

Exercises Astronomical Observing Techniques, Set 8

Exercise 1

There are two different ways to operate a CCD: in front and in back illumination mode (see figure below). In front illumination, the metal electrode is replaced by heavily doped silicon (since pure metal would block the incoming photons), but it is still not transparent in blue and UV wavelengths. Therefore, for detectors used at short wavelengths, back illumination is used.

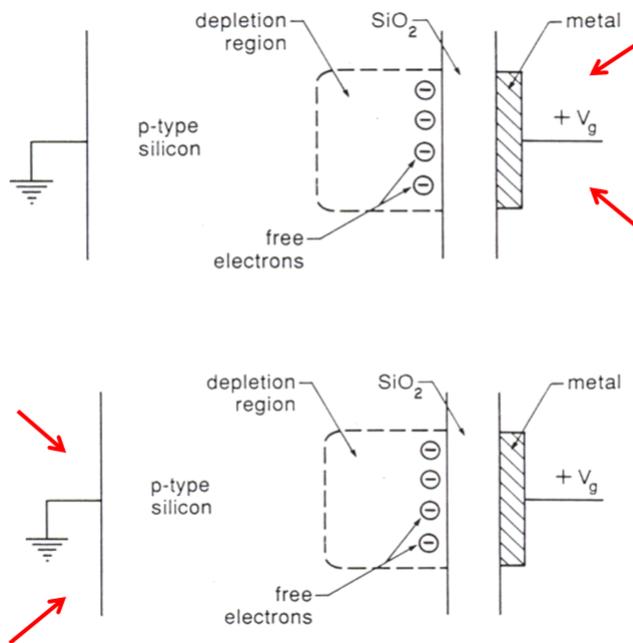


Figure 1: Front (top) and back illuminated (bottom) CCDs, arrows indicate the incoming photons.

- Although the absorption of UV/blue photons in the p-type silicon is efficient, the quantum efficiency of a back illuminated CCD, as illustrated in the above figure, is generally low. Please explain the reason.
- Some CCD manufacturers sell “thinned CCDs” where the thickness of the p-type silicon is reduced. Explain the objective of the “thinning” and provide some considerations on minimum/maximum thickness.

Exercise 2

How do you think a color image can be produced with a CCD (like in a pocket camera)? Describe at least two different solutions.

Exercise 3

- a) For what wavelength range is a bolometer preferentially used? Why don't we use it at other wavelength ranges?
- b) For which two reasons is the operation and production of a bolometer more difficult than the CCD?

Exercise 4

- a) Determine a suitable local oscillator frequency (LOF) for the WSRT radio telescope operating a 1.4 GHz, where we would like to down-convert the signal to a 50 MHz carrier.
- b) An instrument uses high frequency heterodyne receiver operating a 300 GHz with a system temperature (T_{sys}) of 30 K. We want to increase the sensitivity of the instrument. What properties of the receiver do we need to change to achieve this?
- c) same as b) but now for a system temperature of 14.4 K.

Exercise 5

The Fermi distribution for the probability of finding an electron with an energy E in a given physical system is given by:

$$f(E) = \frac{1}{1 + e^{(E-E_F)/kT}} \quad (1)$$

- a) What is the probability of finding an electron in the conduction band at zero temperature? Can you explain this in terms of physics?
- b) What is the probability of finding an electron with the Fermi energy at zero temperature? And at 100 K? What does this imply about the Fermi energy? Make a drawing of $f(E)$ for $T=0$ and $T>0$.

The Fermi distribution gives a probability, but in a physical system, each energy has several states associated with it. To account for the actual number of electrons within an energy range dE , we need to know the density of states $N(E)$. The concentration of electrons n_0 in the energy range $[E_1, E_2]$ is

$$n_0 = \int_{E_1}^{E_2} f(E)N(E)dE \quad (2)$$

For the conduction band, $N(E)$ can be derived as

$$N(E) = \frac{1}{2\pi^2} \left(\frac{2m_{eff}}{\hbar^2} \right)^{3/2} (E - E_c)^{1/2} \quad (3)$$

with $\hbar = h/2\pi$.

- c) Which famous equation do you use to derive a density of states?
- d) What are (E_1, E_2) for the electron concentration in the conduction band?

e) Show that in the limit where $E - E_F \gg kT$, the concentration of electrons is given by:

$$n_0 = 2 \left(\frac{2\pi m_{eff} kT}{h^2} \right)^{3/2} e^{(E_F - E_c)/kT} \quad (4)$$

Tip:

$$\int_0^\infty x^{1/2} e^{-ax} dx = \frac{\sqrt{\pi}}{2a\sqrt{a}} \quad (5)$$

f) The bandgap energy for pure silicon is 1.11 eV. What is $E_c - E_F$, using the definition of the Fermi energy?

g) Calculate the electron concentration in the conduction band at $T = 300\text{K}$ and $T = 30\text{K}$ for a “pixel” of volume 1 mm^3 . Note that m_{eff} for silicon is $\sim 1.1 m_e$.