What's cooking

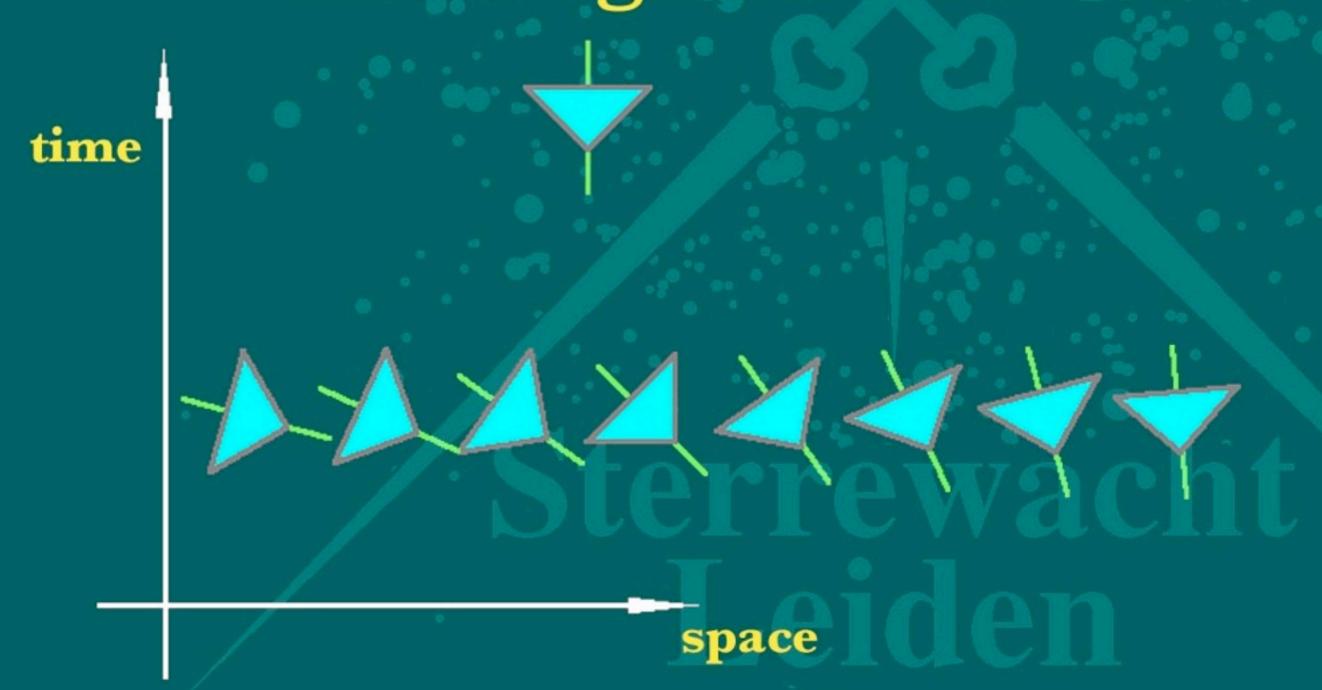
- (Non)relativistic behaviour
 - ♦ Consequences of v=Hr
 - ♦ v~c and acceleration -> GRT
 - ♦ Metric theory, metric tensor
 - ♦ Second-order derivatives
 - ♦ Connection with Newton -> Einstein Eqs
- The connection with Lagrangian theory: local Lorentz symmetry
- H&I specialization: Friedmann Equations

Local Light Cones

Example: the Schwarzschild Black Hole

Sterrewach Leiden

Building Spacetime with Light Cones



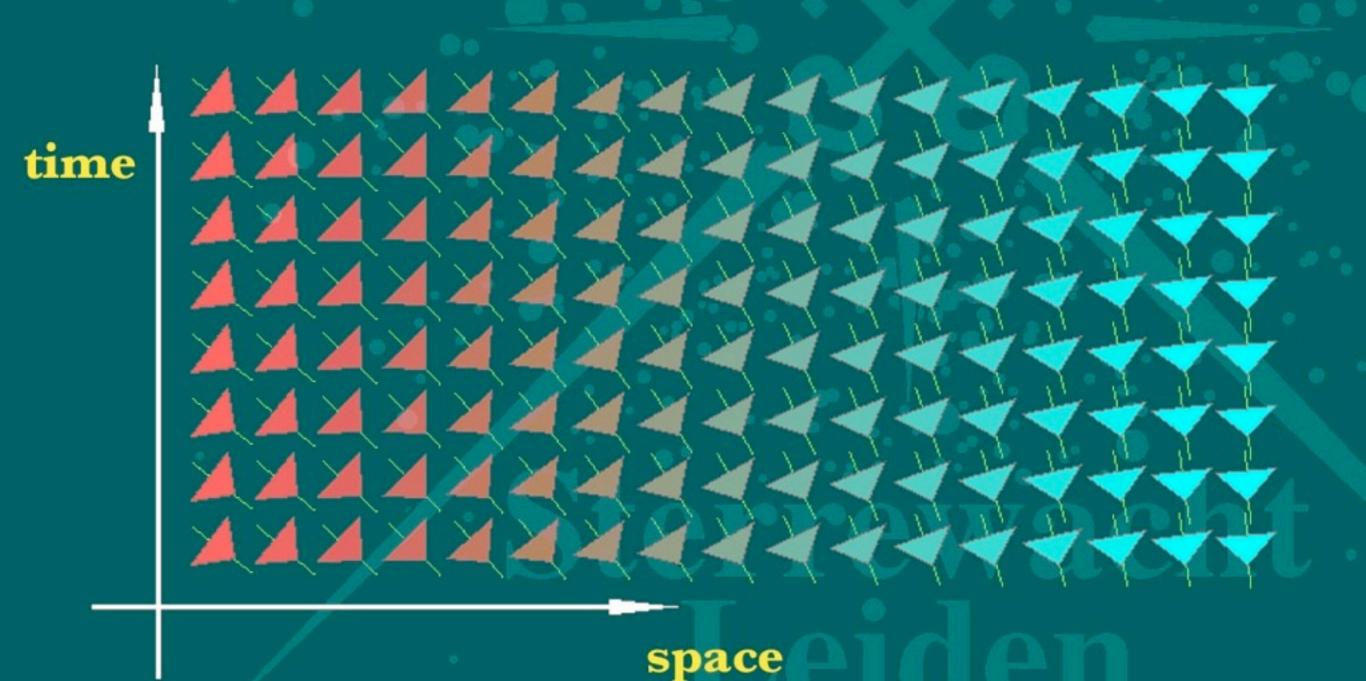
$$ds^2 = \left(1 - rac{1}{r}
ight)c^2 dt^2 - \left(1 - rac{1}{r}
ight)^{-1} dr^2$$

If α is the angle between the axis of the light cone and the direction of the global t-axis, we have

$$an lpha = rac{1}{1-2r}$$

Sterrewacht Leiden

Schwarzschild Black Hole

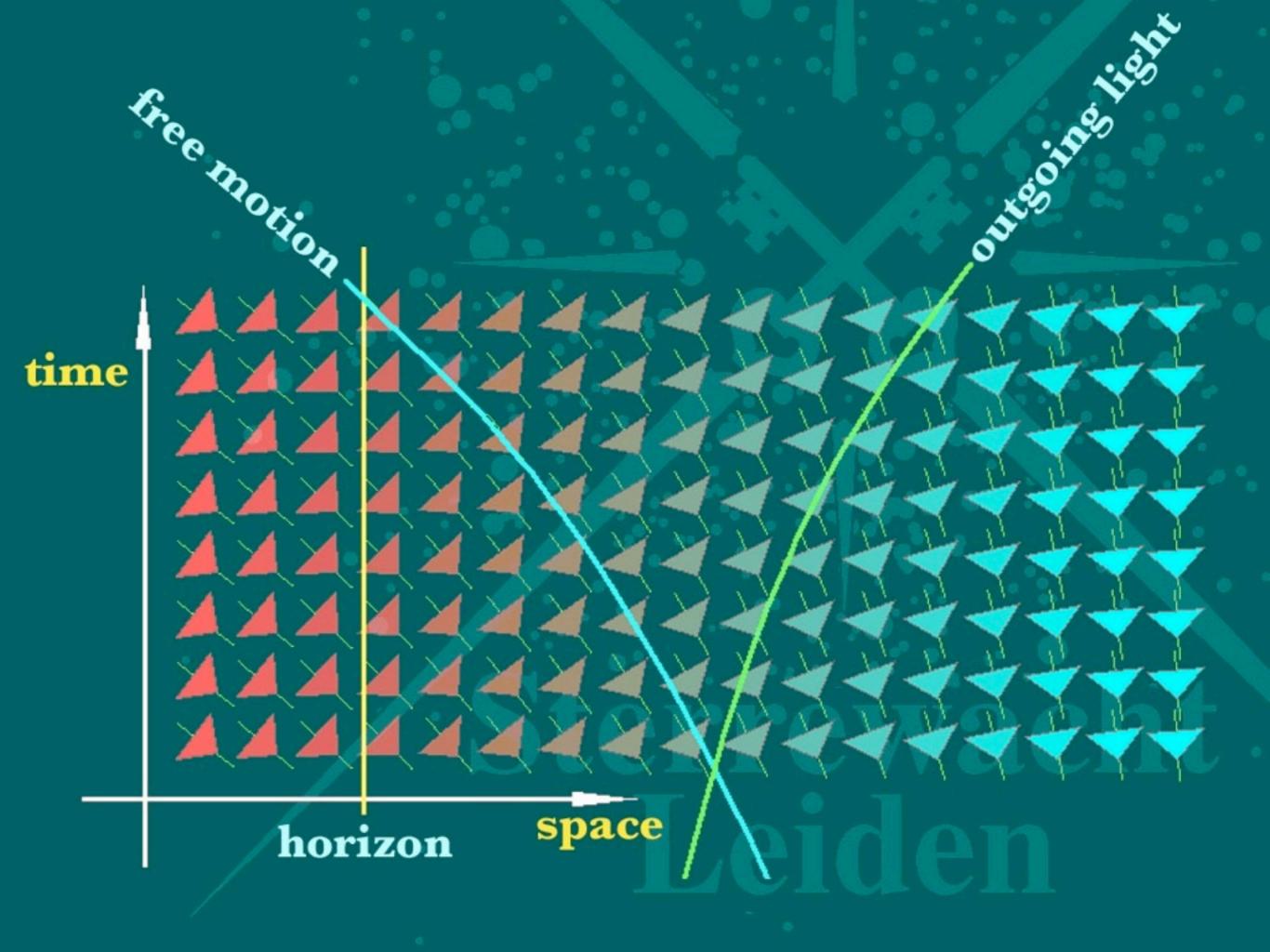


$$ds^2 = \left(1 - \frac{1}{r}\right)c^2 dt^2 - \left(1 - \frac{1}{r}\right)^{-1} dr^2$$

Path of a light ray: ds = 0, so that

$$ds \propto \sqrt{rac{r}{r-1}} dr$$

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$$ds \propto \sqrt{rac{r}{r-1}} dr$$

$$r = (\cosh \chi)^2$$

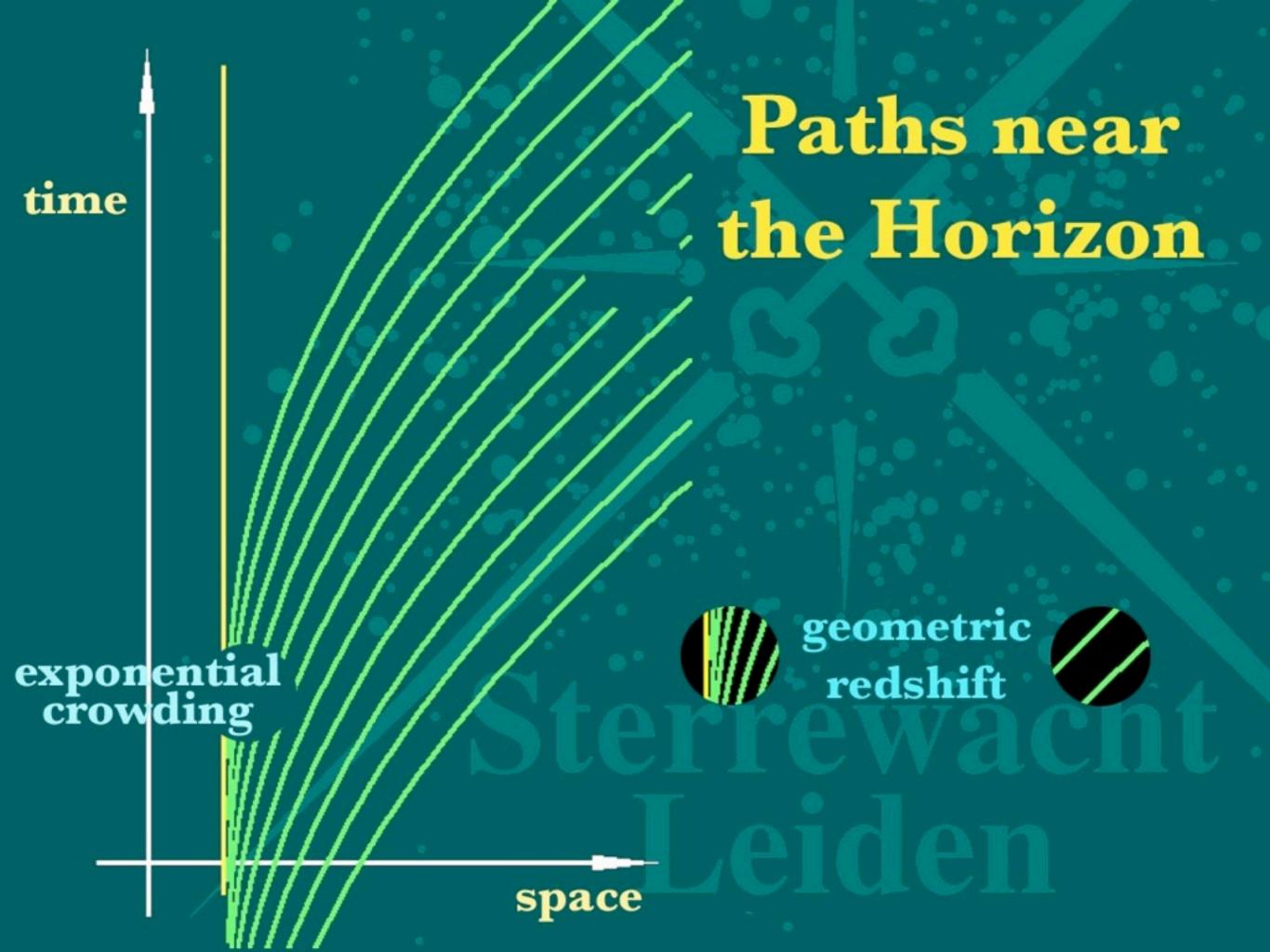
$$ds = 2 \left(\cosh\chi\right)^2 d\chi$$

$$s = \sinh \chi \cosh \chi + \chi$$

$$s = \sqrt{r^2 - r} + \log(2r - 1 + 2\sqrt{r^2 - r})$$

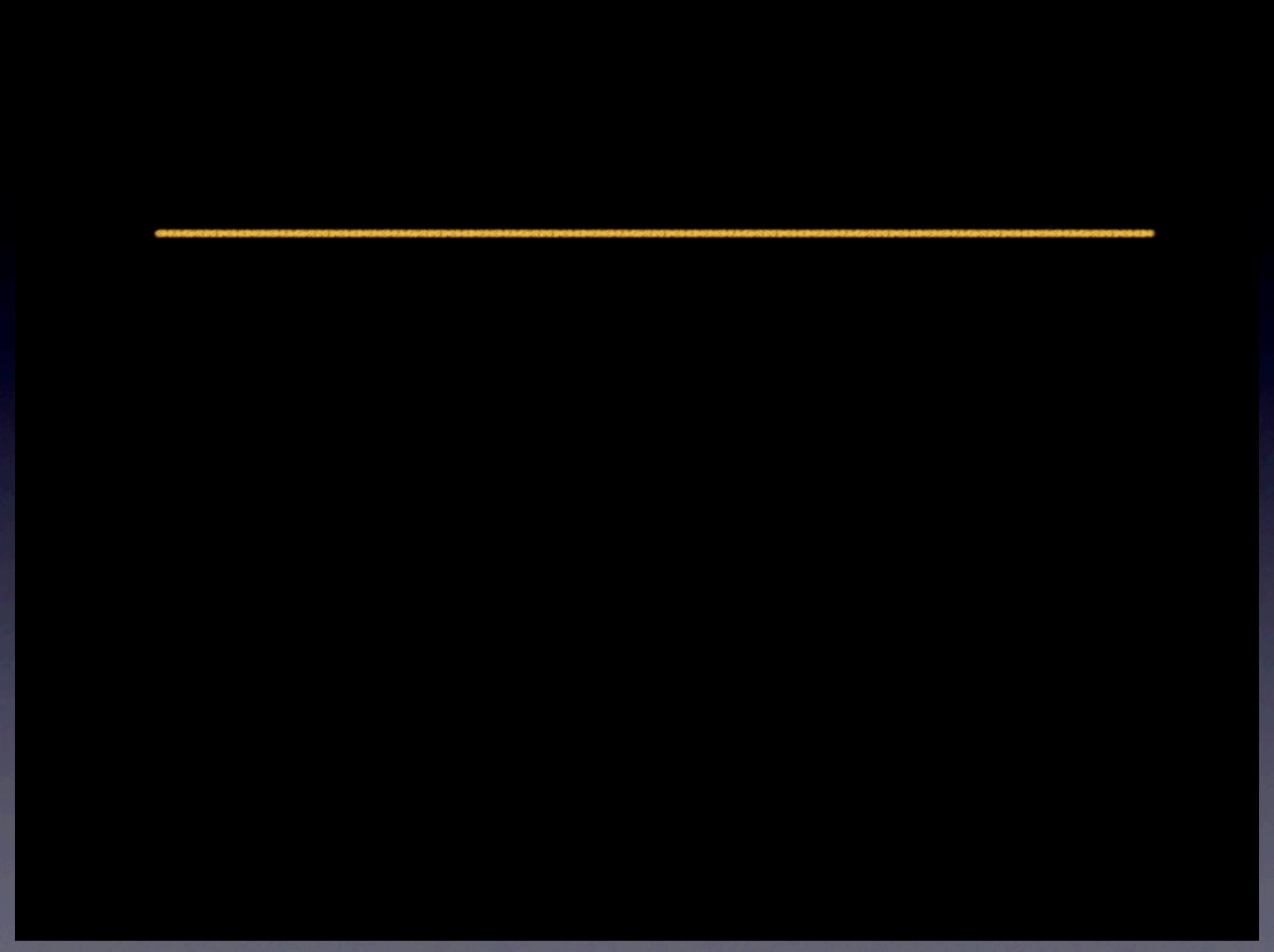
Light Paths time space

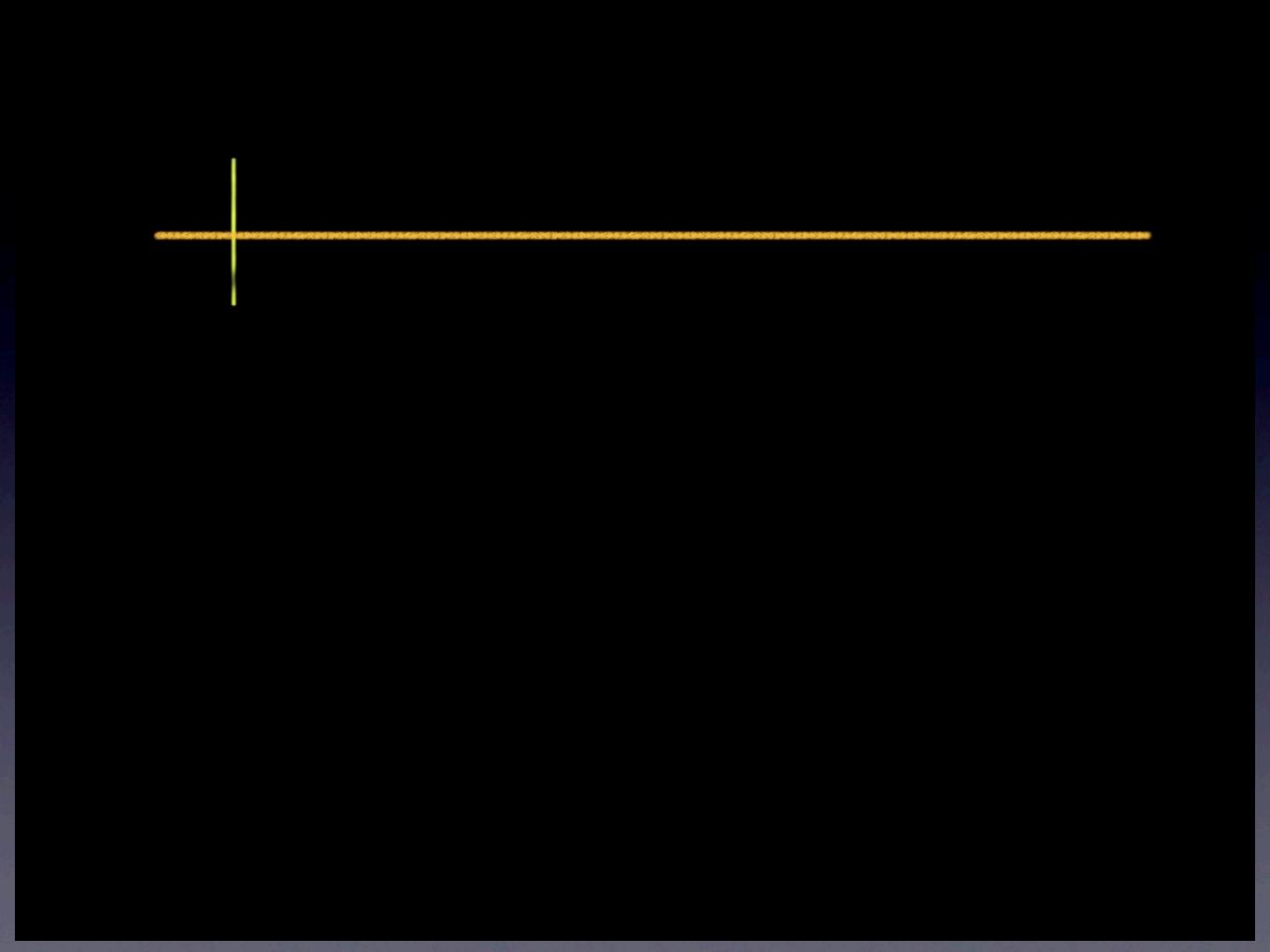
Light Paths time geometric redshift space

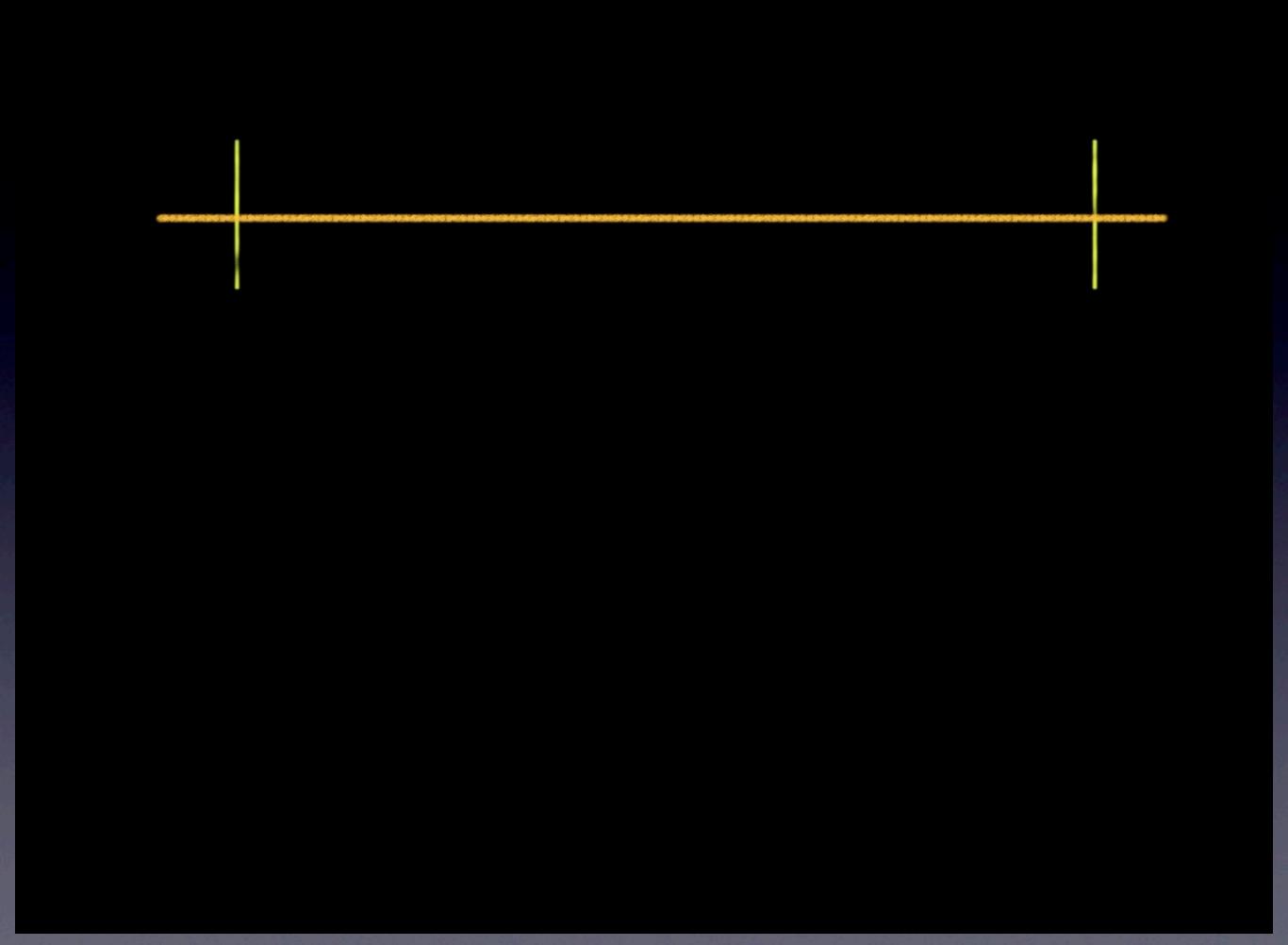


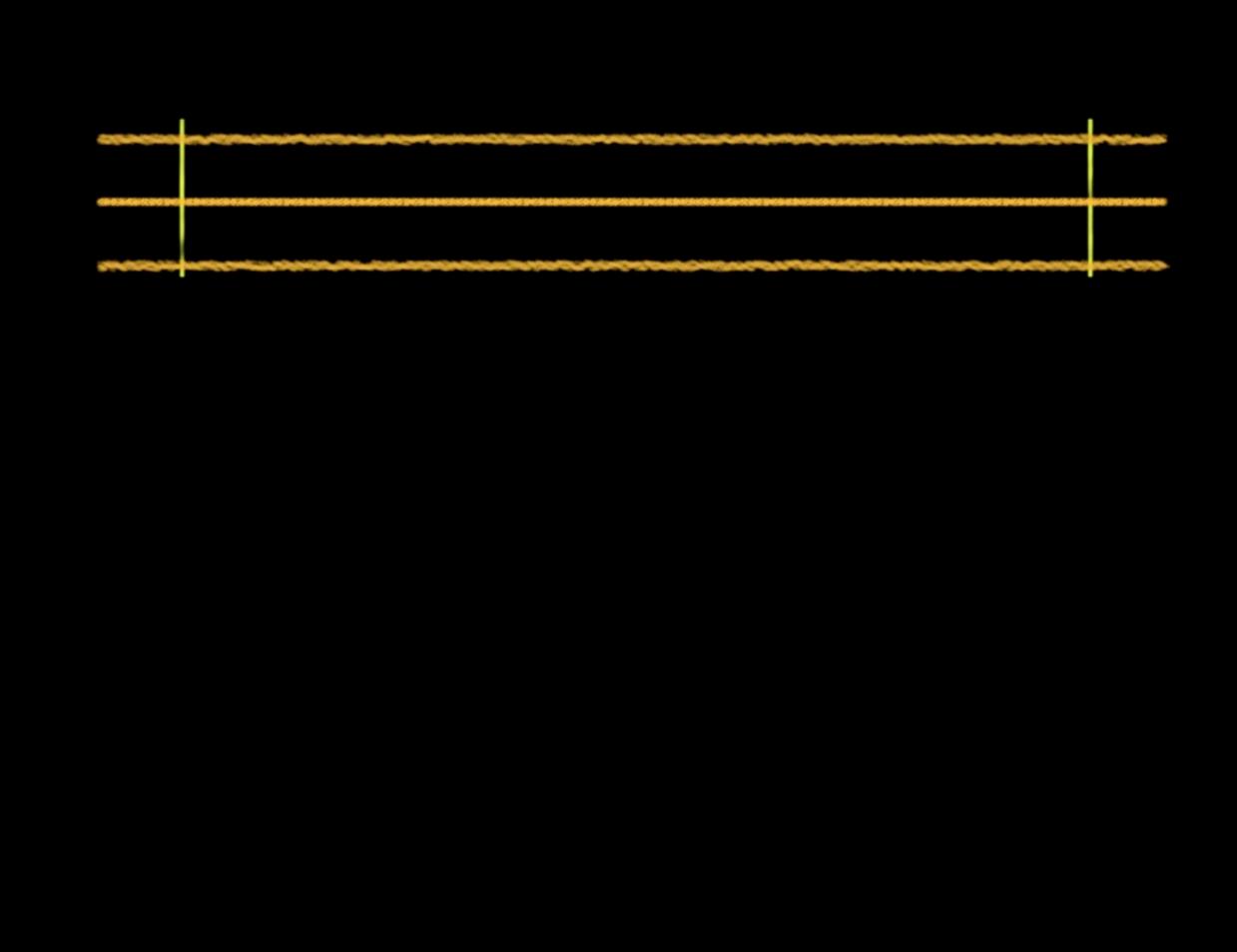
Gravitational Redshift

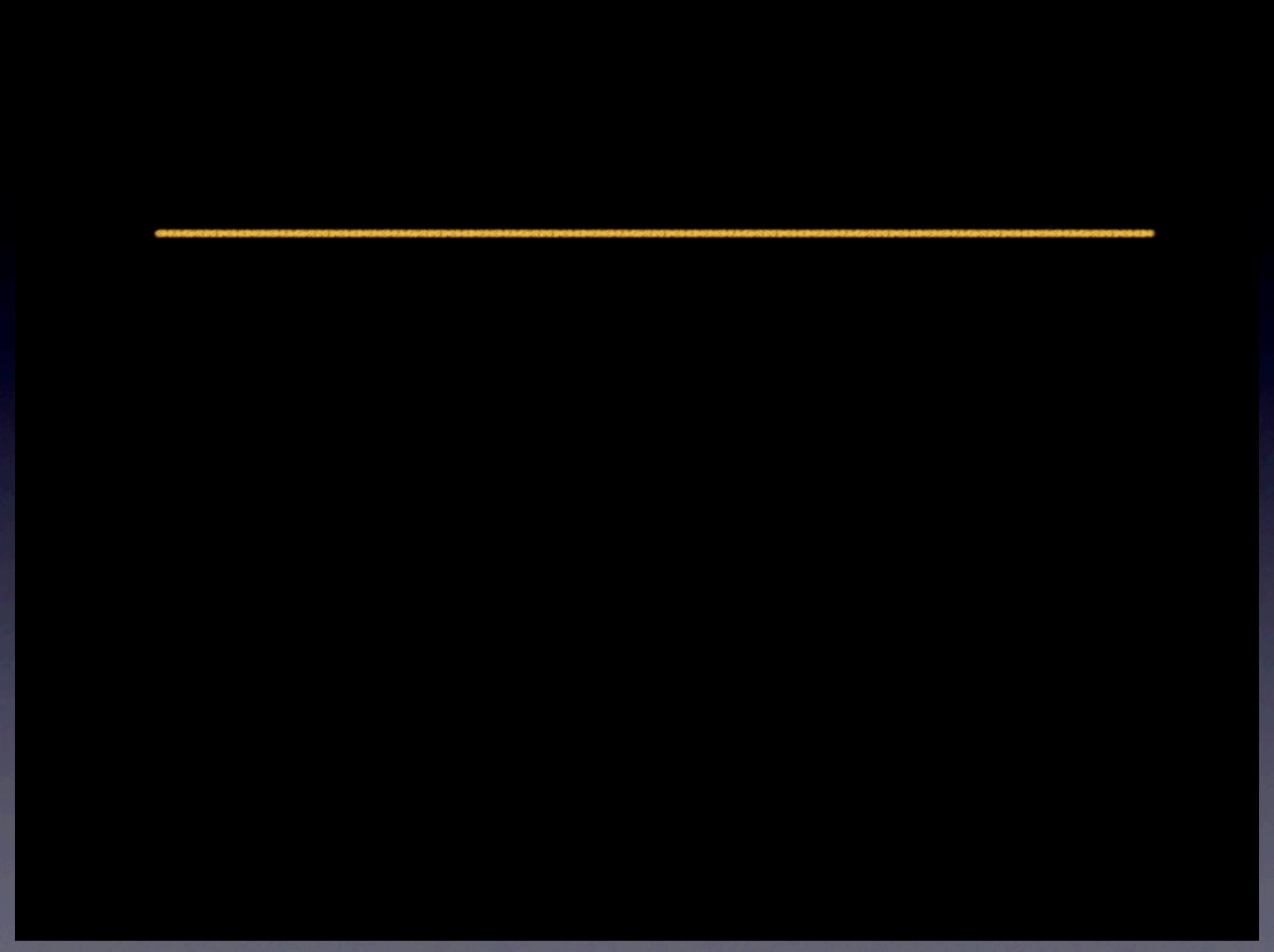
- An external observer sees time running more slowly when looking into a potential well
- Consequences for the CMBR
- Unique time only in a H&I universe

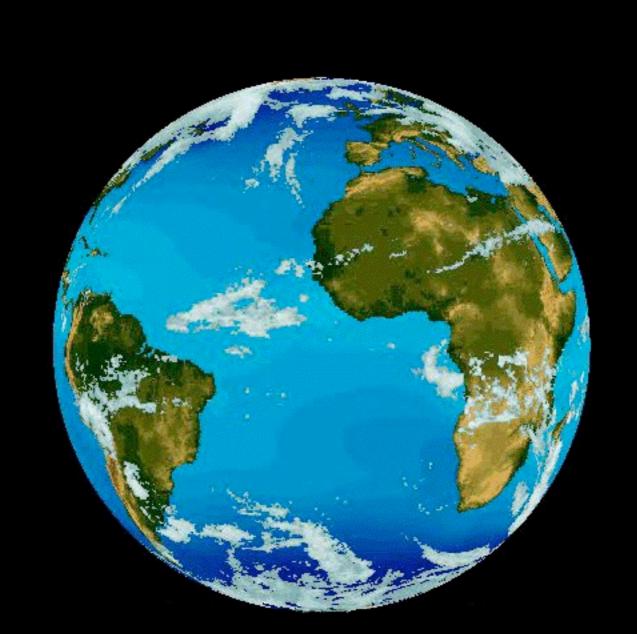


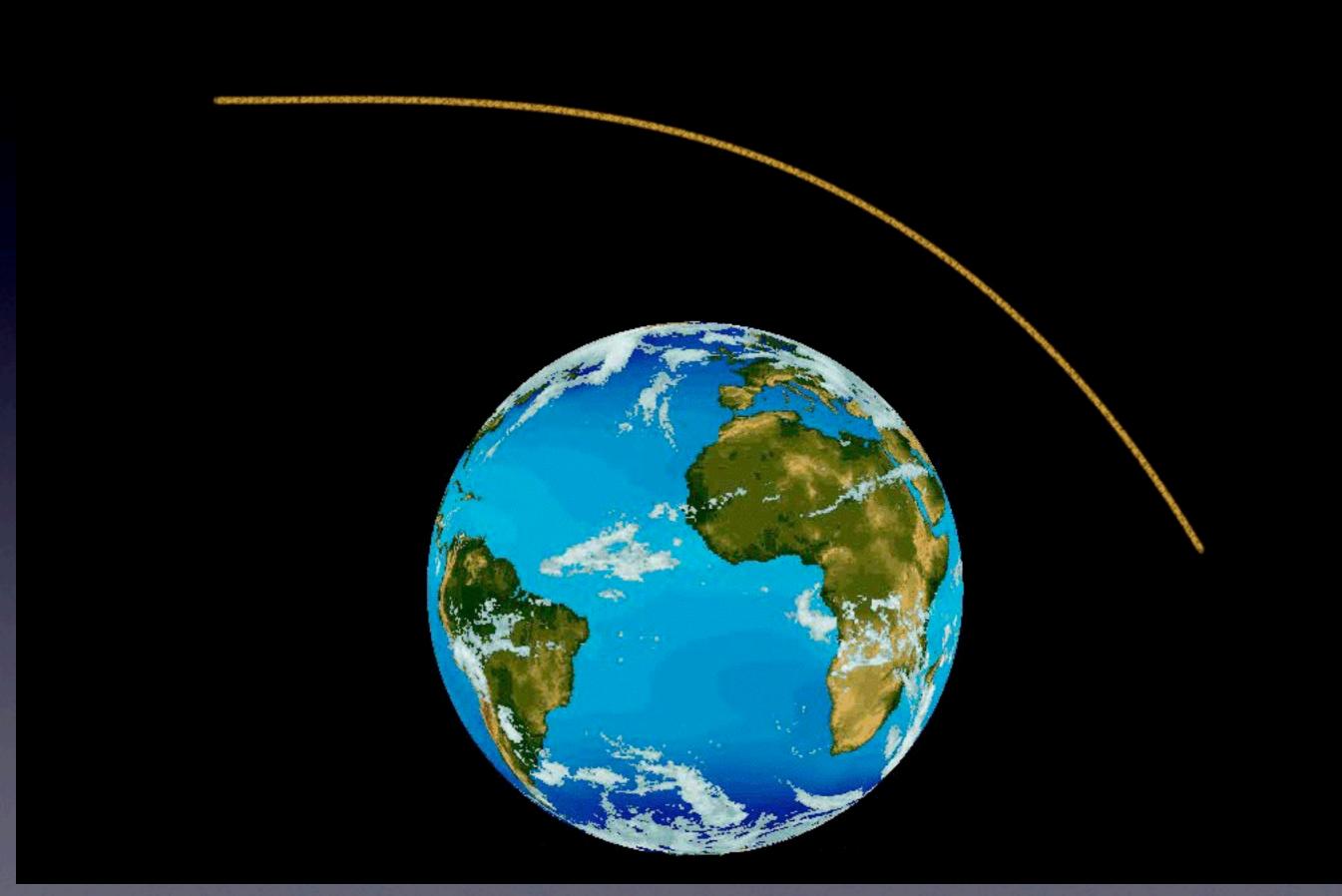


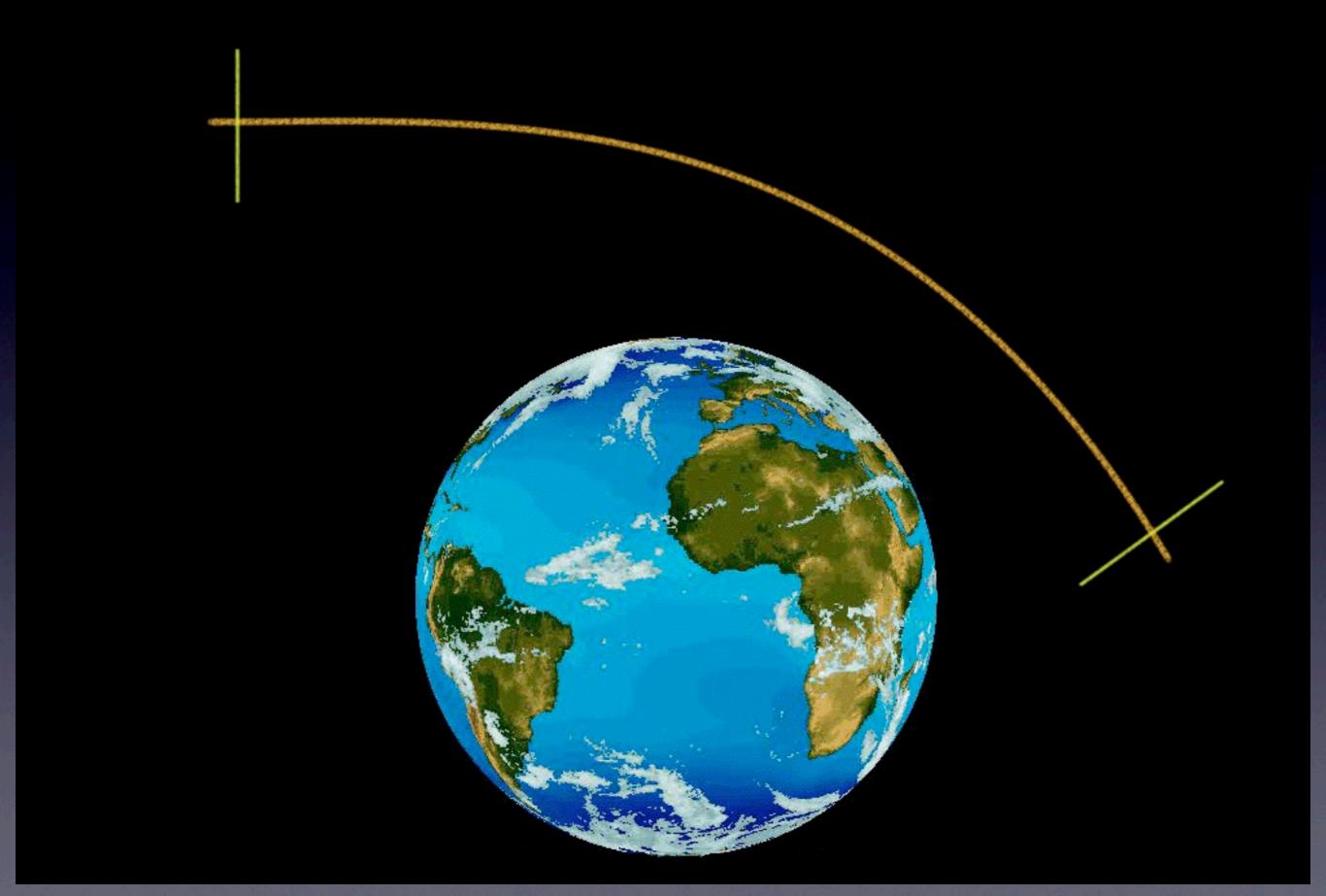


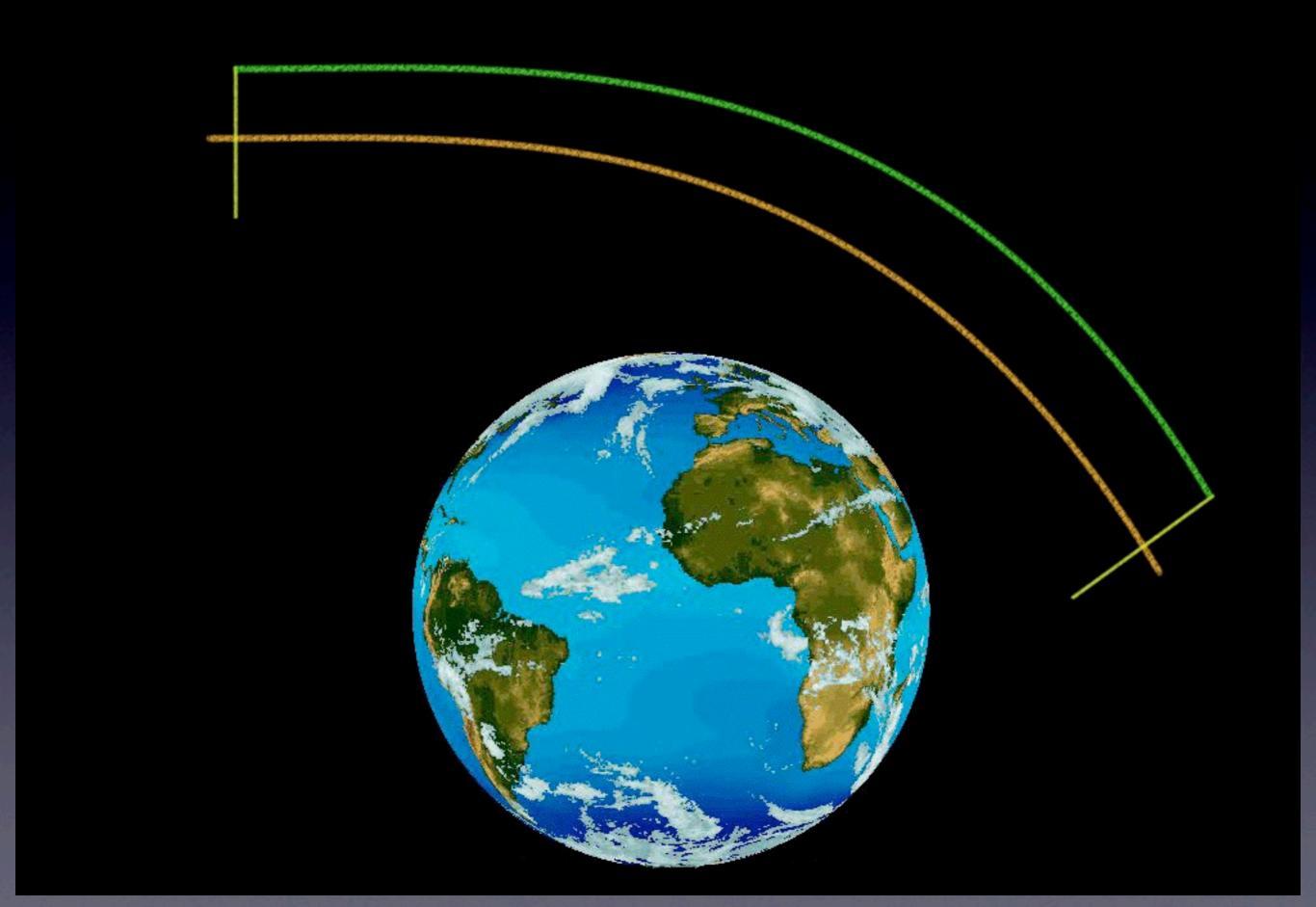


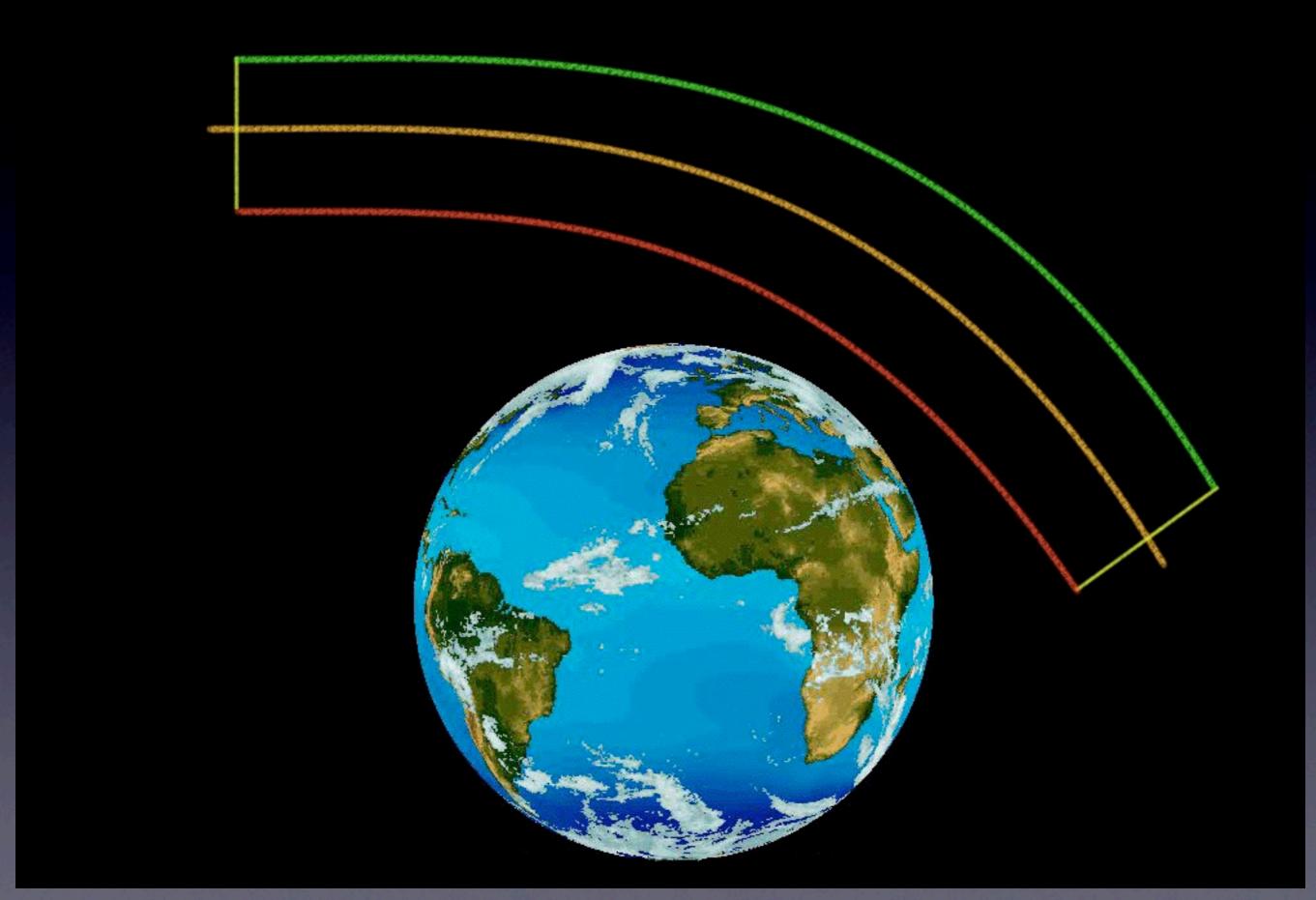


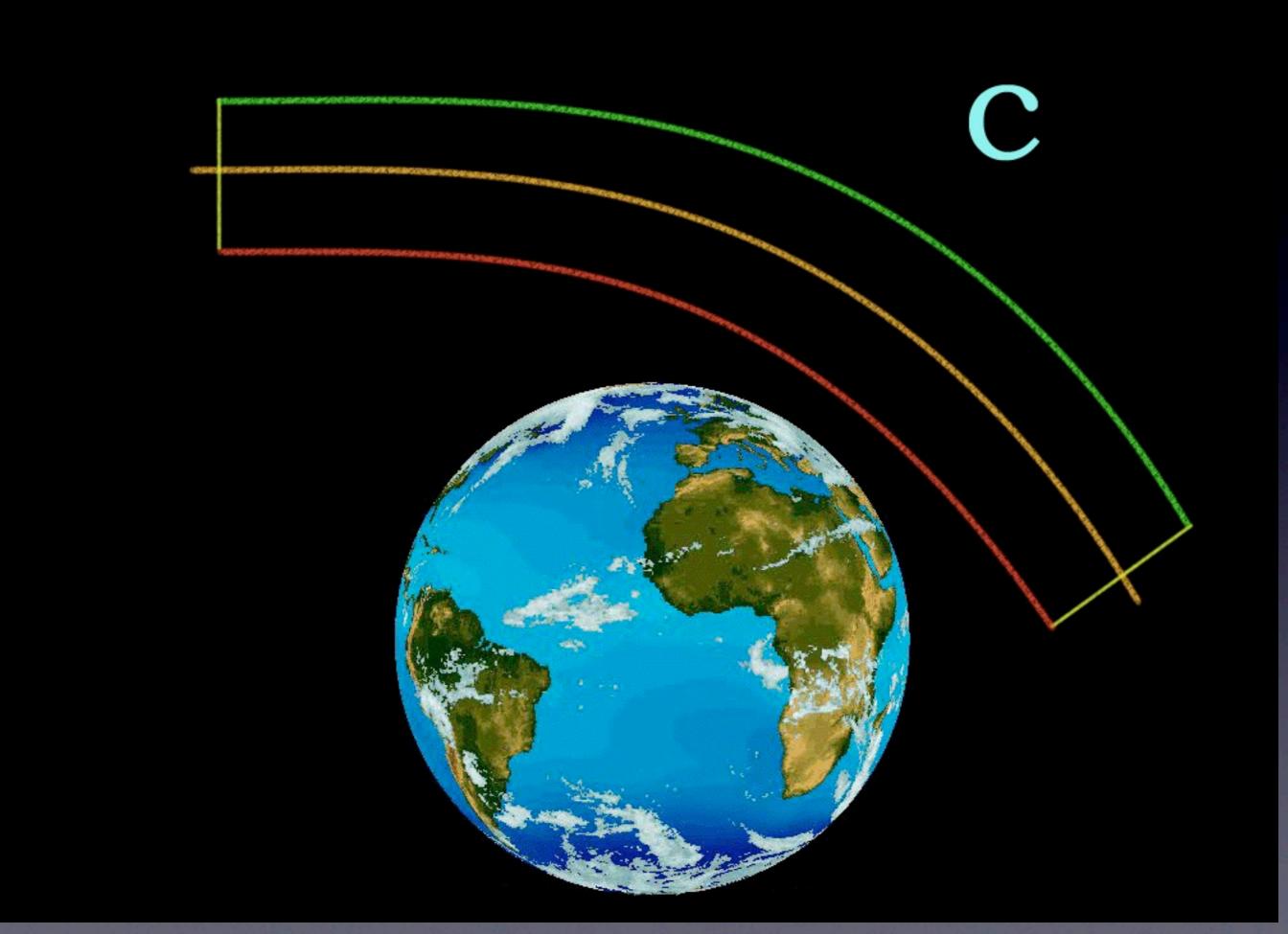






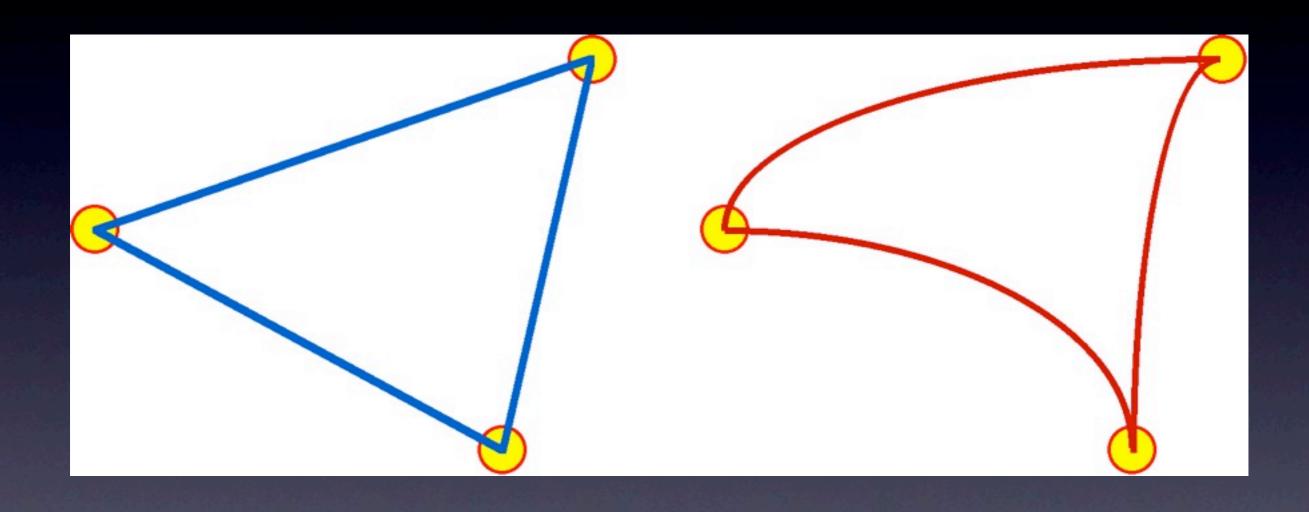


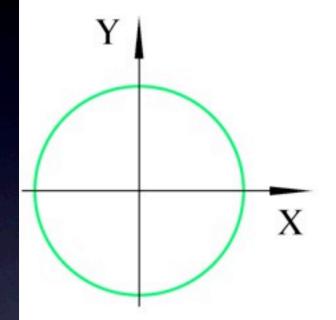


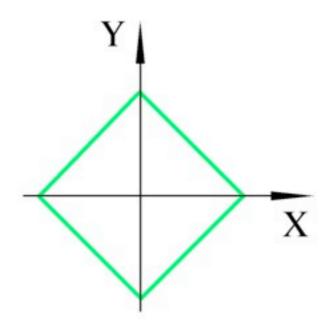


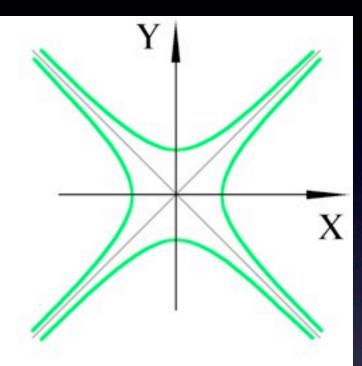
Towards the Einstein Equation

- Relativistic behaviour
 - ♦ Metric theory, metric tensor
 - ♦ Second-order derivatives
 - ♦ Connection with Newton -> Einstein Eqs
- The connection with Lagrangian theory: local Lorentz symmetry





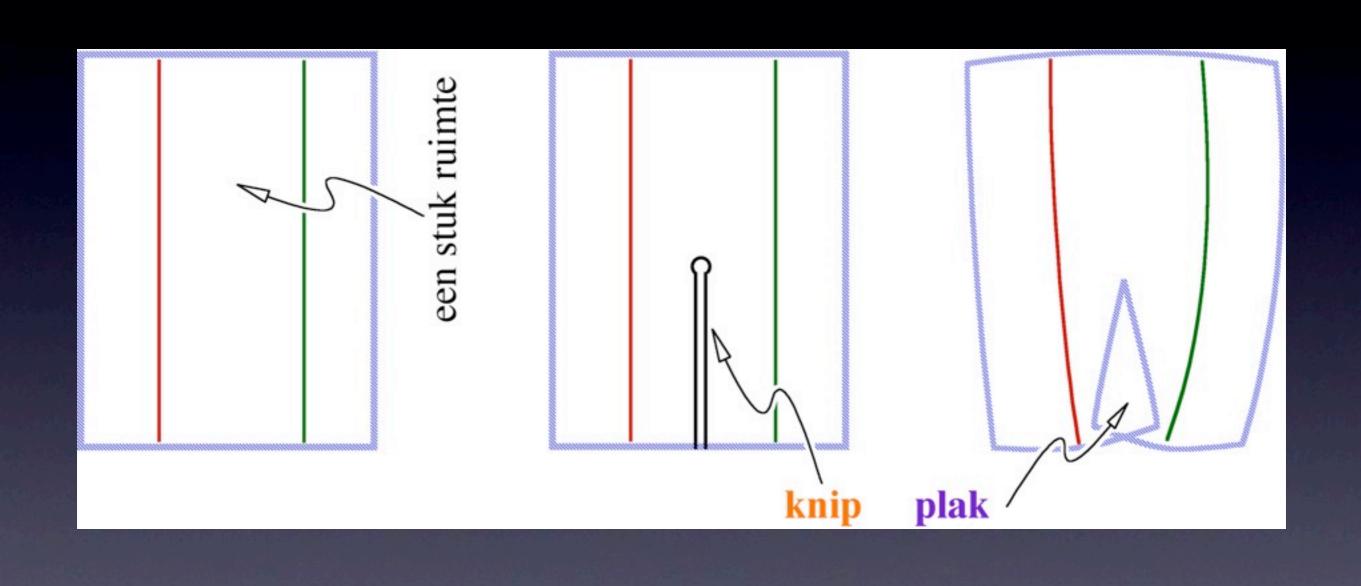


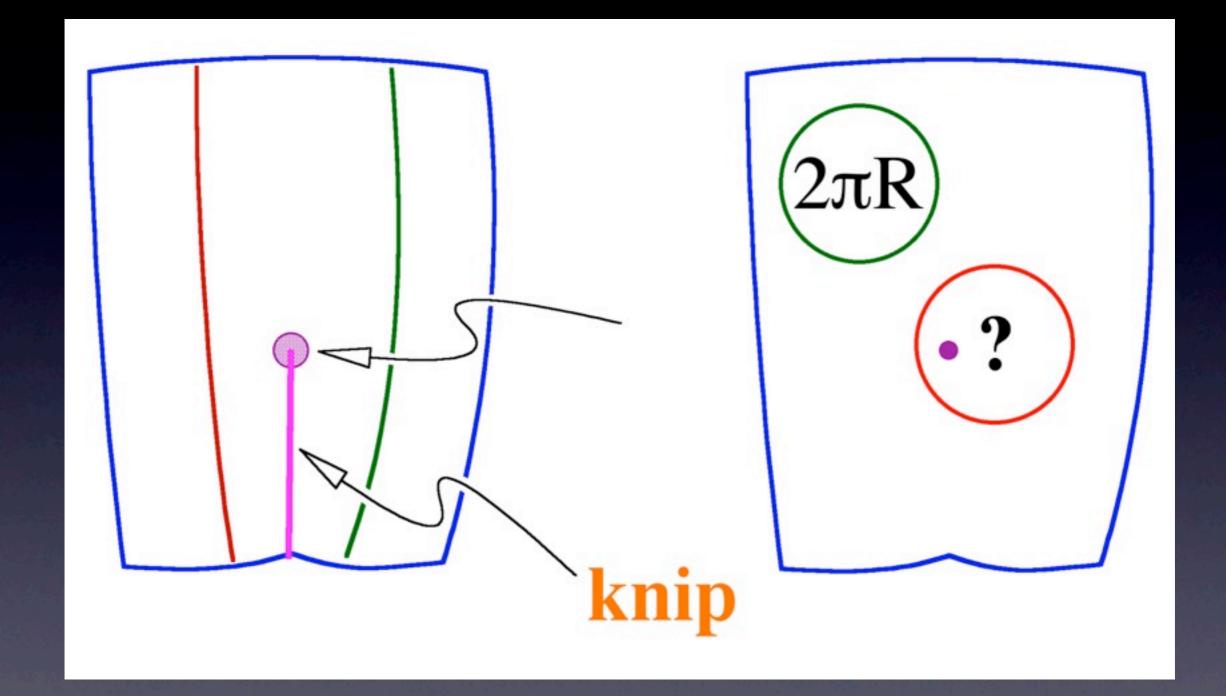


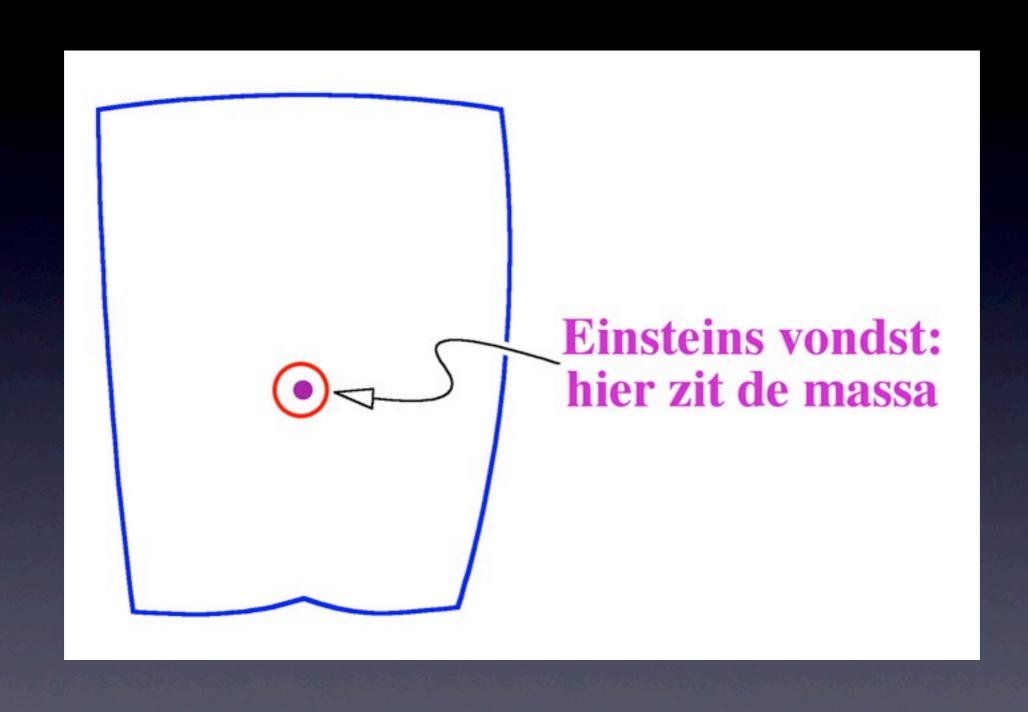
$$S^{2} = X^{2} + Y^{2}$$
Pythagoras

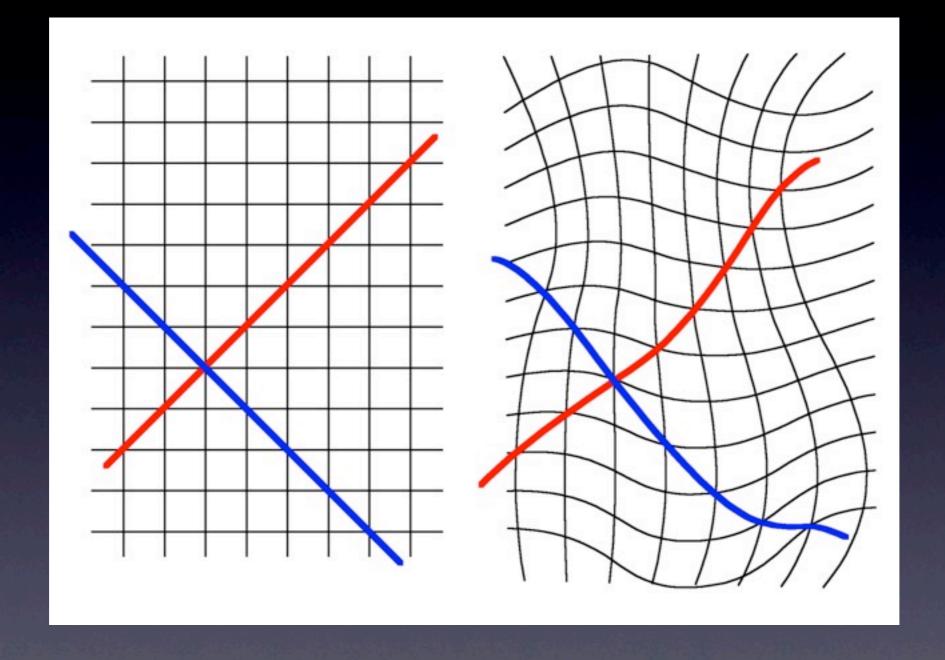
$$S = |X| + |Y|$$
Manhattan

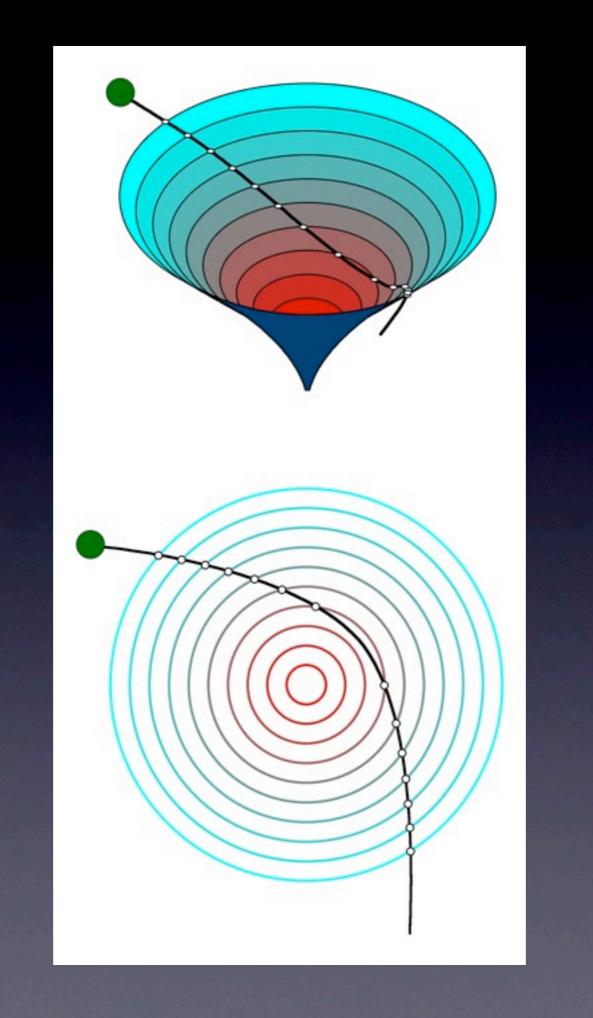
$$S^2 = X^2 - Y^2$$
Minkowski

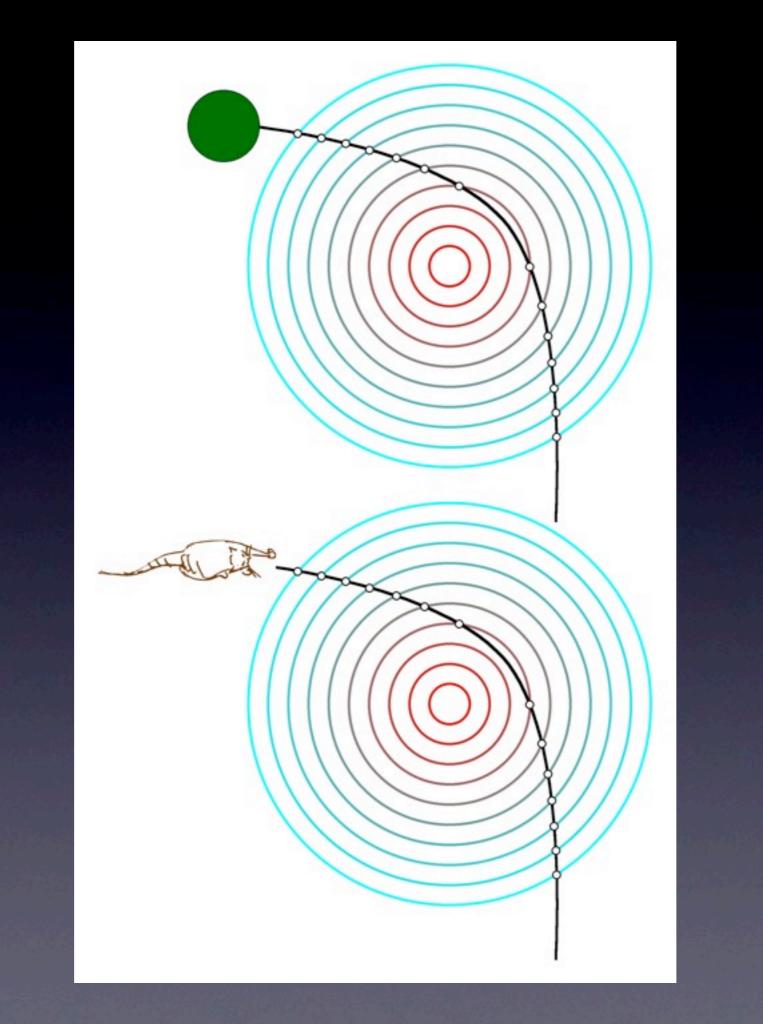


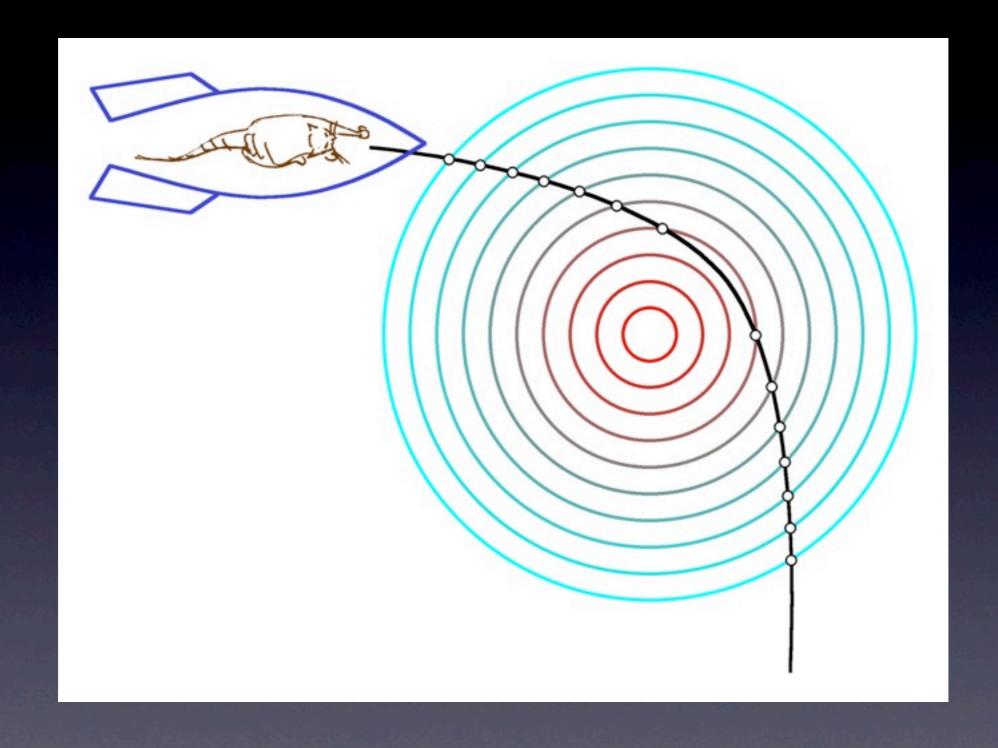












Einstein Equation

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} - \Lambda g_{\mu\nu} = 8\pi G T_{\mu\nu}$$

Sterrewacht Leiden

Friedmann Equations

$$\left(\frac{da}{dt}\right)^{2} = \frac{8\pi}{3}G\rho a^{2} - kc^{2} + \frac{\Lambda}{3}a^{2}$$

$$\frac{d}{dt}\left(\rho a^{3}\right) + \frac{P}{c^{2}}\frac{da^{3}}{dt} = 0$$

Preview of the solutions

- Present epoch
- Ionized plasma
- Relativistic plasma
- Quantum plasma?
- Evolution of mass scales, looking ahead to interpretation of CMBR observations