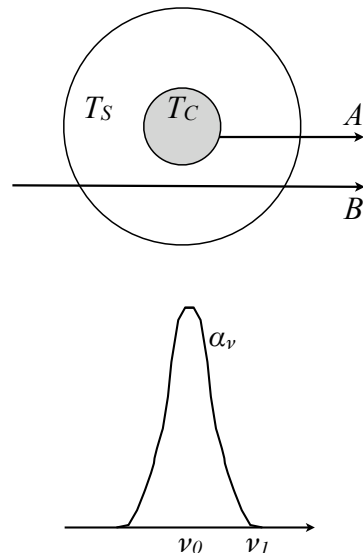


## 1 Shell around an object

Suppose a spherical and opaque object emitting as a blackbody at temperature  $T_c$  is surrounded by a spherical shell of material that is thermally emitting at a temperature  $T_s$  ( $T_s < T_c$ ). This shell absorbs in a narrow spectral line, i.e. its absorption coefficient becomes large at the frequency  $\nu_0$  and is negligible at other frequencies  $\nu_1$ ,  $\alpha_{\nu_0} \gg \alpha_{\nu_1}$ . The object is observed at  $\nu_0$  and  $\nu_1$  and along two different lines of sight A and B (see figure). Assume that the Planck function does not vary appreciably from  $\nu_0$  to  $\nu_1$ .



1. At which frequency will the observed brightness be larger when observed along A? And along B?
2. Now assume  $T_s > T_c$ : answer the same question.

## 2 Forbidden lines vs. permitted lines

The optical spectra of laboratory plasma's are characterized by allowed transitions, while for interstellar plasma's, forbidden lines are prominent. HII regions are a case in point. Explain this difference. In what interstellar environment do you expect that allowed recombination lines will far outshine forbidden transitions?

## 3 Saha-Boltzmann equation

The LTE version of the Saha equation is

$$\frac{n_p n_e}{n_n} = \left( \frac{2\pi m_e kT}{h^2} \right)^{3/2} \frac{1}{n^2} e^{-\chi_n/kT}, \quad (1)$$

where  $\chi_n = 13.6\text{eV}/n^2$ , and assume that  $n_e = n_p$ .

1. Evaluate the constants in this relation.
2. For hydrogen, for  $T = 5000\text{K}$ ,  $10^4\text{K}$ , and  $2 \times 10^4\text{K}$ , determine the ratio of populations in the  $n = 1$  and  $n = 100$  states with respect to the number of ions (i.e. the left hand side of the relation). From these results can you explain why the Orion nebula is fully ionized given that the temperature of the gas is  $8000\text{K}$ ?

## 4 Strömngren sphere (I)

The Strömngren spheres around two stars emitting  $10^{47}$  and  $10^{49}$  UV photons/s are observed to be in pressure equilibrium with their surroundings. What is the ratio of the interstellar gas densities around the two stars if the Strömngren spheres have identical radii? Assume that the temperature of the interstellar gas is the same in both cases.

## 5 Strömngren sphere (II)

Consider a Strömngren sphere of radius  $R_S = 10\text{pc}$  and internal density  $n_e = 10^6\text{m}^{-3}$  with a central ionizing source of  $10^{49}$  photons/s.

1. How long will it take to become neutral once the ionizing star has switched off?
2. Suppose that the sphere expands at a rate equal to the sound speed in a fully ionized  $10^4\text{K}$  gas. How long will it take to expand to a size of  $100\text{pc}$ ?

## 6 HII regions

1. Describe qualitatively the ionization structure and energy balance of HII regions, focussing on the Strömgren sphere, the neutral fraction, the ionization front, and the effects of helium, trace species, and dust.
2. Describe the emission characteristics of HII regions.
3. Describe how the observed spectra of HII regions can be analysed to determine the physical characteristics of the gas and ionizing star. (See Figure 1 for an example spectrum.)