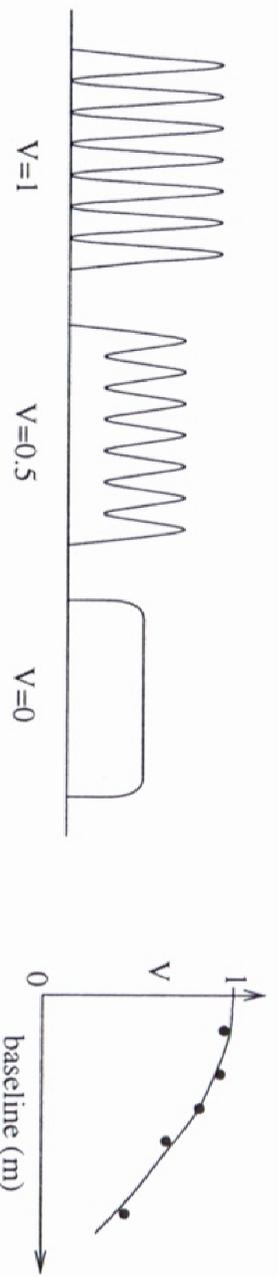
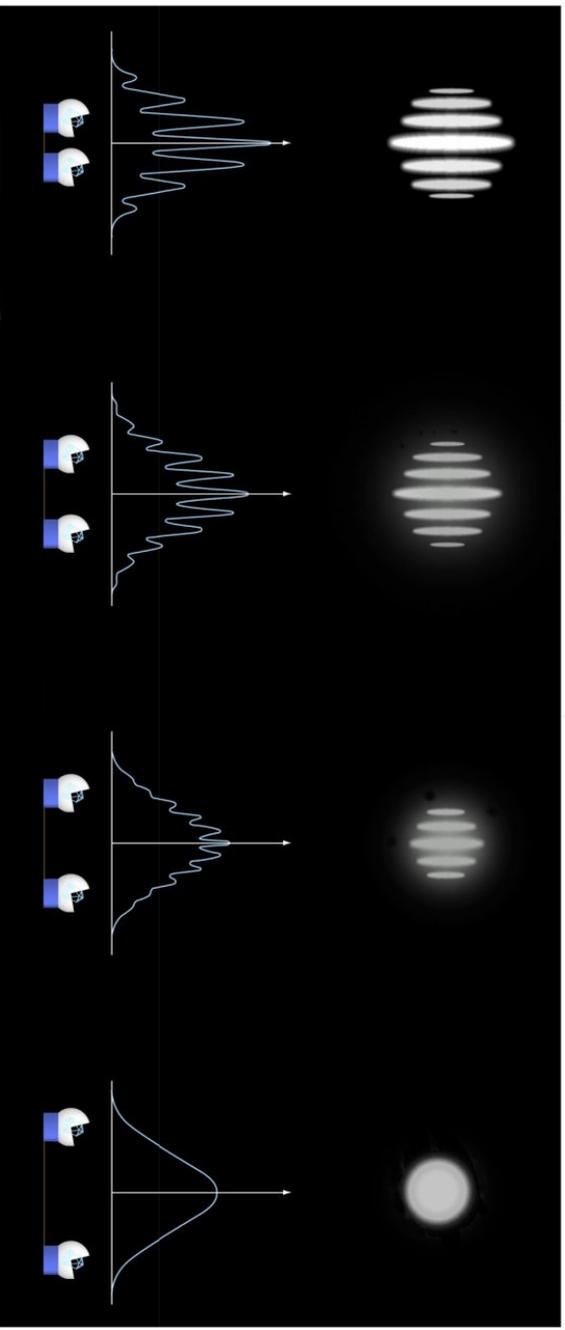


Fig. 2. Left: examples of fringes with visibilities of 1, 0.5 and 0. Right: visibility as a function of baseline for a resolved star.

# Fringe Visibility - Baseline



Interferometric Fringes at Different Telescope Baselines  
(Simulation)

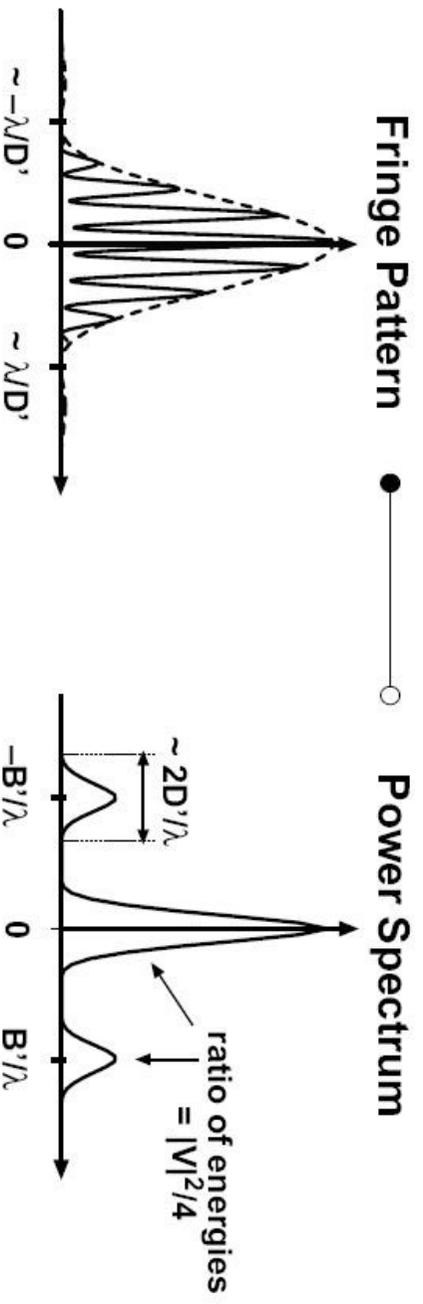
ESO PR Photo 10e/01 (18 March 2001 )

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The observed pattern from a single star at the focal plane clearly changes as the distance between the two telescopes is gradually increased. The "fringes" disappear completely when the star is resolved.

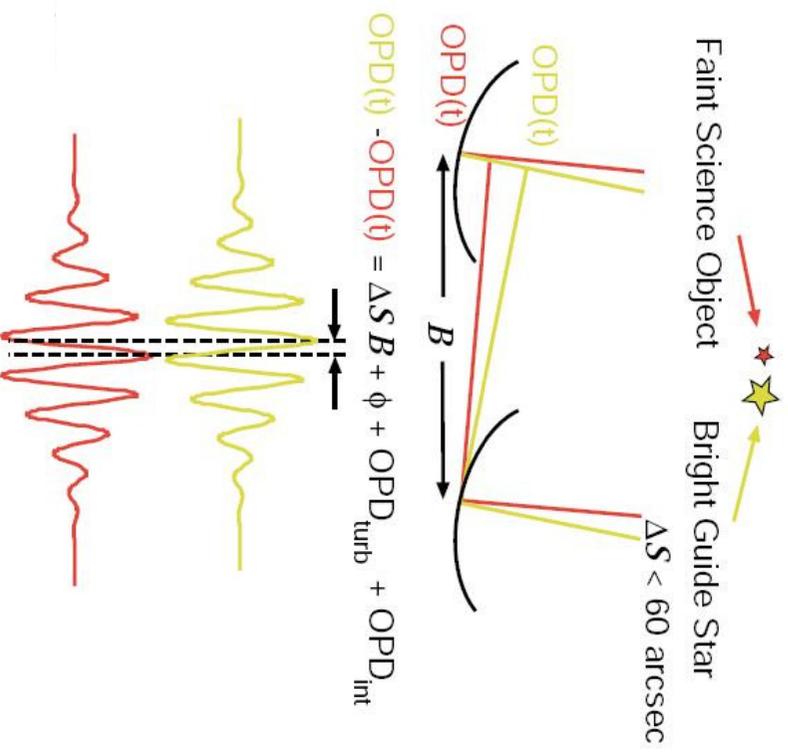
# Fringe Visibility and Power Spectrum



# Fringe Tracking (Co-Phasing)

The white-light fringe has to be **actively tracked**, which requires tracking fluctuations within a small fraction of wavelength in real-time.

Example: ESO's FINITO scans the center of the fringe packet in H band with high speed and sends a co-phasing signal to the VLTI delay lines. FINITO operates on two channels, i.e. tracks three baselines.



## Closure Phase (1)

Fringe visibility tells one component of the objects Fourier transform = **amplitude** of the fringes

The **phase** is determined by the position of the fringes.

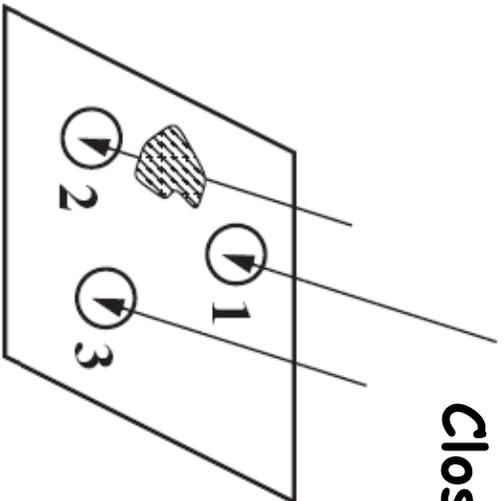
Problem: due to atmospheric turbulence (which changes the optical path length), the fringes move constantly forward and backward.

**Idea:** use **three telescopes** → three sets of fringes:  
(1-2), (2-3), (1-3)

In all three sets the fringes move, but **not independently!**

→ this information is called **closure phase** (or **self-calibration** in aperture synthesis imaging - the standard technique in radio interferometry) and can be used to cancel out phase error terms.

## Closure Phase (2)



$$\begin{aligned} \text{Observed} & & \text{Intrinsic} & & \text{Atmosphere} \\ \Phi(1-2) & = & \Phi_o(1-2) & + & [\phi(2)-\phi(1)] \\ \Phi(2-3) & = & \Phi_o(2-3) & + & [\phi(3)-\phi(2)] \\ \Phi(3-1) & = & \Phi_o(3-1) & + & [\phi(1)-\phi(3)] \end{aligned}$$

$$\text{Closure Phase} = \Phi_o(1-2) + \Phi_o(2-3) + \Phi_o(3-1)$$

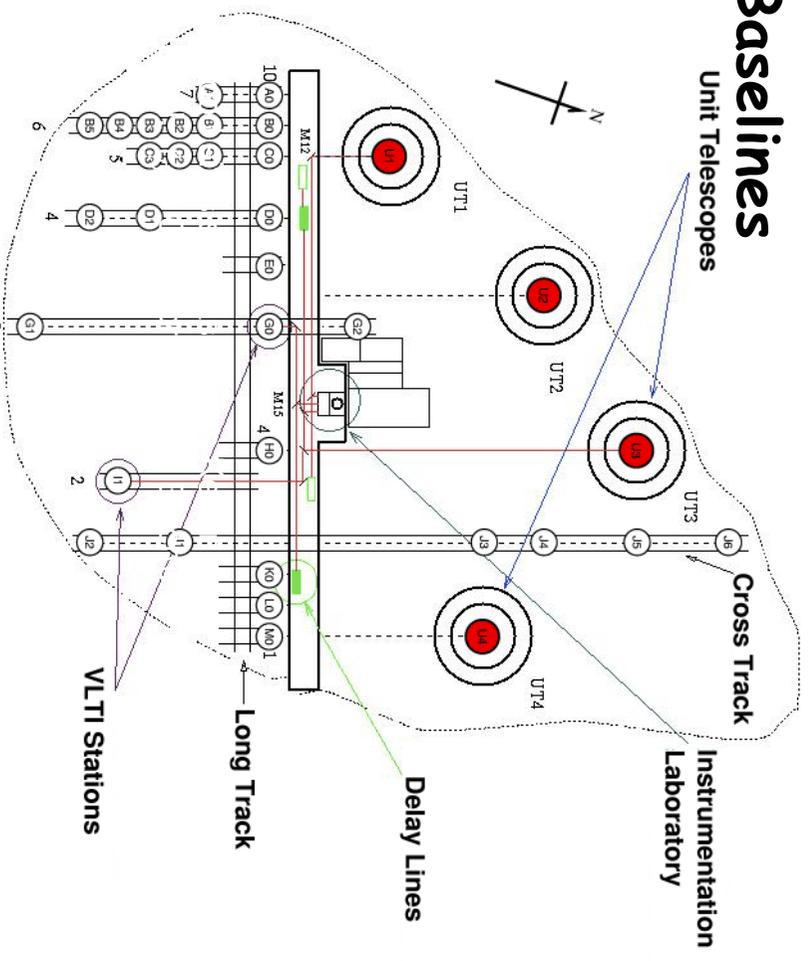
The error terms cancel out!

Table 1. Phase information contained in the closure phases alone.

Number of telescopes	Number of Fourier phases	Number of closing triangles	Number of independent closure phases	Percentage (%) of phase information
3	3	1	1	33
7	21	35	15	71
21	210	1330	190	90
27	351	2925	325	93
50	1225	19600	1176	96

2D Imaging  
(requires more baselines)

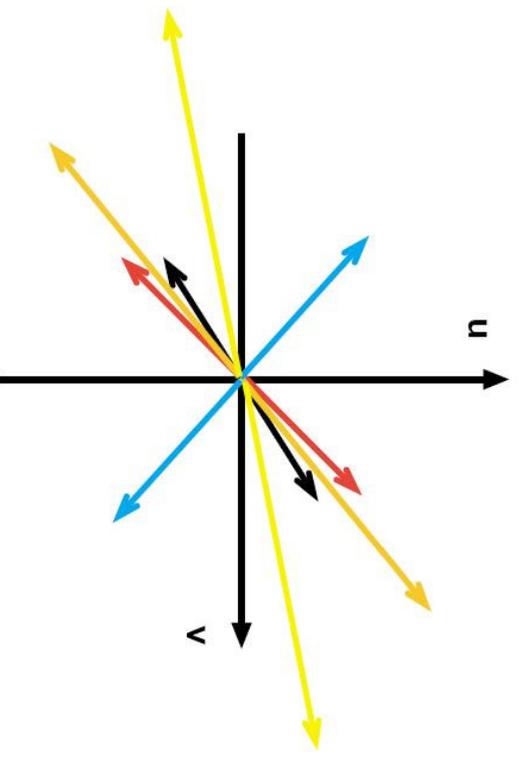
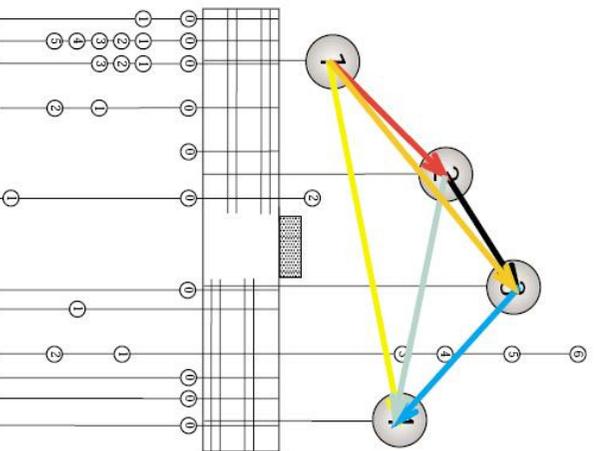
# The VLTI Baselines



The three ATs move on rails between the thirty observing stations above the holes that provide access to the underlying tunnel system. The light beams from the individual telescopes are guided towards the centrally located, partly underground Interferometry Laboratory

## Baseline Coverage (1)

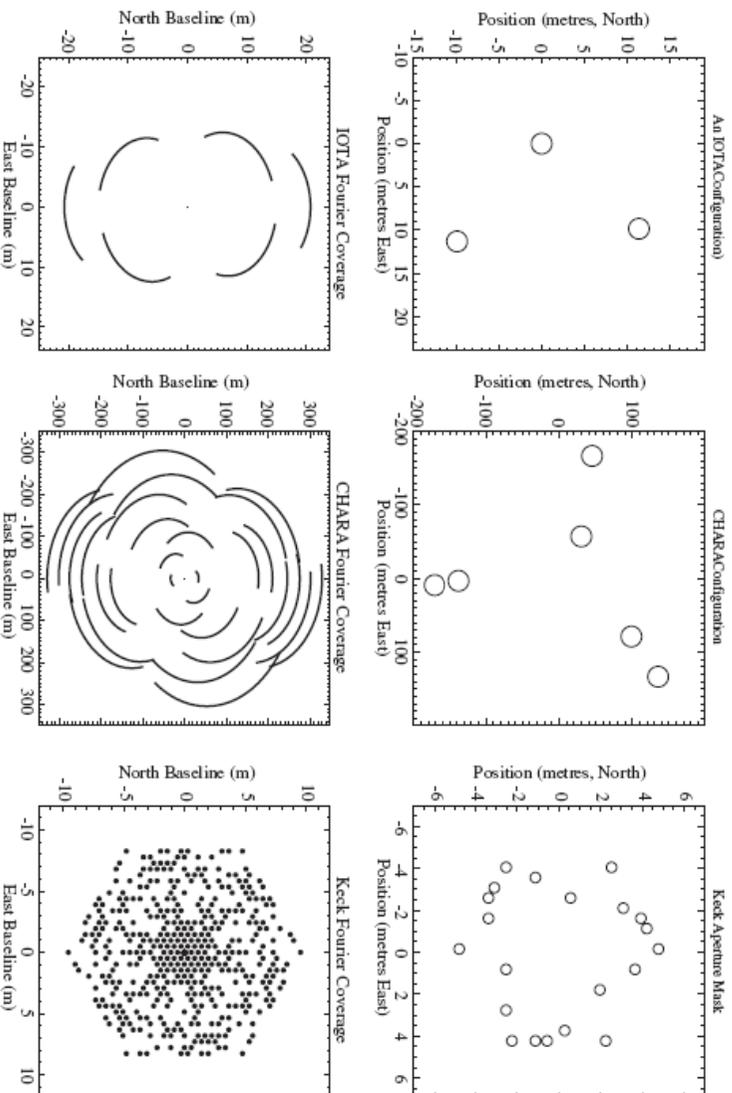
A smooth reconstruction of the object's intensity distribution  $I$  requires a good coverage of the  $(u,v)$  plane.



Note: This is the  $uv$ -plane for an object at zenith. In general, the projected baselines have to be used.

## Baseline Coverage (2)

The Earth's rotation helps to fill the (u,v) plane. Assumed is a source at  $45^\circ$  declination, observed for 3 hr both before and after transit.



# Fundamental Limitations

# Field of View and Limiting Magnitude

The **field of view** is typically limited to a few arcseconds only

(except for Fizeau interferometers):  $\theta_{\max} \leq \frac{\lambda}{D} \frac{\lambda}{\Delta\lambda}$

- the size of the complex transfer optics. Larger field = larger optical elements
- spatial filters, which limit the FOV

The **limiting magnitude** is given by the atmospheric turbulence, which requires either:

- to use integration times shorter than  $\tau_0$  or
- to use an AO system (guide stars!)

## Sensitivity of an Interferometer

The signal-to-noise for the measurement of visibility or phase with an interferometer is:

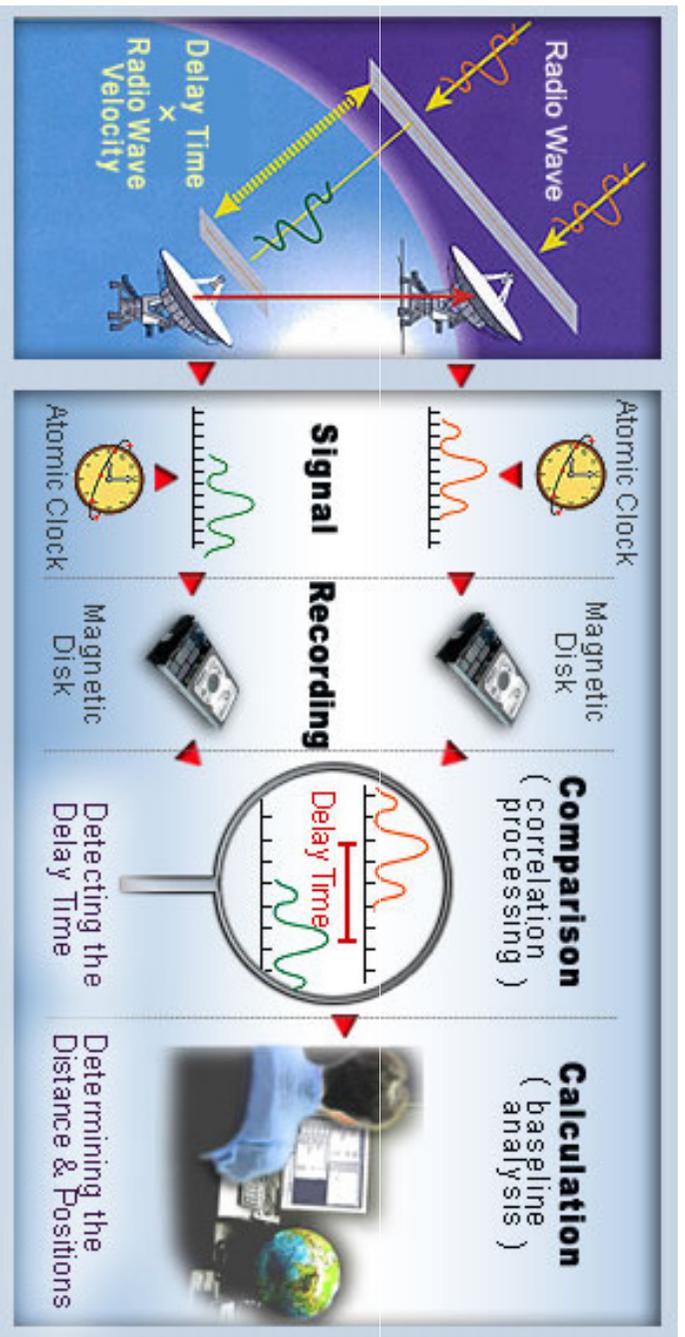
in the **photon-limited regime** (visible):  $SNR_{Poisson} = \sqrt{\frac{nV^2}{1 + \frac{1}{nV^2}}} \propto \sqrt{n} \cdot V$

in the **background-limited regime** (IR):  $SNR_{BLIP} = \sqrt{\frac{\frac{n^2V^2}{b}}{1 + \frac{1}{n^2V^2} / b}} \propto n \cdot V$

where  $n$  is the number of source photons per **coherence volume**  $D^2 \cdot \tau_0$ ,  $b$  is the number of background photons per coherence volume, and  $V$  is the fringe visibility.

# Radio Interferometry Projects

## The Basic Principle - VLBI



## European VLBI (Very Long Baseline Interferometry) Network



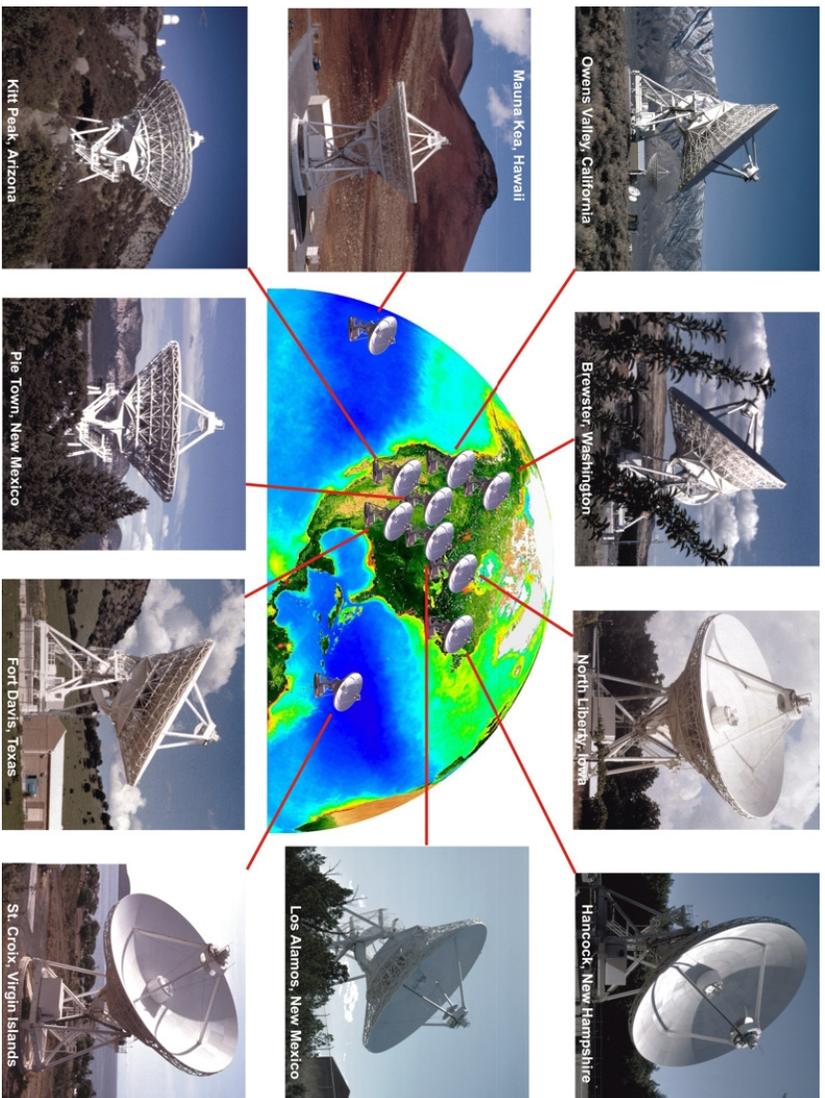
## Very Large Array VLA

- *Y-shaped array of 27 telescopes moved on railroad tracks*
- *telescope diameter 25-m each*
- *located: high Plains of San Augustin in New Mexico*
- *"D", "C", "B", and "A" configurations, spanning 1.0, 3.4, 11, and 36 km, respectively*



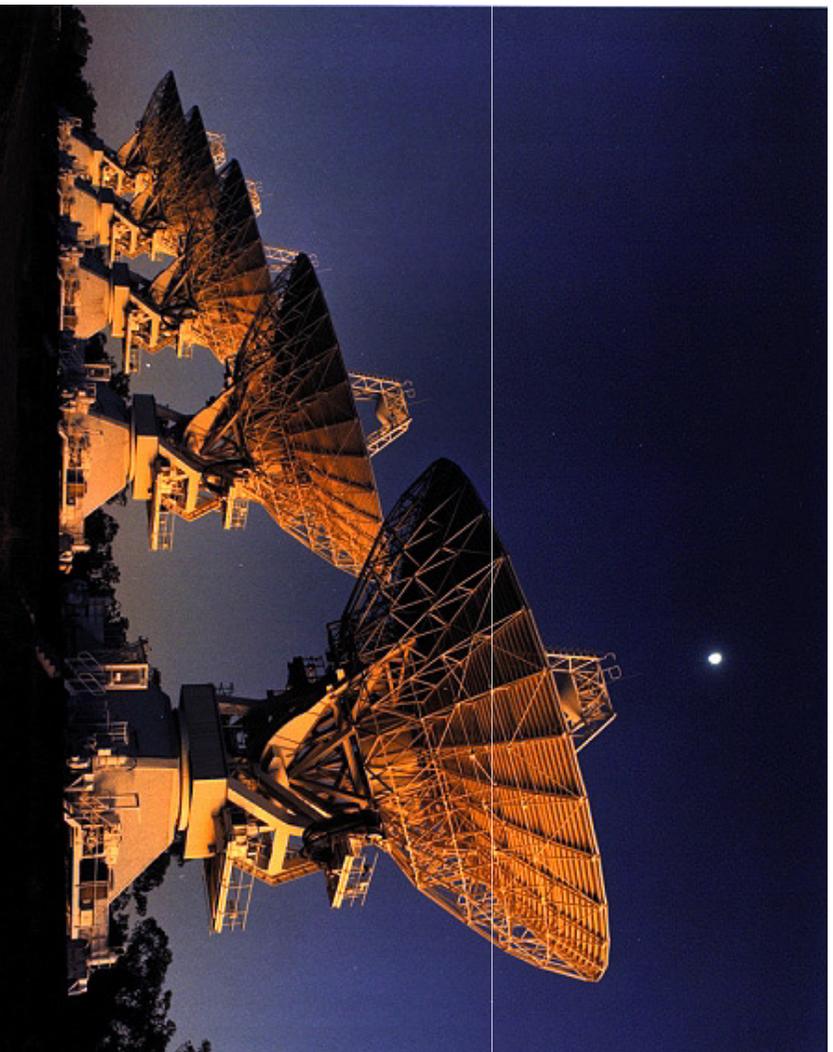
# Very Long Baseline Array VLBA

*Ten 25 m antennas form an array of 8000 km in size.*



# Australia Telescope Compact Array ATCA

*Six 22 m telescopes on an east-west baseline*



# Westerbork

- *Westerbork Synthesis Radio Telescope (WSRT)*
- *14 telescopes*
- *25-meter each*
- *East-west baseline*
- *3 km in length*
- *effective collecting area of a 92 m dish*



# LOFAR

*25,000 antennas for radio frequencies below 250 MHz.*



# Sub-mm Interferometry Projects

## **Plateau de Bure**

*Interferometer of six 15 m antennas*



# Combined Array for Research in Millimeter-wave Astronomy (CARMA)

*CARMA = six 10-meter telescopes from Caltech's Owens Valley Radio Observatory + nine 6-meter telescopes from the Berkeley-Illinois-Maryland Association → Cedar (CA)*



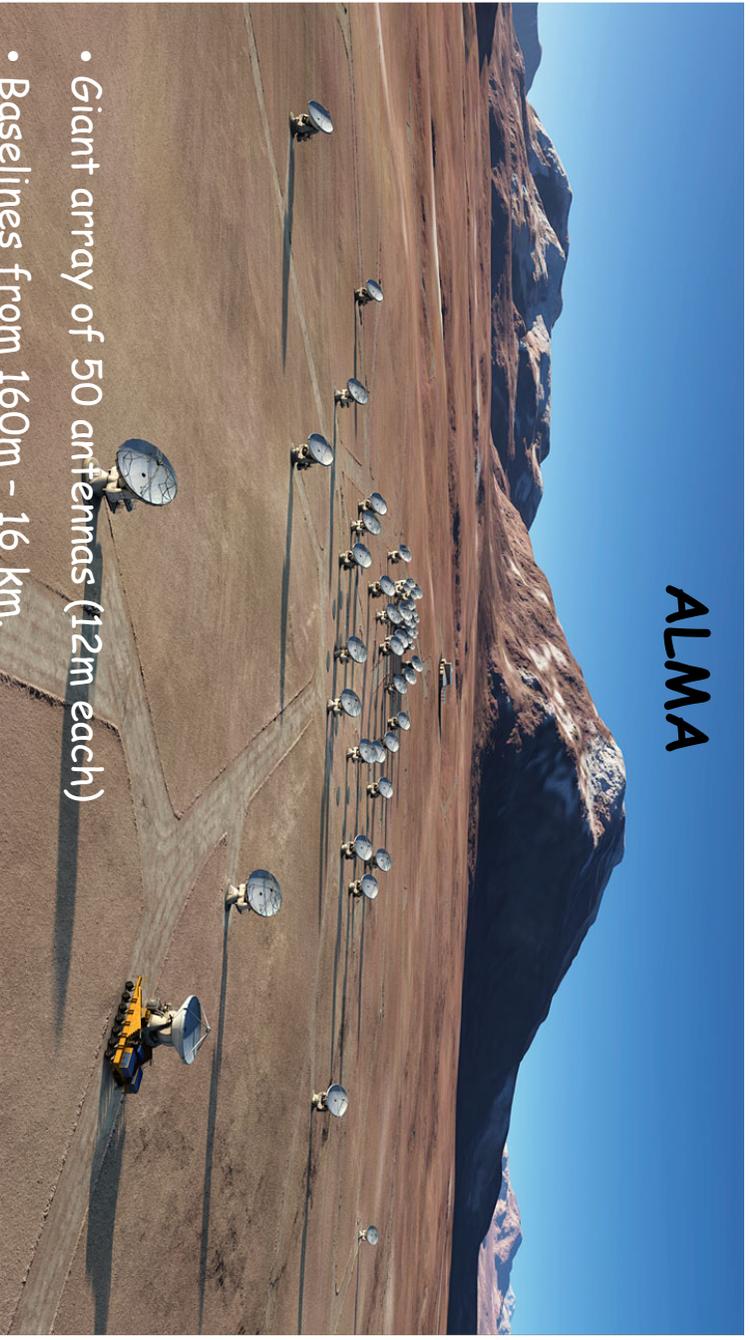
# Sub-Millimeter Array (SMA)

*The SMA consists of eight 6 m antennas on Mauna Kea (HI)*



# ALMA

- Giant array of 50 antennas (12m each)
- Baselines from 160m - 16 km.
- Additional compact array of twelve 7m and four 12m antennas
- Located on the Chajnantor plain at 5000m altitude
- Wavelength range 3 mm - 400  $\mu\text{m}$  (84 to 720 GHz)



**Observing frequencies: Band 3 (>84 GHz) to band 9 (<720 GHz).**

**Field of view ~ size of individual antennas & frequency (but independent of array configuration). FWHM of beam is 21" at 300 GHz To . To achieve uniform sensitivity over a larger field mosaicking is required**

**Spatial resolution: ~ frequency & maximum baseline.**

**Most extended configuration (~16 km): 6 mas at 675 GHz**

**Structures  $> 0.6 \gg \lambda/b_{\text{min}}$  ( $b_{\text{min}}$ =shortest baseline) are not well reproduced in reconstructed images  $\rightarrow$  measure with the ALMA Compact Array (ACA) using the 7-m antennae (come closer).**

**Spectral resolution: up to 8192 frequency channels (spectral resolution elements). At 110 GHz, R=30,000,000 or 10m/s velocity resolution.**

**Sensitivity: use ALMA Sensitivity Calculator to estimate noise levels or required integration times at**

**<http://almascience.eso.org/cal1-for-proposals/sensitivity-calculator>**

