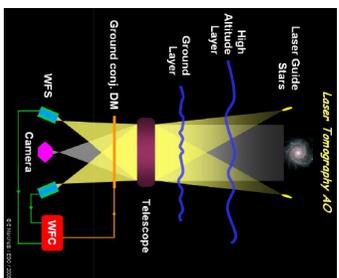
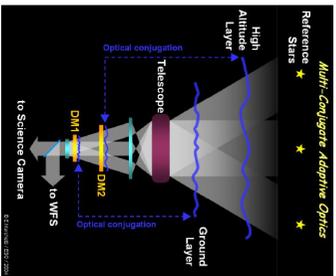
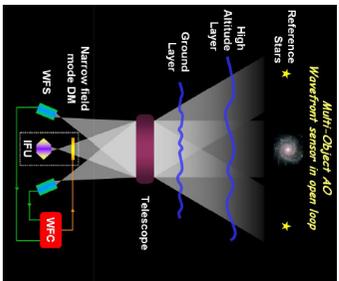


# Astronomische Waarneemtechnieken (Astronomical Observing Techniques)

10<sup>th</sup> Lecture: 23 November 2011



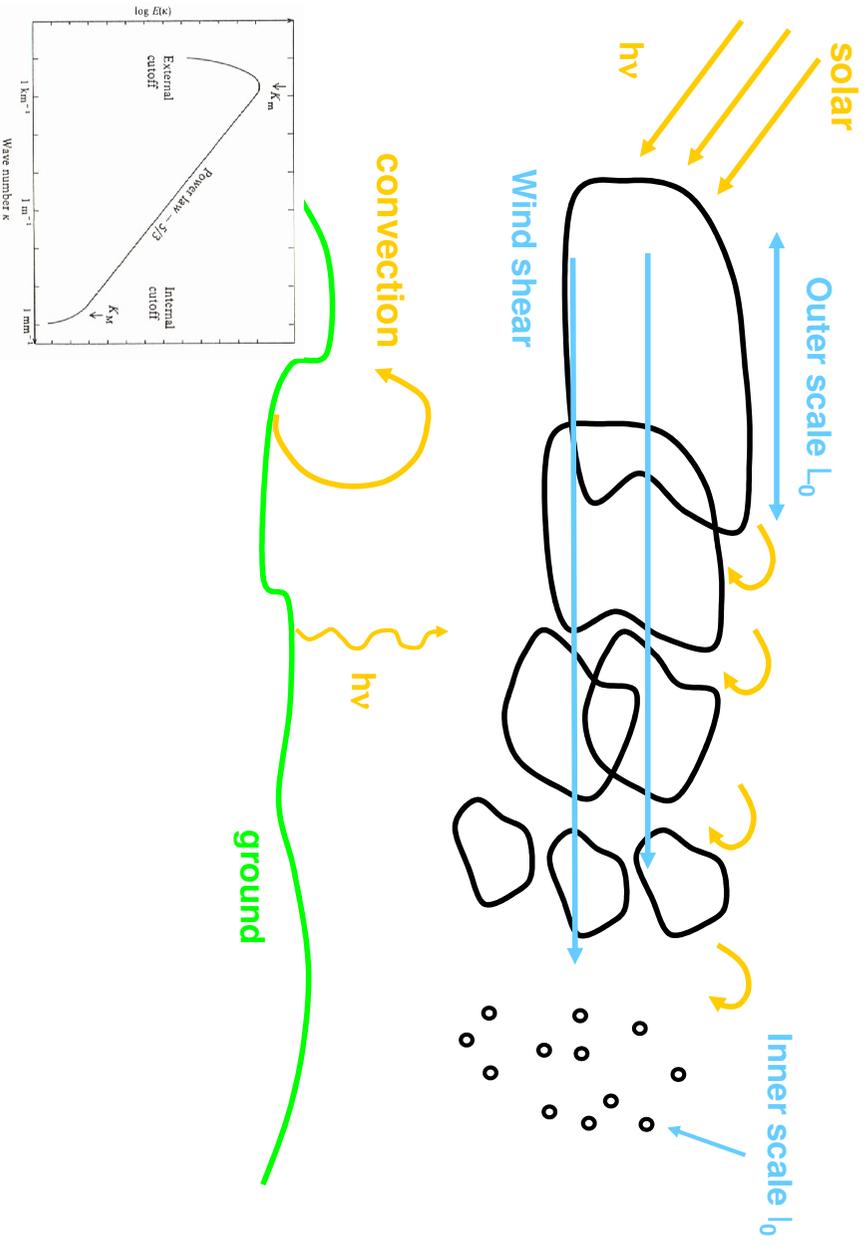
- Content:
1. Atmospheric Turbulence
  2. Why AO?
  3. Basic Principle
  4. Key Components
  5. Error Terms
  6. Laser Guide Stars
  7. Types of AO Concepts

Based on:

"Adaptive Optics in Astronomy" (Cambridge UP) by F. Roddier (ed.),  
Claire Max's lecture course on AO <http://www.ucoick.org/~max/289C/>  
and ESO: [http://www.eso.org/projects/aot/DSM/AO\\_modes.html](http://www.eso.org/projects/aot/DSM/AO_modes.html)

# Reminder: Atmospheric Turbulence

# Kolmogorov Turbulence



## $r_0$ , seeing, $\tau_0$ , $\theta_0$

The Fried parameter  $r_0(\lambda) = 0.185 \lambda^{6/5} \left[ \int_0^\infty C_n^2(z) dz \right]^{-3/5}$  is the radius of the spatial coherence area.

It is the average turbulent scale over which the RMS optical phase distortion is 1 radian. Note that  $r_0$  increases as  $\lambda^{6/5}$ .

$\Delta\theta = \frac{\lambda}{r_0} \sim \lambda^{-1/5}$  is called the seeing. At good sites  $r_0$  (0.5 $\mu$ m)  $\sim$ 10 - 30 cm.

The atmospheric coherence (or Greenwood delay) time is:  $\tau_0 = 0.314 \frac{r_0}{v}$ . It is the maximum time delay for the RMS wavefront error to be less than 1 rad (where  $v$  is the mean propagation velocity).

The isoplanatic angle  $\theta_0 = 0.314 \cos \zeta \frac{r_0}{h}$  is the angle over which the RMS wavefront error is smaller than 1 rad.

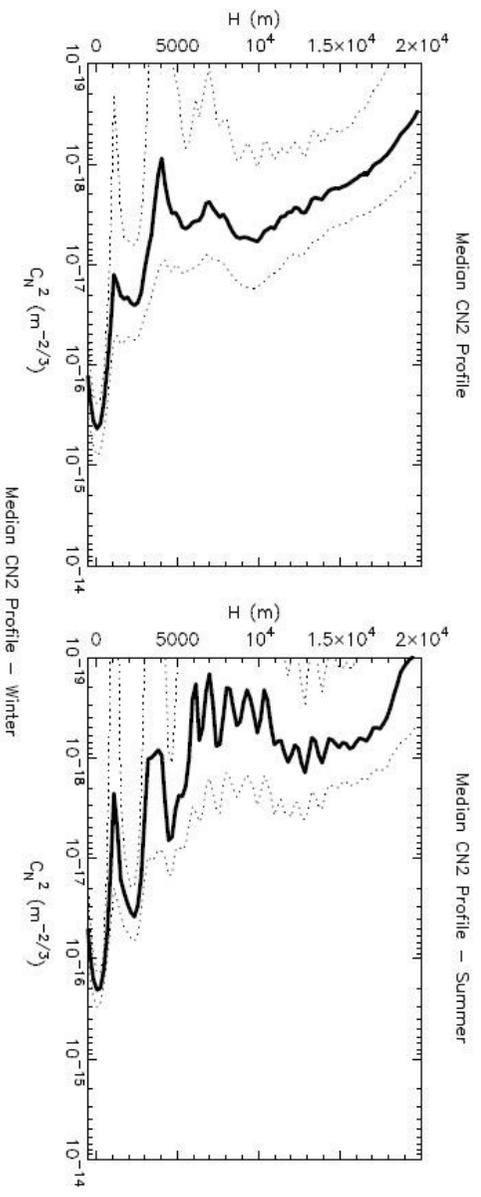
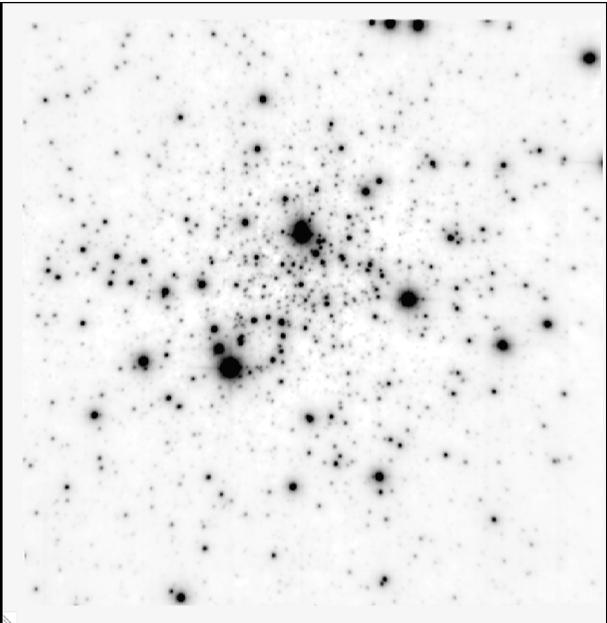


Figure 2. Median  $C_N^2$  profile obtained with the complete sample of 43 nights, the summer [April-June] and winter [October-March] time samples. Results are obtained with the standard GS technique.

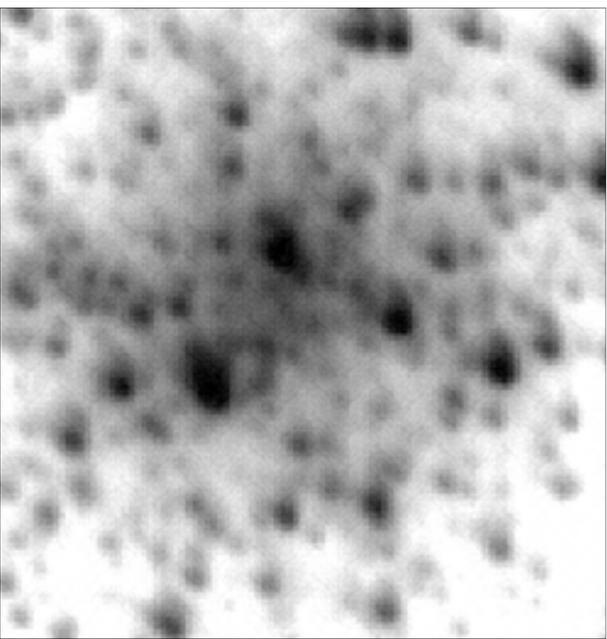
# Why Adaptive Optics?

# Improvement in Resolution and Sensitivity

1. **Angular resolution:**  $\theta = \frac{\lambda}{r_0} \rightarrow \theta = \frac{\lambda}{D} \Rightarrow \text{gain} = \frac{D}{r_0}$
2. **Point source sensitivity:**  $S/N \sim D^2 \Rightarrow \text{gain in } t_{\text{int}} \sim \frac{1}{D^4}$



PHARO LGS Ks image  
500s integ., 40" FOV, 150 mas FWHM

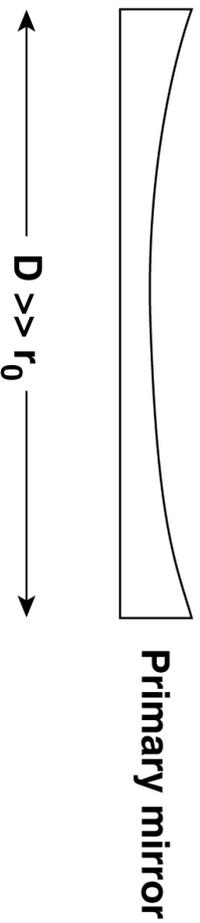


WIRO H image  
Kobulnicky et al. 2005, AJ 129, 239-250

# Basic AO Principle

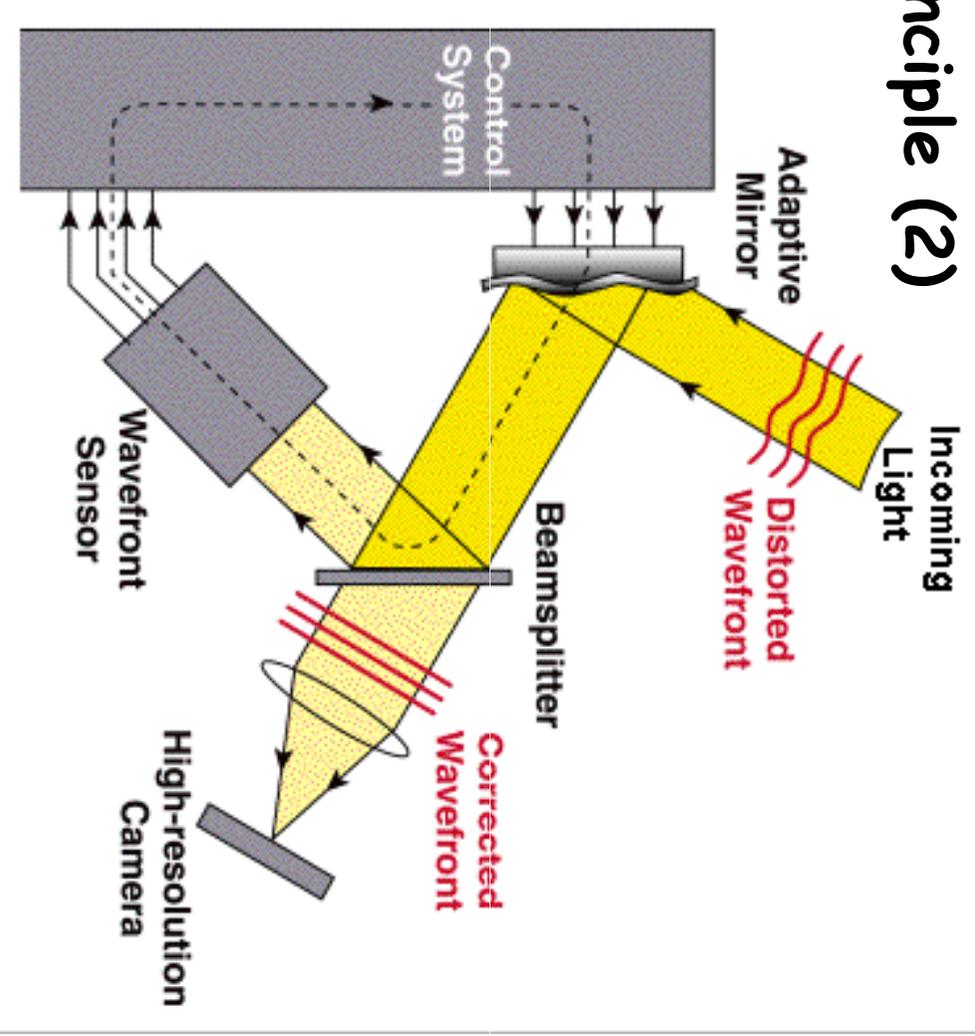
# AO Principle

1. Maximum scale of tolerated wavefront deformation is  $r_0$   
→ subdivide the telescope aperture into  $r_0$ 's
2. Measure the wavefront deformations.
3. Correct the wavefront deformations by "bending back"  
the patches of size  $r_0$ .



The number of subapertures is  $(D/r_0)^2$  at the observing wavelength → can easily require hundreds to thousands of actuators for very large telescopes.

## AO Principle (2)

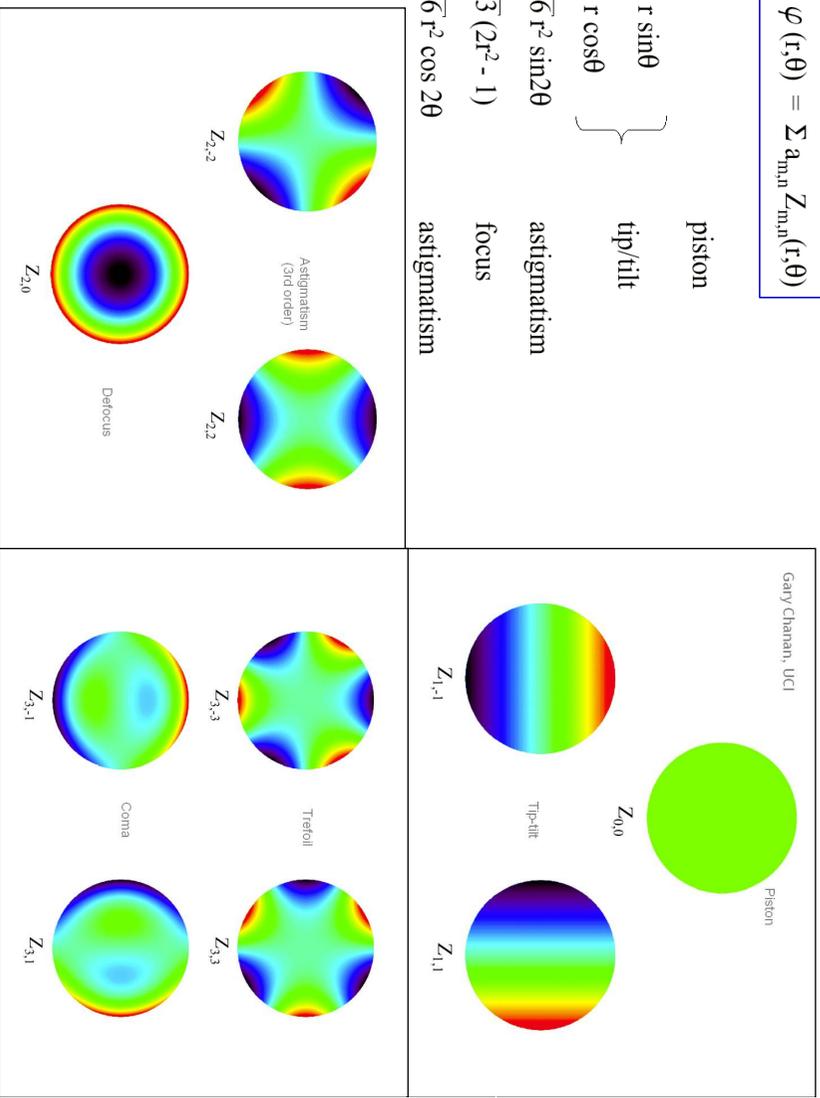


# Wavefront Description: Zernike Polynomials

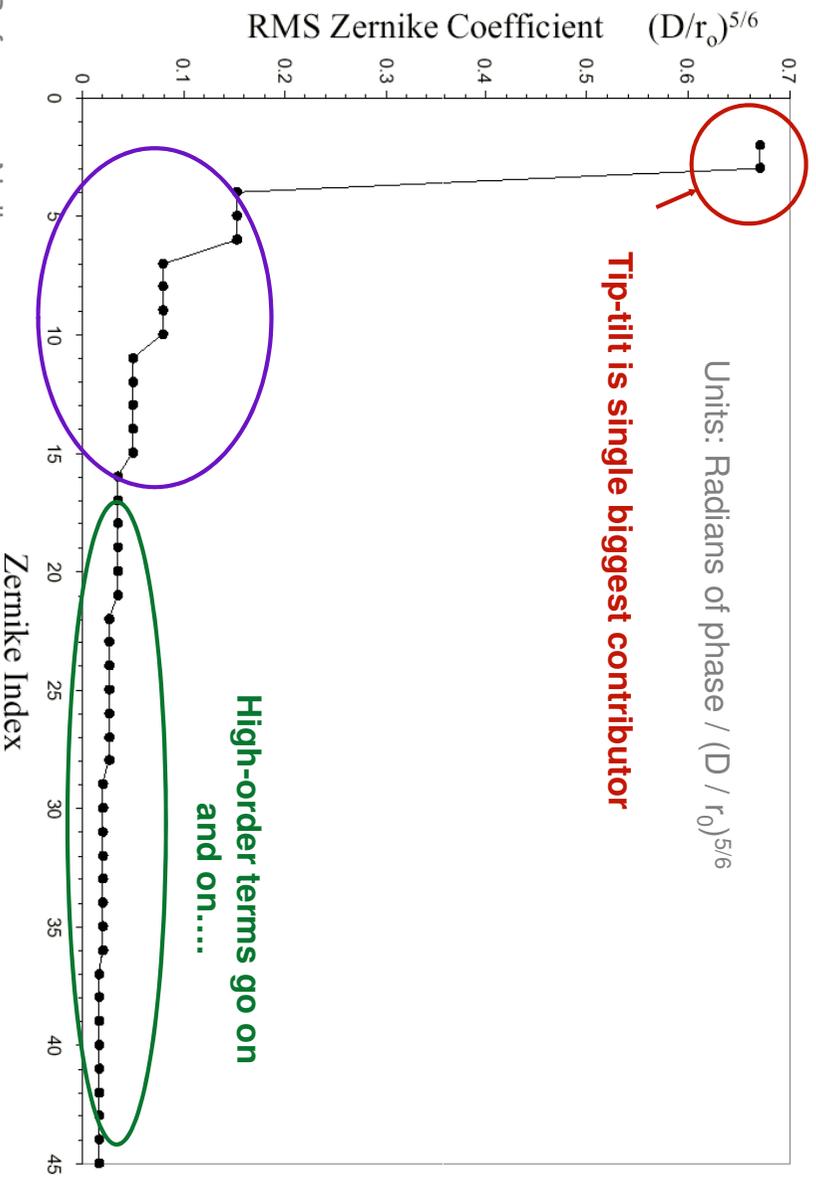
Expansion into a series of orthogonal terms:

$$\varphi(r,\theta) = \sum a_{m,n} Z_{m,n}(r,\theta)$$

- $Z_{0,0} = 1$  piston
- $Z_{1,-1} = 2 r \sin\theta$  tip/tilt
- $Z_{1,1} = 2 r \cos\theta$  tip/tilt
- $Z_{2,-2} = \sqrt{6} r^2 \sin 2\theta$  astigmatism
- $Z_{2,0} = \sqrt{3} (2r^2 - 1)$  focus
- $Z_{2,2} = \sqrt{6} r^2 \cos 2\theta$  astigmatism



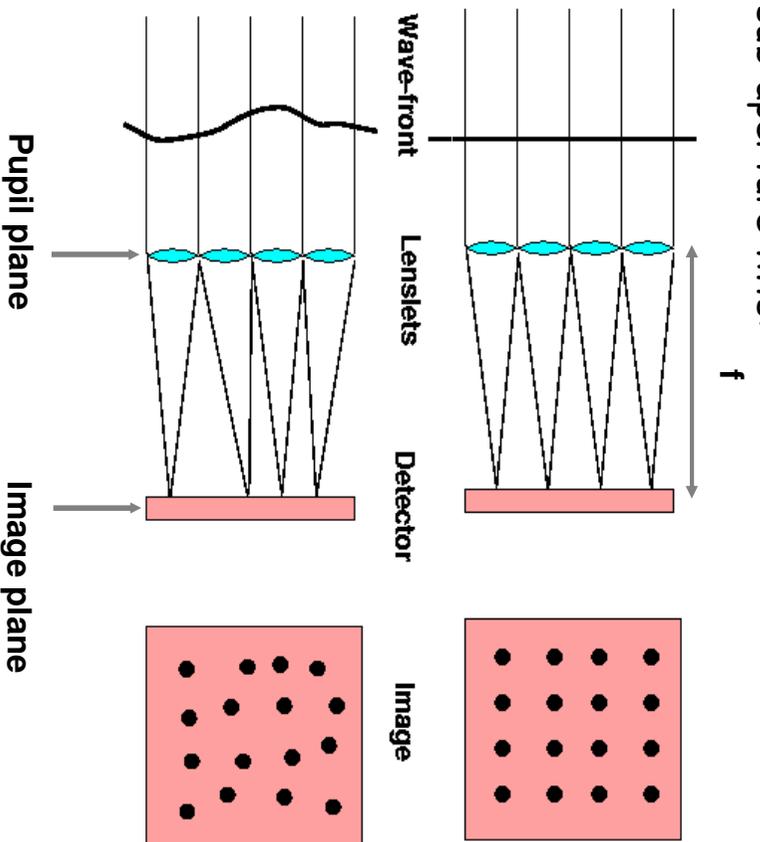
## Tip-Tilt and higher order Terms (1)



# AO – Key Components

## Wavefront Sensors – Shack Hartmann

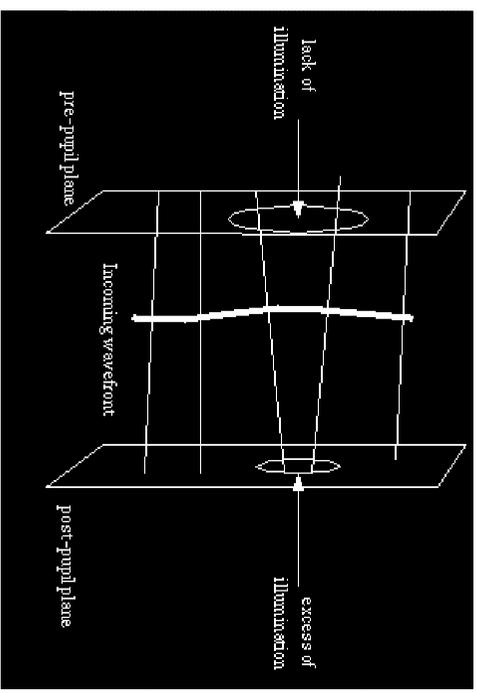
Most common principle is the **Shack Hartmann** wavefront sensor measuring sub-aperture tilts:



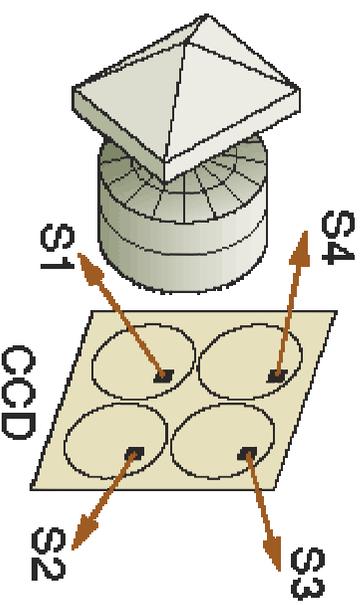
# WFS: Curvature and Pyramid Sensors

Other common principles are the

curvature sensor →

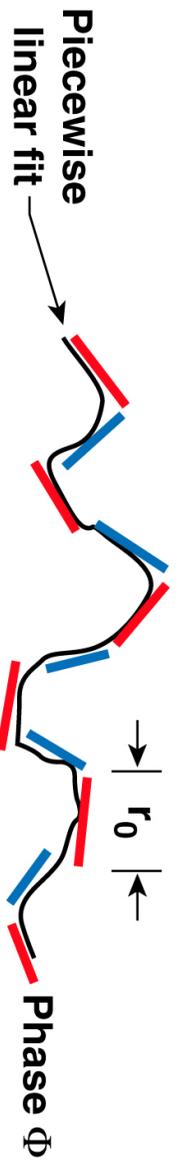


and the pyramid sensor →

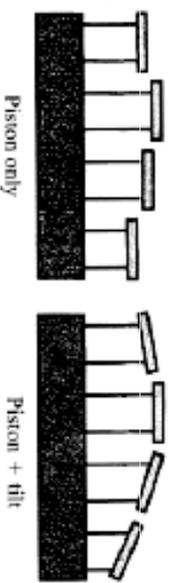


## Deformable Mirrors

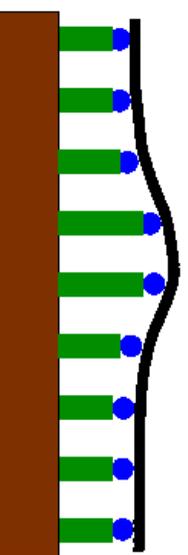
Basic principle: piece-wise linear fit of the mirror surface to the wavefront.  $r_0$  sets the number of degrees of freedom.



Two general types: segmented mirrors



and continuous face-sheet mirrors:



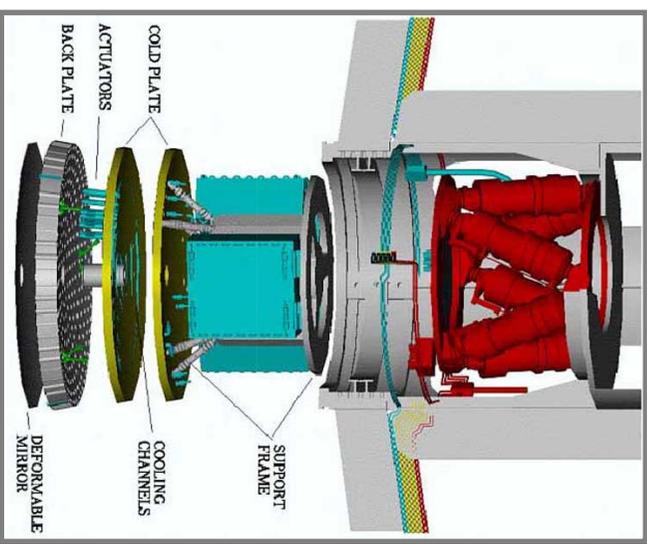
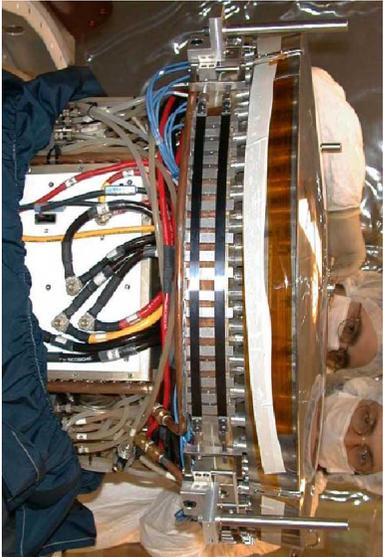
Note that the (piezo) actuator stroke is typically only a couple of micrometers → requires separate tip-tilt mirror.

# Adaptive Secondary Mirrors

Concept: integrate DM into the telescope  
→ **adaptive secondary mirrors**.

Advantages:

- no additional optical system needed → lower emission, higher throughput
- large surface → higher actuator density
- larger stroke → no tip-tilt mirror needed
- ...but also more difficult to build, control, and handle.



DM for MMT Upgrade

# AO Correction Error Terms

# Typical AO Error Terms

- **Fitting errors** from insufficient approximation of the wavefront (finite actuator spacing, influence function of actuators, etc.).

$$\sigma_{fit}^2 \approx 0.3 \left( \frac{D}{r_0} \right)^{5/3}$$

- **Temporal errors** from the time delay between measurement and correction (computing, exposure time).

$$\sigma_{temp}^2 \approx \left( \frac{1}{\tau_0} \right)^{5/3}$$

- **Measurement errors** from the WFS (S/N!)

$$\sigma_{measure}^2 \sim S / N$$

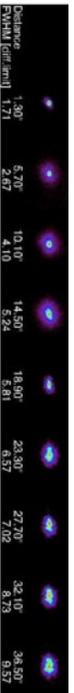
- **Calibration errors** from aberrations in the non-common path between sensing channel and imaging channel.

$$\sigma_{calibration}^2 \sim ???$$

- **Angular anisoplanatism** from sampling different lines of sight through the atmosphere.

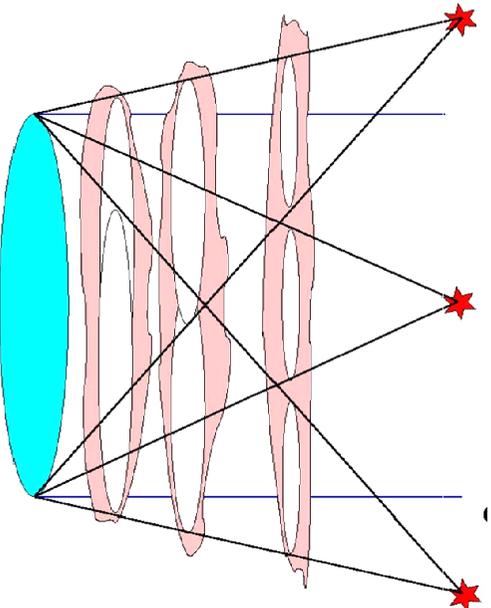
$$\sigma_{aniso}^2 \approx \left( \frac{\theta}{\theta_0} \right)^{5/3}$$

## Angular Anisoplanatism

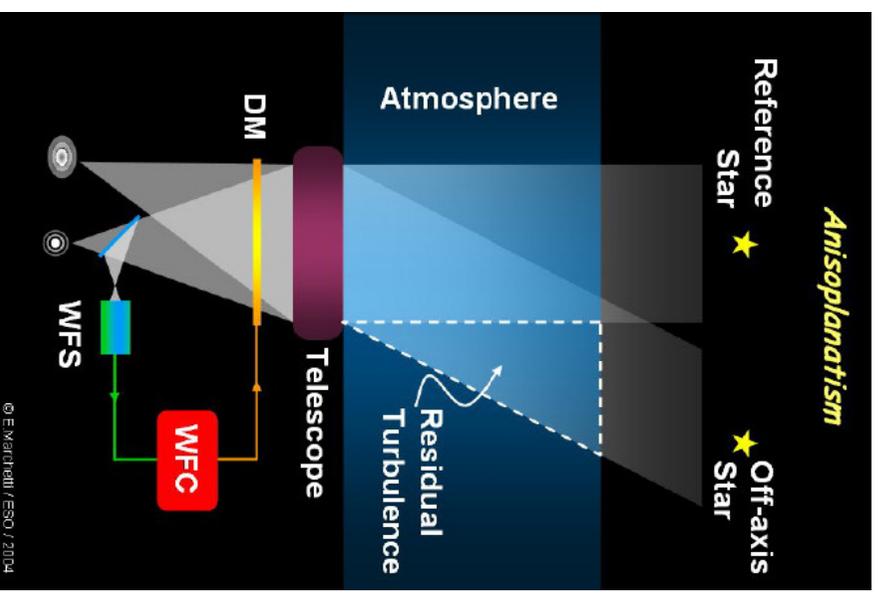


Angular anisoplanatism is a severe limitation to:

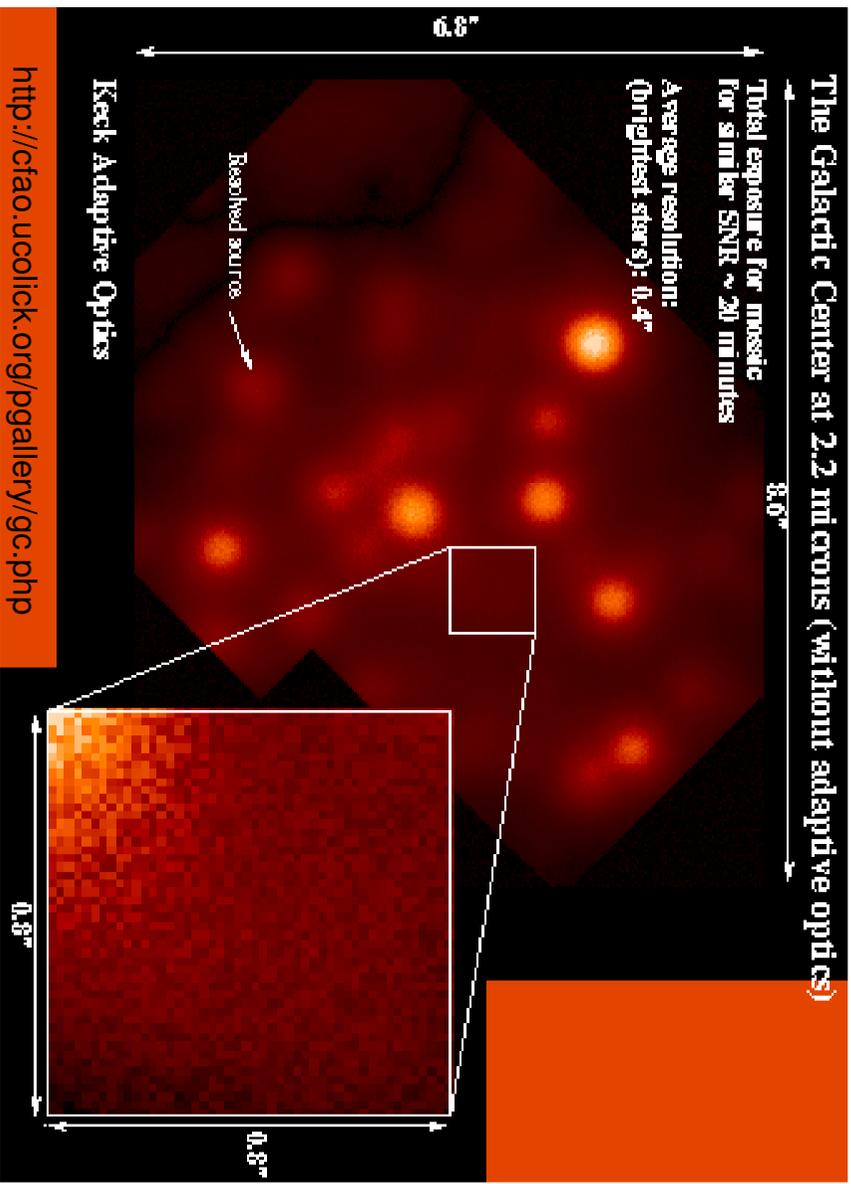
- wide-field imaging
- sky coverage (finding a guide star within the isoplanatic angle)



Multi-LGS allows to fight cone effect AND increase FOV



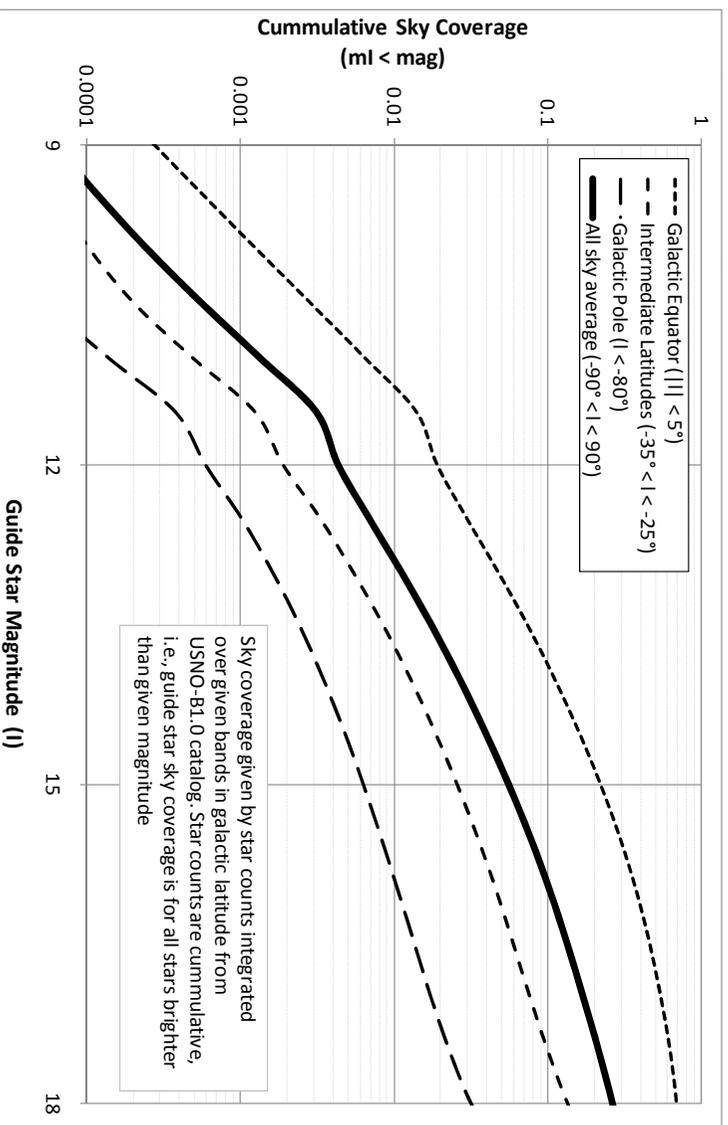
# “Typical” Correction and Residuals



# Laser Guide Stars

# Sky Coverage

To sense the wavefront one needs a bright reference/guide star within the isoplanatic angle.



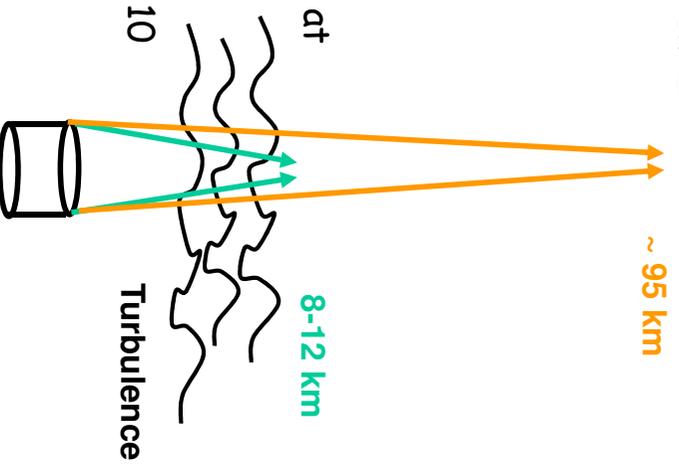
Cumulative sky coverage, i.e., the chance of finding stars brighter than given magnitude, for a random target as a function of I-band magnitude using the USNO-B1.0 catalogue.

## Laser Guide Stars

Solution to the sky coverage problem:  
*create your own guide star.*

Two principle concepts:

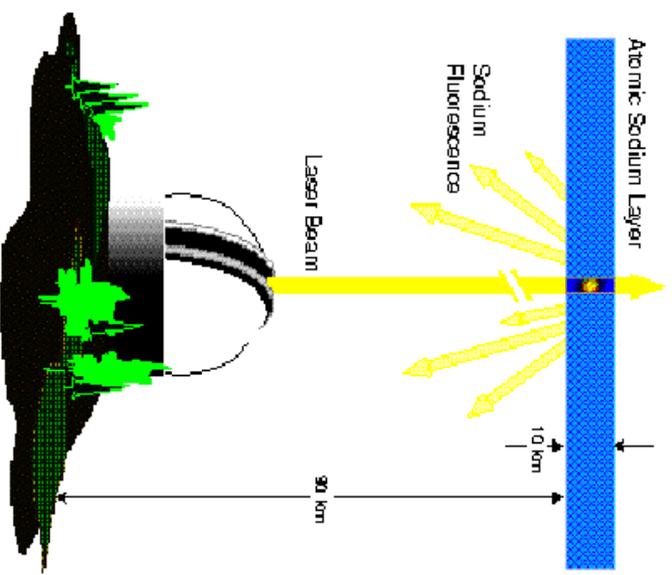
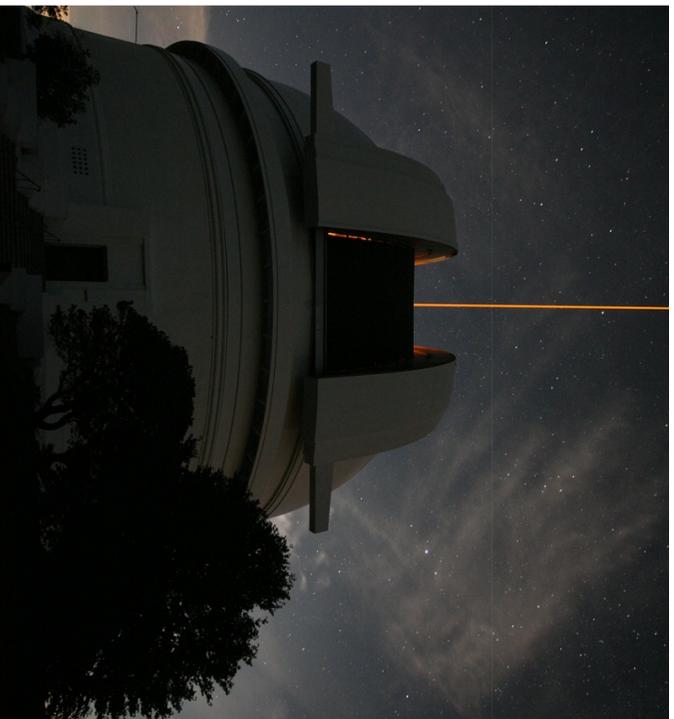
- **Sodium LGS** - excite atoms in "sodium layer" at altitude of  $\sim 95$  km.
- **Rayleigh beacon LGS** - scattering from air molecules sends light back into telescope,  $h \sim 10$  km



Since the beam travels twice (up and down) through the atmosphere, tip-tilt cannot be corrected  $\rightarrow$  LGS-AO still needs a natural guide star, but this one can be much fainter ( $\sim 18$ mag) as it is only needed for tip-tilt sensing.

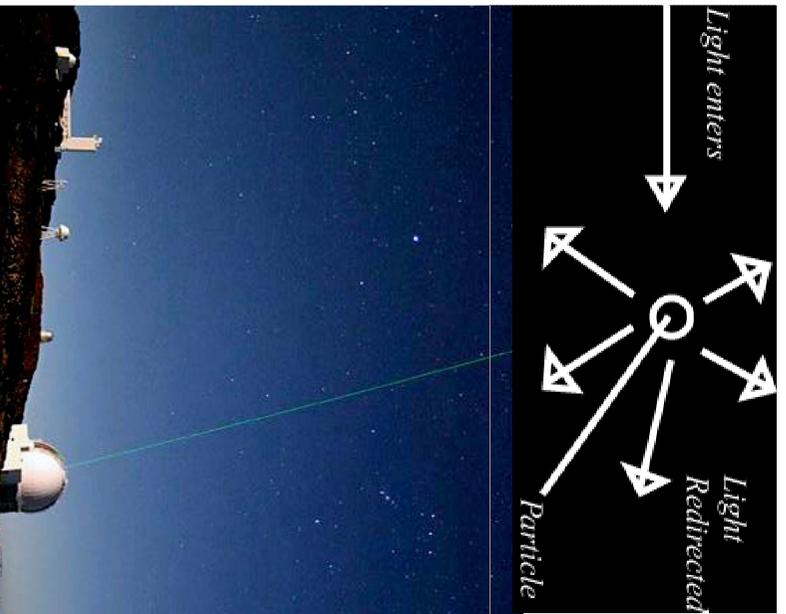
# Sodium Beacons

Layer of neutral sodium atoms in mesosphere (height ~ 95 km, thickness ~10km) thought to be deposited as smallest meteorites burn up. Resonant scattering occurs when incident laser is tuned to D2 line of Na at 589 nm.



# Rayleigh Beacons

Due to interactions of the electromagnetic wave from the laser beam with molecules in the atmosphere.



- Advantages:**
- cheaper and easier to build
  - higher power
  - independent of Na layer

- Disadvantages:**
- larger focus anisoplanatism
  - laser pulses → timing

## Focus Anisoplanatism

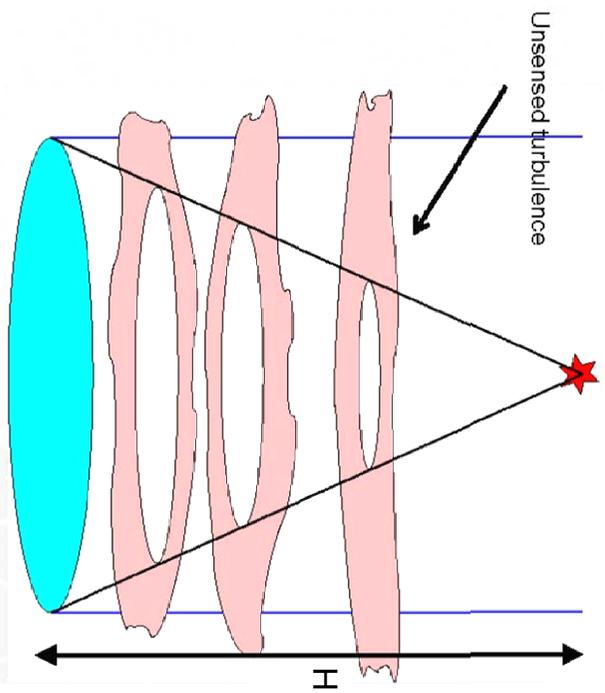
The LGS is at finite distance  $H$  above the telescope and does not sample all turbulence and not the same column of turbulent atmosphere (“cone effect”):

The contribution to the wavefront error contribution from focus

$$\text{anisoplanatism is: } \sigma_{FA}^2 = \left( \frac{D}{d_0} \right)^{5/3}$$

where  $d_0 \sim \lambda^{6/5}$  depends only on wavelength and turbulence profile at the telescope site.

→ very large telescopes need multiple LGSs due to this cone effect.

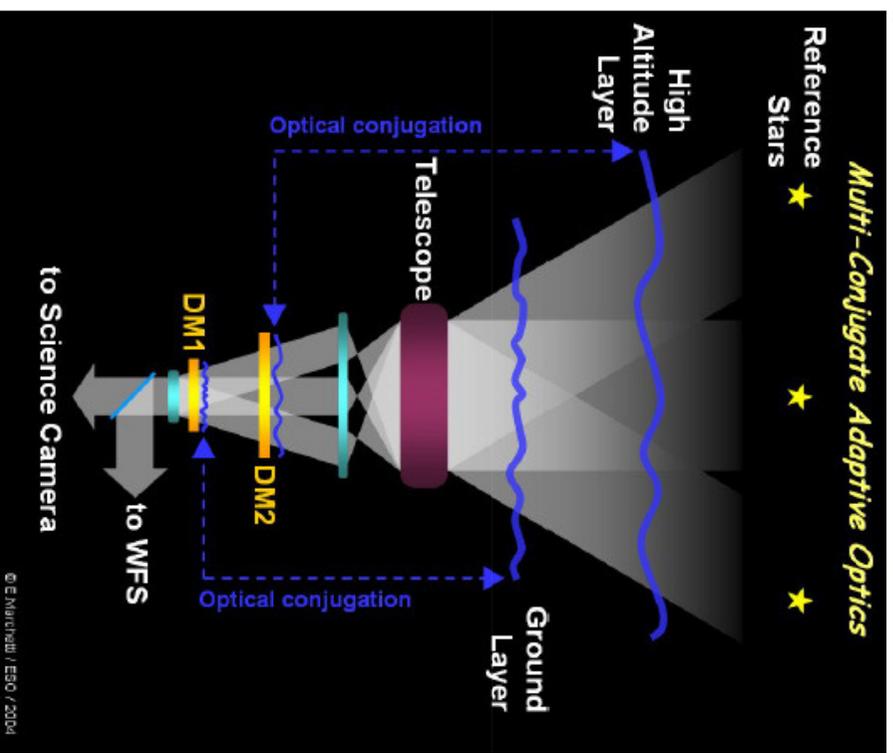


# More Types of AO Concepts

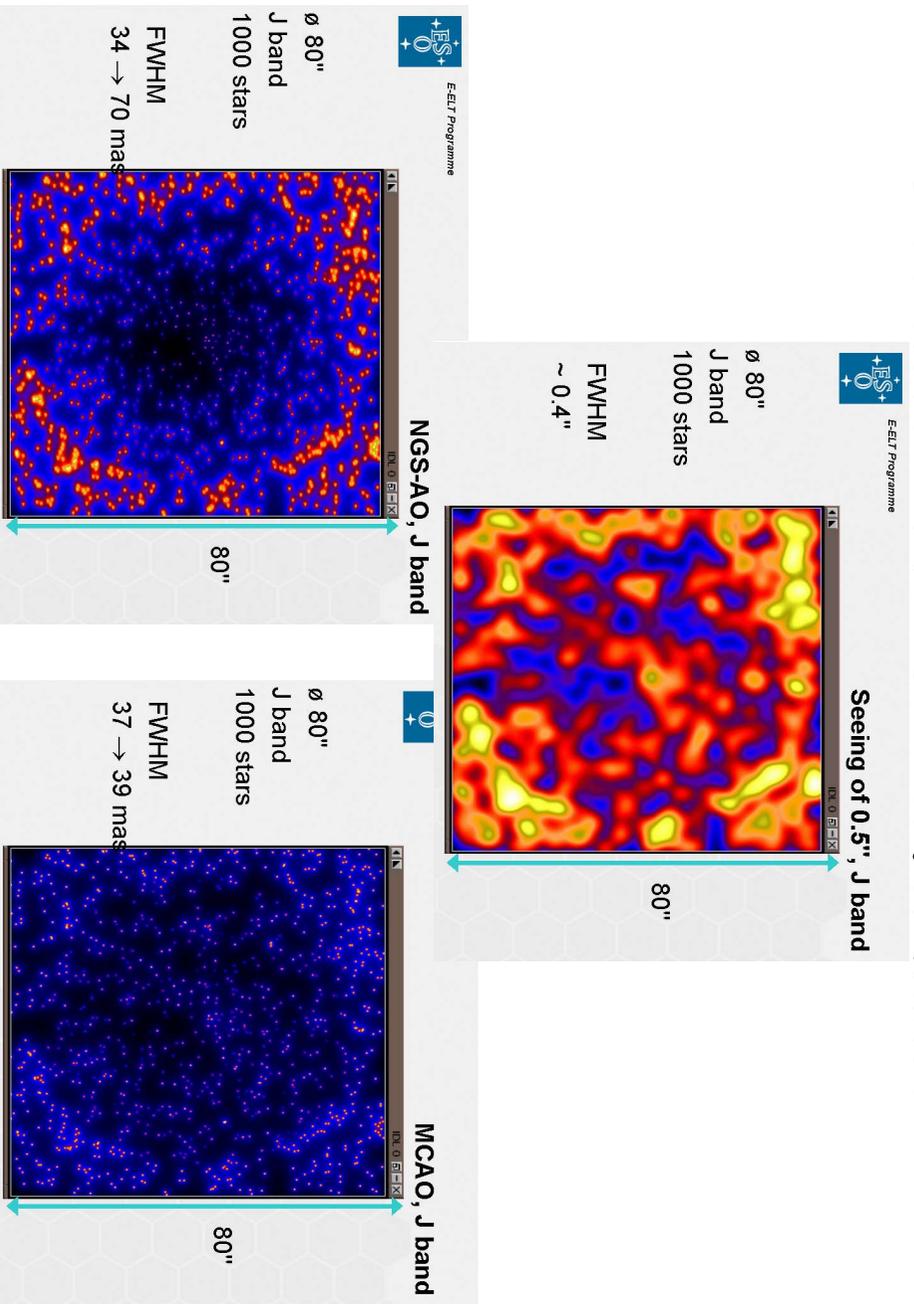


# Multi-Conjugate AO - MCAO

- to overcome anisoplanatism, the basic limitation of single guide star AO.
- MCAO uses multiple NGS or LGS.
- MCAO controls several DMS
- each DM is conjugated to a different atmospheric layer at a different altitude
- at least one DM is conjugated to the ground layer
- best approach to larger corrected FOV.

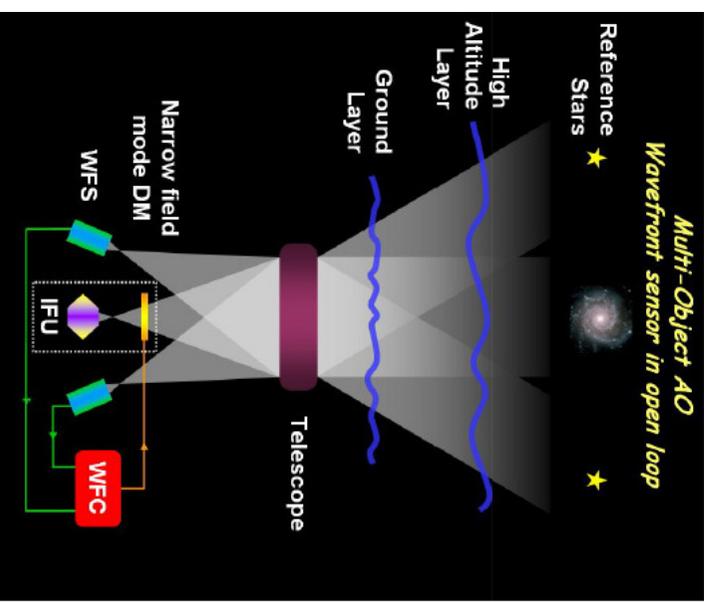
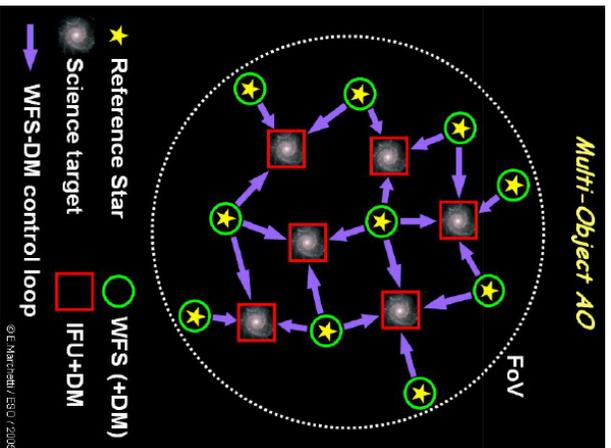


## Side note: MCAO: Performance



# Multi-Object AO - MOAO

- MOAO provides **correction** not over the entire FOV of several arcmin but **only in local areas** within several arcmin → **multi-object spectroscopy**.
- needs (several) **guide stars** close to each science target.
- picks up the WFS light via small "arms" inserted in the FOV.
- **each science target has its DM**
- systems work in **open loop (i)**



# Extreme AO - XAO

- XAO is configured **similarly** than SCAO
- high Strehl **on-axis** and **small corrected FOV**
- however, Strehl values in excess of 90%
- requires **many thousands of DM actuators**
- requires to minimize optical and alignment errors
- main application: **search for exoplanets**, like with SPHERE on the VL T →

